

## Inclusive $B_s \rightarrow D_s X$ decays with $B_s$ semi-leptonic tagging at Belle

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We present an analysis of the inclusive decay  $B_s \rightarrow D_s X$  tagged with semi-inclusive decay  $B_s \rightarrow D_s X l \nu$ , where  $X$  denotes a final state that may consist of additional hadrons or photons and  $l$  is an electron or muon. The analysis methods are demonstrated and the results with generic MC are shown in this proceedings.

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## 1. Introduction

Study of the  $B_s$  meson properties at the  $\Upsilon(5S)$  resonance, together with those of the lighter  $B^0$  and  $B^+$  decays, may provide important insights into the CKM matrix and hadronic structure, as well as sensitivity to new physics phenomena [1, 2, 3]. The branching fraction of the inclusive decay  $B_s \rightarrow D_s X$  plays an important role for the determination of the  $B_s$  production rate in the  $\Upsilon(5S)$  decays. The measurement of the  $B_s$  production rate  $f_s$  is necessary to compare with theoretical models of b-hadron production.

Two experiments, ALEPH [4] and OPAL [5] from LEP, have measured the combined branching fraction of  $B(\bar{b} \rightarrow B_s^0) \cdot B(B_s^0 \rightarrow D_s X)$ . By using  $B(\bar{b} \rightarrow B_s^0)$  from theory predictions, the branching fraction  $B(B_s^0 \rightarrow D_s X)$  has been measured, although with large uncertainties from statistics and theory. Belle has measured the branching fraction of  $\Upsilon(5S) \rightarrow D_s X$  [6] with data of  $1.86 \text{ fb}^{-1}$  collected near the  $\Upsilon(5S)$  energy.

The average branching fraction of the previous measurements is  $(93 \pm 25) \%$  from PDG 2018 [7]. The methods these measurements used are not direct measurements, and their results depend on other measurements and have large uncertainties. In this proceedings, we present a direct measurement of  $B_s \rightarrow D_s X$  decay using a  $B_s$  semi-leptonic tagging method.

We use the data sample of  $121.4 \text{ fb}^{-1}$  that was collected with the Belle detector [8] at the KEKB asymmetric-energy  $e^+e^-$  collider [9] operating near the  $\Upsilon(5S)$  resonance. The Belle detector is a general purpose large-solid-angle spectrometer consisting of a silicon vertex detector (SVD), a central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. Outside the coil, an iron flux-return yoke is instrumented to detect  $K_L^0$  mesons and to identify muons (KLM). A detailed description of the detector can be found in Ref. [8].

## 2. Analysis Strategy

In this analysis, the  $B_s$  semi-leptonic decay  $B_s \rightarrow D_s X l \nu$  is used to tag  $B_s^0 \bar{B}_s^0$  events. Particles in one event are separated to two sides: tag side and signal side.

In the tag side,  $D_s$  is reconstructed with two decay modes:  $D_s^\pm \rightarrow \phi \pi^\pm$ ,  $\phi \rightarrow K^+ K^-$  and  $D_s^\pm \rightarrow K_S^0 K^\pm$ ,  $K_S^0 \rightarrow \pi^+ \pi^-$ . Other than the  $D_s$  meson, a charged lepton ( $e$  or  $\mu$ ) is also reconstructed. The missing mass square of  $B_s \rightarrow D_s X l \nu$ , ( $l = e$  or  $\mu$ ) is used to tag the  $B_s$  meson:

$$M_{miss}^2 = (E_{Beam}^* - E_{D_s l}^*)^2 - p_{D_s l}^{*2}, \quad (2.1)$$

where  $E_{Beam}^* = \frac{\sqrt{s}}{2}$ . The energy and momentum of the  $D_s$  and lepton system are used in the calculation of missing mass square ( $E_{D_s l}^*$  and  $p_{D_s l}^*$ ). The number of tagged ( $N_{tag}$ ) events is obtained by fitting the missing mass square distribution using shapes determined via MC.

In the signal side, one  $D_s$  is constructed by using the same decay modes selection rules for tag side  $D_s$  with one additional decay mode  $D_s^\pm \rightarrow K^{*0} K^\pm$ ,  $K^{*0} \rightarrow K^\pm \pi^\mp$  to increase signal statistics. It should also have no shared charged tracks with the tag side tracks. The number of signal events ( $N_{sig}$ ) is obtained by fitting the  $D_s$  invariant masses in tag side and signal side, together with the missing mass square after the signal side event selection.

The branching fraction of  $B_s \rightarrow D_s X$  can be calculated as:

$$B(B_s \rightarrow D_s X)_{measured} = \frac{N_{sig}}{N_{tag} \cdot \epsilon_{rec}}, \quad (2.2)$$

where  $\epsilon_{rec}$  is the signal side  $D_s$  reconstruction efficiency.

