

Quasi-PDFs with twisted mass fermions

Constantia Alexandrou^{ab}, Krzysztof Cichy^{*c}, Martha Constantinou^d, Kyriakos Hadjiyiannakou^b, Karl Jansen^e, Aurora Scapellato^c, Fernanda Steffens^f

^a*Department of Physics, University of Cyprus, P.O. Box 20537, 1678 Nicosia, Cyprus*

^b*Computation-based Science and Technology Research Center, Cyprus Institute, 20 Kavafi Str., Nicosia 2121, Cyprus*

^c*Faculty of Physics, Adam Mickiewicz University, Uniwersytetu Poznańskiego 2, 61-614 Poznań, Poland*

E-mail: kcichy@amu.edu.pl

^d*Temple University, 1925 N. 12th Street, Philadelphia, PA 19122, USA*

^e*John von Neumann Institute for Computing (NIC), DESY, Platanenallee 6, D-15738 Zeuthen, Germany*

^f*Institut für Strahlen- und Kernphysik, Rheinische Friedrich-Wilhelms-Universität Bonn, Nussallee 14-16, 53115 Bonn*

We discuss the recent progress in extracting partonic functions from the quasi-distribution approach, using twisted mass fermions. This concerns, among others, the investigation of several sources of systematic effects. Their careful analysis is a prerequisite to obtain precise determinations of PDFs from the lattice with realistic estimates of all uncertainties. In these proceedings, we shortly discuss systematic effects in the matching procedure. Moreover, we present preliminary results from our new simulations at the physical point. They involve, additionally, the dynamical strange and charm quarks, as well as a larger volume and a smaller lattice spacing than in our previous computations. In addition, we show first results from computations of generalized parton distributions (GPDs) in the quasi-distribution framework.

*37th International Symposium on Lattice Field Theory - Lattice2019
16-22 June 2019
Wuhan, China*

^{*}Speaker.

1. Introduction

Recent years have witnessed a tremendous progress in calculations of partonic distribution functions from first principles. For a long time, lattice computations were restricted to the lowest 2-3 moments of parton distribution functions (PDFs) or generalized parton distributions (GPDs). The situation changed with the advent of Ji's proposal [1] to calculate quasi-distributions, objects related to the desired light-cone distributions and computable on the lattice. Quasi-distributions share the same infrared physics with their light-cone counterparts and the difference in the ultraviolet can be subtracted using perturbation theory, in the so-called matching procedure. The approach has been very vigorously explored theoretically and numerically, see e.g. Refs. [2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29] for published studies concerning PDFs of the nucleon, including renormalizability, concrete renormalization prescriptions, matching, nucleon mass corrections, finite volume effects, higher-twist effects and lattice simulations with non-physical and finally physical quark masses. The quasi-distribution approach was also applied to other hadrons, see e.g. Refs. [30, 31, 32], and other direct approaches for extracting the x -dependence of partonic functions were also pursued, e.g. Refs. [33, 34, 35, 36, 37, 38, 39, 40]. For an extensive review of recent activities in this field, we refer to Refs. [41, 42].

2. Theoretical and lattice setup

Starting with the renormalized matrix elements $h_{\Gamma}^{\overline{\text{MMS}}}(z, P_3) = Z^{\overline{\text{MMS}}}(z) \langle P | \bar{\psi}(z) \Gamma W(z, 0) \psi(0) | P \rangle$ (where the nucleon momentum is $P = (P_0, 0, 0, P_3)$, $Z^{\overline{\text{MMS}}}(z)$ is the renormalization function in the $\overline{\text{MMS}}$ scheme [28], $W(z, 0)$ is the Wilson line of length z and Γ determines the type of PDF), one obtains quasi-PDFs as the Fourier transform with respect to z , $\tilde{q}^{\overline{\text{MMS}}}(x, P_3) = \int_{-\infty}^{+\infty} \frac{dz}{4\pi} e^{-ixP_3z} h_{\Gamma}^{\overline{\text{MMS}}}(z, P_3)$. We perform the computations for one ensemble of configurations, with $N_f = 2$ maximally twisted mass quarks with a clover term (MTM+clover), at the physical pion mass, with lattice size of $48^3 \times 96$ and lattice spacing $a = 0.0938(3)(2)$ fm. The nucleon is boosted to $\frac{6\pi}{L}$, $\frac{8\pi}{L}$ and $\frac{10\pi}{L}$ (0.83, 1.11, 1.38 GeV). The three-point functions entering the matrix elements are computed at four source-sink separations ($t_s = 0.75, 0.84, 0.93$ and 1.12 fm). The number of measurements at the largest t_s is 9600, 38250 and 72990 measurements (for our three boosts, respectively). For more details about the computation of the bare matrix elements and their renormalization functions, we refer to Ref. [28].

Thus computed quasi-PDFs differ from light-cone PDFs only in the UV region and this difference can be accounted for in perturbation theory, using a matching procedure. In this work, we use the matching formulae developed in Refs. [18, 28], for which the input quasi-PDF is expressed in the $\overline{\text{MMS}}$ scheme. The final step is to apply nucleon mass corrections, derived in Ref. [5].

3. Systematic effects in matching

In Ref. [28], we analyzed several systematic effects that appear at different stages of the computation. Here, we briefly discuss the ones at the level of the matching procedure, for the unpolarized PDFs case. However, the magnitudes of the considered effects in helicity and transversity PDFs were found to be very similar.

In Fig. 1 (upper left), we show the effect of taking into account the conversion factor between the $\overline{\text{MS}}$ scheme and the $\overline{\text{MMS}}$ scheme. In Refs. [18, 25], we used the matching formulae that require the input quasi-PDF renormalized in the $\overline{\text{MMS}}$ scheme, but the conversion factor $\overline{\text{MS}} \rightarrow \overline{\text{MMS}}$ was then unavailable. An explicit test of the effect of this conversion factor (derived in

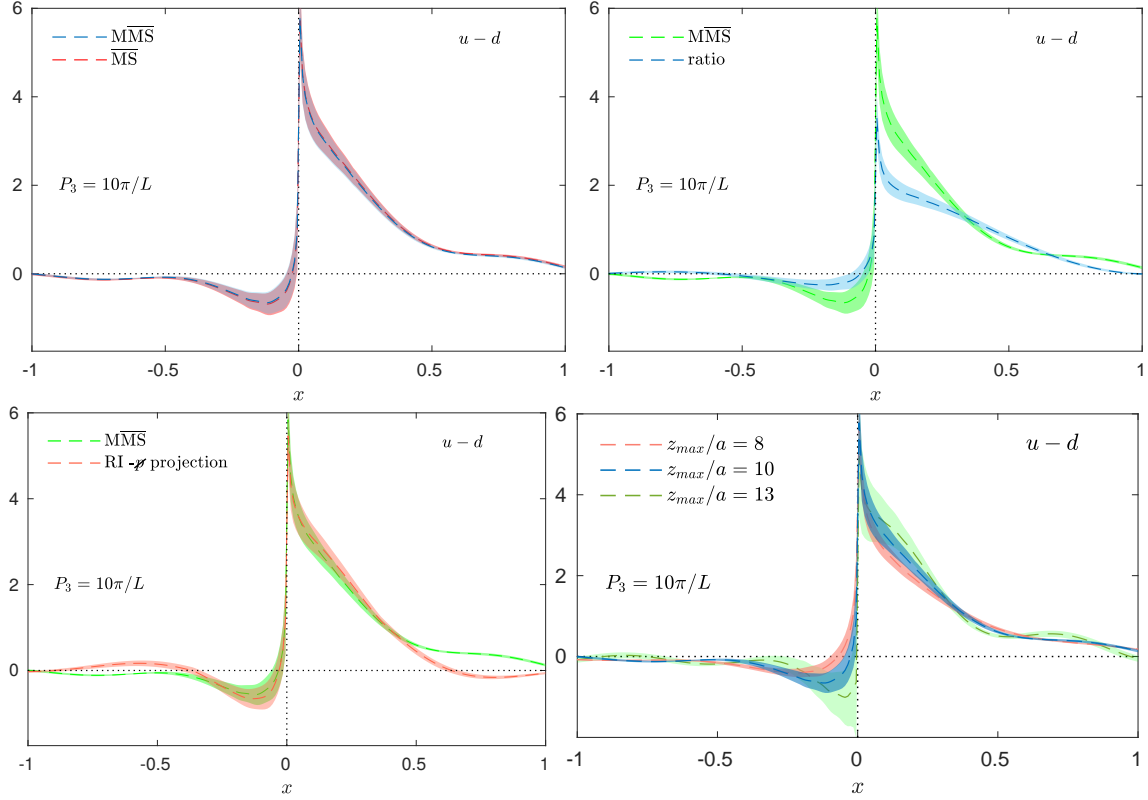


Figure 1: Selected tests of the matching procedure for the unpolarized PDF ($P_3 = 10\pi/L$). We show a comparison of the matched PDF in the $\overline{\text{MMS}}$ scheme and the $\overline{\text{MS}}$ scheme (top left), the ratio scheme (top right) and the RI scheme (bottom left). The bottom right plot illustrates the dependence of the $\overline{\text{MMS}} \rightarrow \overline{\text{MS}}$ matched PDF on the choice of the maximum z/a used in the Fourier transform.