In this analysis, the tagging mode,  $B_s \rightarrow D_s l \nu X$ , is part of the signal mode,  $B_s \rightarrow D_s X$ . The following correction needs to be applied to the measured branching fraction:

$$B(B_s \rightarrow D_s X) = \frac{(2 - B_{semi}) \cdot B_{meas} + B_{semi}}{2}, \quad (2.3)$$

where  $B_{meas}$  is the directly measured result of  $B(B_s \rightarrow D_s X)$ , and  $B_{semi}$  is the branching ratio of  $B_s$  semi-leptonic decay  $B(B_s \rightarrow D_s l \nu X) = (16.2 \pm 2.6)\%$  ( $l = e, \mu$ ) [7].

### 3. Event Selection

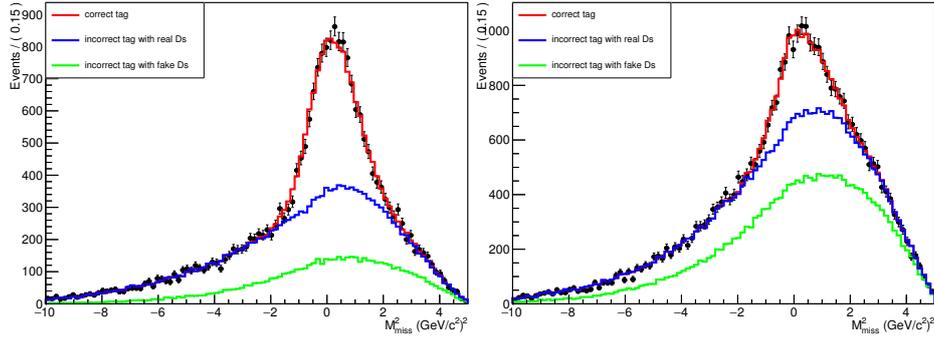
The charged tracks, except those from  $K_S$  decay, are required to originate from the interaction point (IP) and have the point of closest approach to the IP within 2.0 cm along the beam axis and 0.5 cm in the plane transverse to the beam. Additionally, all tracks should have at least one associated hit in the plane transverse to the beam and two hits along the beam axis within the SVD detector. Kaon and pion hypotheses are assigned to the tracks based on the likelihood combining the information from Belle sub-detectors. The leptons should have a minimum momentum of 1.0 GeV in the center of mass frame. The standard Belle lepton identification requirements are used to further select lepton candidates.

The neutral intermediate particles,  $\phi, K_S^0$  or  $K^{*0}$ , are reconstructed with the selected charged tracks. For  $\phi$  reconstruction, any two oppositely charged kaons with invariant mass within  $\pm 15$  MeV of the  $\phi$  nominal mass are considered as a  $\phi$  candidate. For  $K^{*0}$ , the candidate tracks are oppositely charged  $K$  and  $\pi$ , and the invariant mass window is  $\pm 20$  MeV. The  $K_S^0$  candidates are selected with a standard method in Belle and the invariant mass cut of  $\pm 50$  MeV is applied.

The  $D_s$  meson is reconstructed by using the reconstructed intermediate particles,  $\phi, K^{*0}$  and  $K_S^0$ , and one  $\pi$  meson for  $\phi$ , or one  $K$  meson for  $K^{*0}$  or  $K_S^0$ . The reconstructed  $D_s$  should pass the vertex fit and the invariant mass should be within  $\pm 50$  MeV which corresponds to  $7.5 \sigma$ . The momentum of the reconstructed  $D_s$  in the center of mass system  $P_{D_s}^*$  is required to be within the 0.5 GeV/c – 3.0 GeV/c range. For  $\phi\pi$  and  $K^{*0}K$  decay modes, a vertex fit is performed for the four tracks used to reconstruct the  $D_s$  meson and the  $\chi^2$  of the fit output should be less than 100.

To suppress combinatorial background, the helicity angle for  $D_s \rightarrow \phi(K^+K^-)\pi$  and  $D_s \rightarrow K^{*0}(K\pi)K$  is required as  $|\cos \theta_{hel}| > 0.5$ . The thrust angle, which is defined as the angle between the thrust axis of the selected tag side  $D_s$  and lepton and another thrust axis of the remaining tracks in the event, is required as  $|\cos \theta_{thrust}| < 0.8$  in this analysis. To further suppress continuum background, we require that the event shape variable  $R_2$ , which is the ratio of second to zeroth Fox-Wolfram moments [10], satisfy  $R_2 < 0.4$ .

After the previous  $D_s$  and lepton reconstruction, sometimes there are more than one possible  $D_s$  and lepton combinations. To select one candidate per event, we perform a vertex fit on the tracks forming the  $D_s$  candidate and choose the one giving the smallest  $\chi^2$  as the  $D_s$  tag.



**Figure 1:** Fitting results of the missing mass square for  $\phi\pi$  tag mode (left) and  $K_S^0 K$  tag mode (right). The red lines for real tag. The blue lines are fake tag with real  $D_s$ . The green lines are fake tag with fake  $D_s$ .