Ref. [28]) confirmed the expectation that it is small, roughly an order of magnitude smaller than statistical errors. In the upper right and lower left panels of Fig. 1, we compare the matched PDFs obtained from $\overline{\text{MMS}} \rightarrow \overline{\text{MS}}$ matching formulae [28] and from $\text{ratio} \rightarrow \overline{\text{MS}}$ [17] and $\text{RI} \rightarrow \overline{\text{MS}}$ matching procedures [16]. All these formulae are equivalent, up to neglected higher-order perturbative effects. Since all of them are calculated only to one-loop level, the observed differences can be attributed to truncation effects. Hence, we find these are rather significant, both at low- x ($\overline{\text{MMS}}$ vs. ratio) and at high- x ($\overline{\text{MMS}}$ vs. RI). This necessitates the calculation of at least two-loop matching. Finally, we compare the effects of truncating the Fourier transform at different maximal lengths of the Wilson line, z_{max}/a . We observe that all reasonable choices for z_{max} lead to compatible results. However, as discussed in Ref. [27], the truncated and discretized Fourier transform is ill-defined and advanced reconstruction methods need to be applied in the future.

4. Preliminary results for an $N_f = 2 + 1 + 1$ ensemble

One of our recent research directions involves computations of quasi-PDFs for another ensemble of configurations, with $N_f = 2 + 1 + 1$ MTM+clover quarks at the physical pion mass, larger volume $64^3 \times 128$ and a smaller lattice spacing, $a = 0.081$ fm. In Fig. 2, we present results at the nucleon boost $P_3 = 12\pi/L \approx 1.44$ GeV, obtained from 31770 measurements, and at three values of $t_s = 0.73, 0.89, 1.05$ fm. We do not observe significant excited states effects – for most values

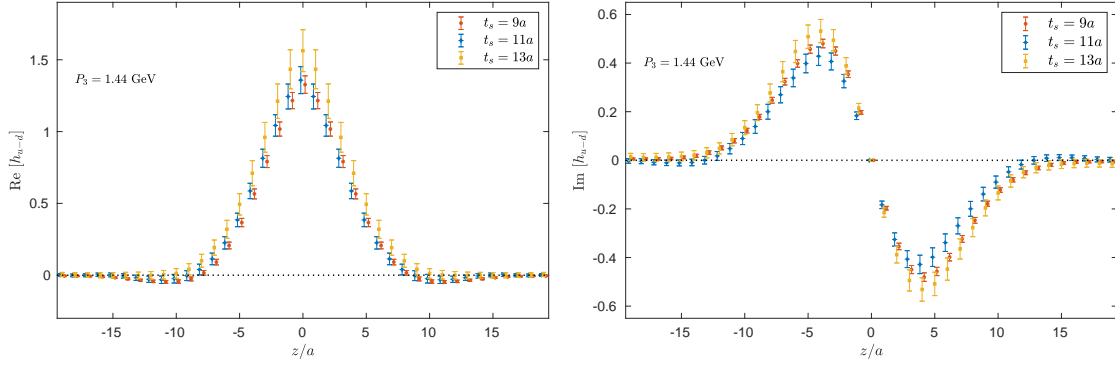


Figure 2: Preliminary results for the real (left) and imaginary (right) part of matrix elements for unpolarized quasi-PDFs. Three source-sink separations are used. Nucleon boost is 1.44 GeV. Ensemble: $N_f = 2 + 1 + 1$ MTM+clover quarks, physical pion mass, lattice size $64^3 \times 128$, $a = 0.081$ fm.

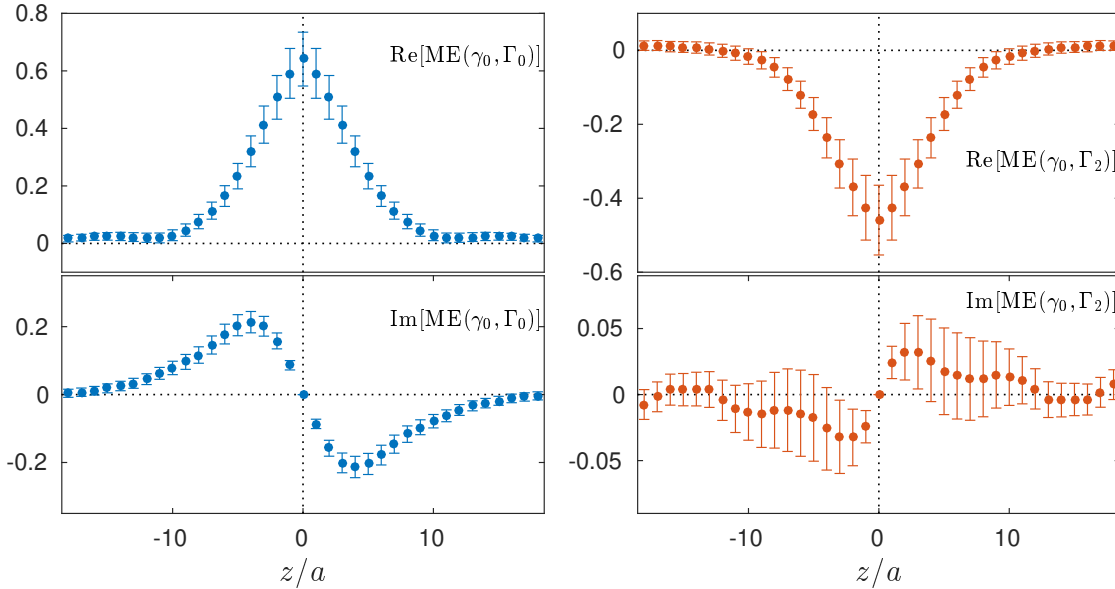


Figure 3: Preliminary results for the matrix elements for unpolarized quasi-GPDs. The upper/lower plots show the real/imaginary part. The left/right plots correspond to unpolarized/polarized projectors defined in the text. The average nucleon boost is 0.83 GeV, $\xi = 0$, $Q^2 = 0.69$ GeV². Ensemble: $N_f = 2 + 1 + 1$ MTM+clover quarks, $m_\pi \approx 270$ MeV, lattice size $32^3 \times 64$, $a = 0.094$ fm.

of z/a , in both the real and imaginary parts, matrix elements are compatible for all source-sink separations. Exceptions are small tensions at low- z between $t_s = 9a$ and $t_s = 13a$ (real part) and at intermediate- z for $t_s = 11a, 13a$ (imaginary part). We are currently increasing statistics for the largest two separations to clarify these effects and obtain statistical precision at the level of the one for $t_s = 9a$.

5. Preliminary results for quasi-GPDs

Another direction that we have been recently exploring is the computation of GPDs using the