After tagging, we reconstruct an additional  $D_s$  from the remainder of the event. The selection criteria are the same as with the tag side  $D_s$ . To increase statistics, one more  $D_s$  decay channel,  $D_s \rightarrow K^{*0} K, K^{*0} \rightarrow K\pi$ , is used. We allow none of the tracks of the  $B_s$  tag candidate, the tagging  $D_s$  and charged lepton, to be used to reconstruct the  $D_s$  signal candidate.

The signal side  $D_s$  reconstruction efficiency  $\epsilon_{rec}$  is defined as the the number of reconstructed  $D_s$ ,  $N_{rec}$ , over the total number of  $D_s$  in the signal side,  $N_{tot}$ . This efficiency is obtained from signal MC sample and it varies only slightly over the tag side  $D_s$  momentum range of 0.5 GeV/c to 3.0 GeV/c.

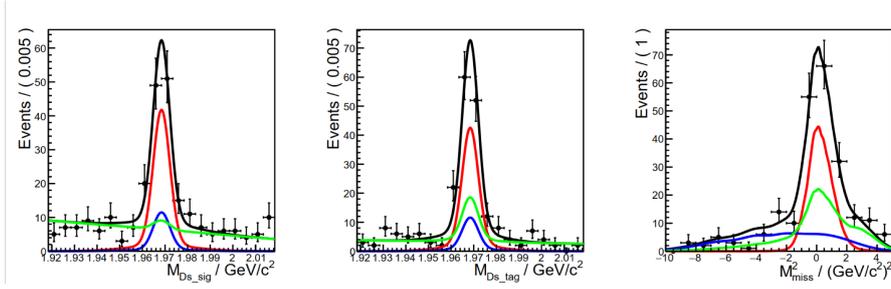
#### 4. Tagging and Fitting

After the tag side  $D_s$  and lepton candidate has been selected, the number of tags events can be extracted by fitting the missing mass square distribution. The tag side missing mass square is defined in 2.1. The selected candidates can be grouped into three categories: real tag events in which the  $D_s$  is correctly reconstructed and combined with the correct lepton; fake tag events with correct  $D_s$  in which the  $D_s$  is correctly reconstructed but combined with the wrong lepton and fake tag events with wrong  $D_s$  in which the  $D_s$  is wrongly reconstructed, which is combinatorial background.

The shapes of the missing mass square distributions for these three categories are obtained from the generic MC samples. By fitting the missing mass square distributions, we can extract the number of tagged events in  $Y(5S)$  data taken by Belle, as shown in Figure 1.

We can extract the number of signal  $D_s$  in  $D_s l$  tag candidate events with a 3D fit. The three fitting variables are: the invariant mass of signal side  $D_s$ ; the invariant mass of tag side  $D_s$  and the missing mass calculated by using tag side  $D_s$  and lepton ( $\mu$  or  $e$ ). The mass of the signal  $D_s$  distribution has two contributions: the corrected reconstructed  $D_s$  and the incorrectly reconstructed  $D_s$ .

For both the tag and signal side  $D_s$  mass, we model the distributions with double Gaussians with a common mean. The widths for each Gaussian and their relative areas are obtained from the signal MC. For incorrectly reconstructed  $D_s$  signal, their invariant mass distribution is modeled as first order linear polynomial. The missing mass distributions for the three tag side categories are



**Figure 2:** 1D projections of results from 3D signal fitting, all  $D_s$  modes combined: data (points with error bars), signal (red), cross-feed (green), background (blue), and total PDF(black).

obtained from signal and generic MC. There are three contributions to the tag side distribution and two the signal side distribution which lead to six distinct contributions to the 3D PDF distribution.

In the fitting procedure, the cross feed events are considered as signal to increase the statistics. The cross feed events are defined as both tag side and signal side  $D_s$  are correctly reconstructed but the tag side lepton is associated with the wrong  $D_s$ . But if we swap the two  $D_s$  by combining lepton with signal side  $D_s$ , the event can be considered as signal event, because signal side  $D_s$  and lepton are decaying from the same  $B_s$  in this case. The relative ratio of the cross feed events respect to the signal events is obtained from the MC samples and can be used in the fitting. The results of signal fitting is shown in Figure 2.

## 5. Results and Conclusions

Applying previous selection rules and fitting procedures to 6 streams of Belle generic MC samples for  $\Upsilon(5S)$  decays, we can get the branching fraction of  $B_s \rightarrow D_s X$  as  $(78.5 \pm 2.5) \%$ . After the correction defined in Eq. 2.3, the corrected branching fraction is  $(80.2 \pm 2.5) \%$ , which is consistent with the truth value in the MC sample  $(81.36 \pm 0.01) \%$ . The analysis with full  $\Upsilon(5S)$  data taken by Belle is still on-going.

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