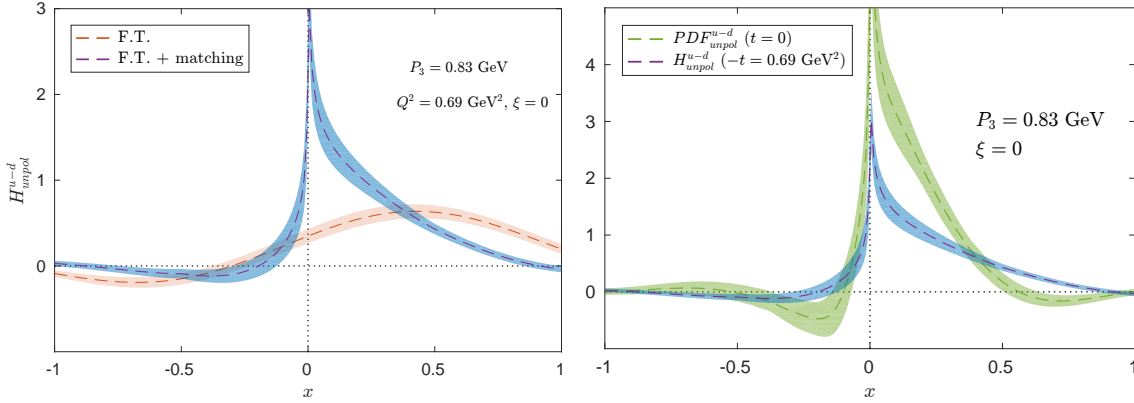


Figure 4: Left: the unpolarized H quasi-GPD and the matched H -GPD. Right: comparison of the unpolarized matched PDF and the H -GPD. The average nucleon boost is 0.83 GeV, for GPD: $\xi = 0$, $Q^2 = 0.69 \text{ GeV}^2$. Ensemble: $N_f = 2 + 1 + 1$ MTM+clover quarks, $m_\pi \approx 270 \text{ MeV}$, lattice size $32^3 \times 64$, $a = 0.094 \text{ fm}$.

quasi-distribution approach¹. Quasi-GPDs are defined analogously to quasi-PDFs, but they involve momentum transfer, $t = -Q^2$, between the initial and final hadron states. The Fourier transform of the underlying matrix elements is a combination of two (four) quasi-GPDs in the chiral-even (odd) case. In the chiral-even case, these are commonly denoted as H and E quasi-GPDs. They are functions of the Bjorken- x , the renormalization scale, the momentum transfer and the so-called quasi-skewness variable, $\xi = -Q_3/2P_3$, where a boost along the 3-direction is assumed and P_3 is the average momentum. Using different projectors, one can disentangle the two (four) contributions and subject them to matching to obtain their light-cone counterparts. For zero quasi-skewness, the matching is identical to the one for quasi-PDFs, while $\xi \neq 0$ implies different matching, as derived in Ref. [44]. Physically, $\xi \neq 0$ implies the existence of the so-called ERBL region ($|x| < \xi$).

Our lattice setup for this exploratory study involves $N_f = 2 + 1 + 1$ MTM+clover quarks at $m_\pi \approx 270 \text{ MeV}$, lattice size $32^3 \times 64$ and $a = 0.094 \text{ fm}$. We compute matrix elements for several nucleon boosts and momentum transfers, using $t_s \leq 12a$. In Fig. 3, we show bare matrix elements for unpolarized GPDs (920 measurements) at $P_3 = 0.83 \text{ GeV}$ ($\xi = 0$, $Q^2 = 0.69 \text{ GeV}^2$), using the unpolarized ($\Gamma_0 \equiv (1 + \gamma_0)/4$) and polarized ($\Gamma_2 \equiv (1 + \gamma_0)i\gamma_5\gamma_2/4$) projectors that allow us to disentangle the H and E functions. The left plot of Fig. 4 shows the Fourier transform of the RI-scheme renormalized matrix element corresponding to the H quasi-function and the matched H -GPD. In the right plot, a comparison of this GPD with the corresponding matched PDF obtained from the same ensemble and with the same nucleon boost. It is clear that the GPD is suppressed with respect to the PDF, as expected. The x -integral of the GPD gives the Pauli form factor F_1^{u-d} and the integral value we obtain, 0.62(8), is compatible with our renormalized matrix element (of the H function) at $z = 0$ (0.61(8)) and independent direct lattice extractions using local matrix elements at similar values of Q^2 . We are currently increasing statistics and computing various kinematic setups to obtain a large coverage of the (P_3, t, ξ) parameter space.

¹See also Ref. [43] for exploratory work about quasi-GPDs in the pion.

Acknowledgments

K.C. is supported by the National Science Centre grant SONATA BIS no. 2016/22/E/ST2/00013. This work has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement no. 642069 (HPC-LEAP). F.S. is funded by the Deutsche Forschungsgemeinschaft (DFG) project no. 392578569. M.C. acknowledges financial support by the U.S. Department of Energy (DoE), Office of Nuclear Physics, within the framework of the TMD Topical Collaboration, by the National Science Foundation under Grant No. PHY-1714407 for the work on quasi-PDFs, and by DoE under Grant No. DE-SC0020405 (Early Career) for the quasi-GPDs. This research used resources of the Oak Ridge Leadership Computing Facility, which is a DOE Office of Science User Facility supported under contract DE-AC05-00OR22725, Jülich Supercomputing Centre, Prometheus supercomputer at the Academic Computing Centre Cyfronet AGH in Cracow, Okeanos supercomputer at the Interdisciplinary Centre for Mathematical and Computational Modelling in Warsaw, Eagle supercomputer at the Poznan Supercomputing and Networking Center. Computations for the work on quasi-GPDs were carried out in part on facilities of the USQCD Collaboration, which are funded by the Office of Science of the U.S. Department of Energy.

References

- [1] X. Ji, *Parton Physics on a Euclidean Lattice*, *Phys.Rev.Lett.* **110** (2013) 262002, [[arXiv:1306.1539](#)].
- [2] X. Xiong, X. Ji, J.-H. Zhang, and Y. Zhao, *One-loop matching for parton distributions: Nonsinglet case*, *Phys.Rev.* **D90** (2014), no. 1 014051, [[arXiv:1310.7471](#)].
- [3] H.-W. Lin, J.-W. Chen, S. D. Cohen, and X. Ji, *Flavor Structure of the Nucleon Sea from Lattice QCD*, *Phys. Rev.* **D91** (2015) 054510, [[arXiv:1402.1462](#)].
- [4] C. Alexandrou, K. Cichy, V. Drach, E. Garcia-Ramos, K. Hadjiyiannakou, K. Jansen, F. Steffens, and C. Wiese, *Lattice calculation of parton distributions*, *Phys. Rev.* **D92** (2015) 014502, [[arXiv:1504.07455](#)].
- [5] J.-W. Chen, S. D. Cohen, X. Ji, H.-W. Lin, and J.-H. Zhang, *Nucleon Helicity and Transversity Parton Distributions from Lattice QCD*, *Nucl. Phys.* **B911** (2016) 246–273, [[arXiv:1603.06664](#)].
- [6] J.-W. Chen, X. Ji, and J.-H. Zhang, *Improved quasi parton distribution through Wilson line renormalization*, *Nucl. Phys.* **B915** (2017) 1–9, [[arXiv:1609.08102](#)].
- [7] C. Alexandrou, K. Cichy, M. Constantinou, K. Hadjiyiannakou, K. Jansen, F. Steffens, and C. Wiese, *Updated Lattice Results for Parton Distributions*, *Phys. Rev.* **D96** (2017), no. 1 014513, [[arXiv:1610.03689](#)].
- [8] R. A. Briceño, M. T. Hansen, and C. J. Monahan, *Role of the Euclidean signature in lattice calculations of quasidistributions and other nonlocal matrix elements*, *Phys. Rev.* **D96** (2017), no. 1 014502, [[arXiv:1703.06072](#)].
- [9] T. Ishikawa, Y.-Q. Ma, J.-W. Qiu, and S. Yoshida, *Renormalizability of quasiparton distribution functions*, *Phys. Rev.* **D96** (2017), no. 9 094019, [[arXiv:1707.03107](#)].
- [10] X. Ji, J.-H. Zhang, and Y. Zhao, *Renormalization in Large Momentum Effective Theory of Parton Physics*, *Phys. Rev. Lett.* **120** (2018), no. 11 112001, [[arXiv:1706.08962](#)].
- [11] M. Constantinou and H. Panagopoulos, *Perturbative renormalization of quasi-parton distribution functions*, *Phys. Rev.* **D96** (2017), no. 5 054506, [[arXiv:1705.11193](#)].
- [12] C. Alexandrou, K. Cichy, M. Constantinou, K. Hadjiyiannakou, K. Jansen, H. Panagopoulos, and F. Steffens, *A complete non-perturbative renormalization prescription for quasi-PDFs*, *Nucl. Phys.* **B923** (2017) 394–415, [[arXiv:1706.00265](#)].
- [13] X. Ji, J.-H. Zhang, and Y. Zhao, *More On Large-Momentum Effective Theory Approach to Parton Physics*, *Nucl. Phys.* **B924** (2017) 366–376, [[arXiv:1706.07416](#)].
- [14] W. Wang, S. Zhao, and R. Zhu, *Gluon quasidistribution function at one loop*, *Eur. Phys. J.* **C78** (2018), no. 2 147, [[arXiv:1708.02458](#)].
- [15] J. Green, K. Jansen, and F. Steffens, *Nonperturbative Renormalization of Nonlocal Quark Bilinears for Parton Quasidistribution Functions on the Lattice Using an Auxiliary Field*, *Phys. Rev. Lett.* **121** (2018), no. 2 022004, [[arXiv:1707.07152](#)].
- [16] I. W. Stewart and Y. Zhao, *Matching the Quasi Parton Distribution in a Momentum Subtraction Scheme*, [arXiv:1709.04933](#).
- [17] T. Izubuchi, X. Ji, L. Jin, I. W. Stewart, and Y. Zhao, *Factorization Theorem Relating Euclidean and Light-Cone Parton Distributions*, *Phys. Rev.* **D98** (2018), no. 5 056004, [[arXiv:1801.03917](#)].
- [18] C. Alexandrou, K. Cichy, M. Constantinou, K. Jansen, A. Scapellato, and F. Steffens, *Light-Cone Parton Distribution Functions from Lattice QCD*, *Phys. Rev. Lett.* **121** (2018), no. 11 112001, [[arXiv:1803.02685](#)].
- [19] R. A. Briceño, J. V. Guerrero, M. T. Hansen, and C. J. Monahan, *Finite-volume effects due to spatially nonlocal operators*, *Phys. Rev.* **D98** (2018), no. 1 014511, [[arXiv:1805.01034](#)].

- [20] G. Spanoudes and H. Panagopoulos, *Renormalization of Wilson-line operators in the presence of nonzero quark masses*, *Phys. Rev.* **D98** (2018), no. 1 014509, [arXiv:1805.01164].
- [21] A. V. Radyushkin, *Structure of parton quasi-distributions and their moments*, arXiv:1807.07509.
- [22] J. Karpie, K. Orginos, and S. Zafeiropoulos, *Moments of Ioffe time parton distribution functions from non-local matrix elements*, arXiv:1807.10933.
- [23] Y.-S. Liu, J.-W. Chen, L. Jin, H.-W. Lin, Y.-B. Yang, J.-H. Zhang, and Y. Zhao, *Unpolarized quark distribution from lattice QCD: A systematic analysis of renormalization and matching*, arXiv:1807.06566.
- [24] H.-W. Lin, J.-W. Chen, X. Ji, L. Jin, R. Li, Y.-S. Liu, Y.-B. Yang, J.-H. Zhang, and Y. Zhao, *Proton Isovector Helicity Distribution on the Lattice at Physical Pion Mass*, *Phys. Rev. Lett.* **121** (2018), no. 24 242003, [arXiv:1807.07431].
- [25] C. Alexandrou, K. Cichy, M. Constantinou, K. Jansen, A. Scapellato, and F. Steffens, *Transversity parton distribution functions from lattice QCD*, *Phys. Rev. D. (Rapid Communication)*, in production, (2018) [arXiv:1807.00232].
- [26] V. M. Braun, A. Vladimirov, and J.-H. Zhang, *Power corrections and renormalons in parton quasidistributions*, *Phys. Rev.* **D99** (2019), no. 1 014013, [arXiv:1810.00048].
- [27] J. Karpie, K. Orginos, A. Rothkopf, and S. Zafeiropoulos, *Reconstructing parton distribution functions from Ioffe time data: from Bayesian methods to Neural Networks*, *JHEP* **04** (2019) 057, [arXiv:1901.05408].
- [28] C. Alexandrou, K. Cichy, M. Constantinou, K. Hadjiyiannakou, K. Jansen, A. Scapellato, and F. Steffens, *Systematic uncertainties in parton distribution functions from lattice QCD simulations at the physical point*, *Phys. Rev.* **D99** (2019), no. 11 114504, [arXiv:1902.00587].
- [29] K. Cichy, L. Del Debbio, and T. Giani, *Parton distributions from lattice data: the nonsinglet case*, *JHEP* **10** (2019) 137, [arXiv:1907.06037].
- [30] J.-H. Zhang, J.-W. Chen, L. Jin, H.-W. Lin, A. Schäfer, and Y. Zhao, *First direct lattice-QCD calculation of the x -dependence of the pion parton distribution function*, *Phys. Rev.* **D100** (2019), no. 3 034505, [arXiv:1804.01483].
- [31] T. Izubuchi, L. Jin, C. Kallidonis, N. Karthik, S. Mukherjee, P. Petreczky, C. Shugert, and S. Syritsyn, *Valence parton distribution function of pion from fine lattice*, *Phys. Rev.* **D100** (2019), no. 3 034516, [arXiv:1905.06349].
- [32] Y. Chai et al., *Parton distribution functions of Δ^+ on the lattice*, 2019. arXiv:1907.09827.
- [33] A. V. Radyushkin, *Quasi-parton distribution functions, momentum distributions, and pseudo-parton distribution functions*, *Phys. Rev.* **D96** (2017), no. 3 034025, [arXiv:1705.01488].
- [34] K. Orginos, A. Radyushkin, J. Karpie, and S. Zafeiropoulos, *Lattice QCD exploration of parton pseudo-distribution functions*, *Phys. Rev.* **D96** (2017), no. 9 094503, [arXiv:1706.05373].
- [35] Y.-Q. Ma and J.-W. Qiu, *Exploring Partonic Structure of Hadrons Using ab initio Lattice QCD Calculations*, *Phys. Rev. Lett.* **120** (2018), no. 2 022003, [arXiv:1709.03018].
- [36] G. S. Bali, V. M. Braun, B. Gläbke, M. Göckeler, M. Gruber, F. Hutzler, P. Korcyl, A. Schäfer, P. Wein, and J.-H. Zhang, *Pion distribution amplitude from Euclidean correlation functions: Exploring universality and higher-twist effects*, *Phys. Rev.* **D98** (2018), no. 9 094507, [arXiv:1807.06671].
- [37] R. S. Sufian, J. Karpie, C. Egerer, K. Orginos, J.-W. Qiu, and D. G. Richards, *Pion Valence Quark Distribution from Matrix Element Calculated in Lattice QCD*, *Phys. Rev.* **D99** (2019), no. 7 074507, [arXiv:1901.03921].
- [38] B. Joó, J. Karpie, K. Orginos, A. Radyushkin, D. Richards, and S. Zafeiropoulos, *Parton Distribution Functions from Ioffe time pseudo-distributions*, arXiv:1908.09771.
- [39] A. V. Radyushkin, *Generalized Parton Distributions and Pseudo-Distributions*, arXiv:1909.08474.
- [40] B. Joó, J. Karpie, K. Orginos, A. V. Radyushkin, D. G. Richards, R. S. Sufian, and S. Zafeiropoulos, *Pion Valence Structure from Ioffe Time Pseudo-Distributions*, arXiv:1909.08517.
- [41] K. Cichy and M. Constantinou, *A guide to light-cone PDFs from Lattice QCD: an overview of approaches, techniques and results*, *Adv. High Energy Phys.* **2019** (2019) 3036904, [arXiv:1811.07248].
- [42] C. Monahan, *Recent Developments in x -dependent Structure Calculations*, *PoS LATTICE2018* (2018) 018, [arXiv:1811.00678].
- [43] J.-W. Chen, H.-W. Lin, and J.-H. Zhang, *Pion generalized parton distribution from lattice QCD*, arXiv:1904.12376.
- [44] Y.-S. Liu, W. Wang, J. Xu, Q.-A. Zhang, J.-H. Zhang, S. Zhao, and Y. Zhao, *Matching generalized parton quasidistributions in the RI/MOM scheme*, *Phys. Rev.* **D100** (2019), no. 3 034006, [arXiv:1902.00307].