The precision study of the 125 GeV Higgs boson offers a new window into the search for new physics beyond the Standard Model. To confront the predictions of models with new interactions, the experimental program should be designed to achieve 1% precision over the full spectrum of Higgs boson couplings, with minimal model-dependence in the analysis and with tight control of systematic errors. In this contribution, we will explain how a precision Higgs program with these capabilities can be achieved at the proposed International Linear Collider. We will compare the capabilities of the ILC to those of the high-luminosity LHC and those of other $e^+e^-$ Higgs factory proposals.
1. Introduction

The discovery of Higgs-like boson with a mass of $\sim 125$ GeV [1, 2] fulfilled one of the most important pieces of particle physics. However, there are still many open questions like the existence of dark matter which cannot be explained by the Standard Model (SM), we need new physics beyond the SM. This newly discovered boson would be a window to uncover new physics. Many new physics models predict the deviation from the SM, and the typical size of the deviation from the SM is estimated to be small, a few % to $\sim 10\%$ [3]. To observe such a small deviation, we need very precise measurements of the Higgs boson.

The International Linear Collider (ILC) is one of the proposed future $e^+e^-$ project. Its center-of-mass energy ($\sqrt{s}$) starts from 250 GeV which is suitable for the precision Higgs measurements, but it is upgradable up to 1 TeV. The polarized beams will be used at the ILC; 80% for electrons and 30% for positrons. In this contribution, we will discuss the precision measurements of the Higgs boson at the ILC, mainly based on the Ref. [4].

2. Higgs Measurements at the ILC

We have evaluated the precision of Higgs measurements based on the full detector simulation of the International Large Detector (ILD) concept and/or Silicon Detector (SiD) concept [5]. In this contribution, we pick up two analyses; recoil mass measurement and Higgs self-coupling measurement. Summary of the analysis and the measurements of individual Higgs decay mode can be found in Ref. [4].

2.1 Recoil Mass Measurement

The key measurement of the Higgs boson at lepton colliders is the measurement of the absolute size of an inclusive cross section $\sigma_{Zh}$ by applying the recoil technique to $e^+e^- \rightarrow Zh$ process. Figure 1 left shows the Feynman diagram of $e^+e^- \rightarrow Zh$ process with the decay of $Z \rightarrow \mu^+\mu^-$. Since the initial state of $e^+e^-$ collision is well-defined, the mass of the Higgs boson can be determined by only measuring muon momenta, without looking at any Higgs decay products. Figure 1 right shows the spectrum of recoil mass taken from Ref. [6]. This recoil technique is also applicable for $Z \rightarrow e^+e^-$ and $Z \rightarrow q\bar{q}$ decay mode and has been analyzed [6, 7]. Assuming the twenty years running scenario of the ILC with beam polarization sharing [8, 9, 10], the mass of the Higgs boson can be measured with a precision of 14 MeV, and $\sigma_{Zh}$ can be determined with 0.7% precision.

2.2 Higgs Self-Coupling Measurement

The measurement of trilinear Higgs self-coupling is quite important because this measurement allows testing the Higgs mechanism by measuring the Higgs potential directly. However, this measurement is very challenging due to its small cross section and the interference. The cross section of $e^+e^- \rightarrow Zhh$ at $\sqrt{s} = 500$ GeV is only $\sim 0.2$ fb$^{-1}$. Figure 2 shows the Feynman diagrams of Higgs pair production; several diagrams that do not involve trilinear Higgs coupling. Full simulation studies at $\sqrt{s} = 500$ GeV are performed by using $e^+e^- \rightarrow Zhh$ process with $Z \rightarrow q\bar{q}/\nu\bar{\nu}/\ell^+\ell^-$ and $hh \rightarrow b\bar{b}b\bar{b}/b\bar{b}WW^*$ channels. With 4 ab$^{-1}$ statistics, a precision of 16.8% can be achieved on the cross section measurement of $e^+e^- \rightarrow Zhh$ [11, 12, 13]. Assuming the...
Figure 1: Left: Feynman diagram of $e^+e^- \rightarrow Zh$ with $Z \rightarrow \mu^+\mu^-$. Right: Recoil mass spectrum of events in the signal region 110-155 GeV at $\sqrt{s} = 250$ GeV. Taken from Ref. [6].

Figure 2: Diagrams contributing to (a) $e^+e^- \rightarrow Zhh$ and (b) $e^+e^- \rightarrow \nu\nu hh$.

SM with only the trilinear self-coupling free, this corresponds to an uncertainty of 27% on that coupling. At $\sqrt{s} = 1$ TeV, the process $e^+e^- \rightarrow \nu\nu hh$ becomes dominant channel. With $8 \text{ ab}^{-1}$ data, the studies [12, 13, 14] show that, in the same context of varying the trilinear Higgs coupling only, this coupling can be determined to 10%.

Since some new physics models, in particular, electroweak baryogenesis models, predict large deviations of the trilinear Higgs coupling, it is important to see how the expected precisions would change in such cases. Figure 3 left shows the cross sections of the two reactions as a function of the triple Higgs coupling $\lambda$, and Figure 3 right shows the expected precisions at the ILC. Since the interference is different for the two reactions, constructive for $e^+e^- \rightarrow Zhh$ but destructive for $e^+e^- \rightarrow \nu\nu hh$, these two reactions are complementary in determining trilinear Higgs coupling. If the trilinear Higgs coupling is a factor of 2 larger than SM value, the $e^+e^- \rightarrow Zhh$ process gets very useful and would provide $\sim 15\%$ precision for the trilinear Higgs coupling.
3. Higgs Couplings — Observables to Couplings

To extract Higgs boson couplings, we use dimension-6 SM Effective Field Theory (EFT) formalism. We use Higgs observables, triple gauge coupling observables, and electroweak precision observables as the inputs to the global fit under the EFT framework. We additionally use the ratio of branching ratio from the HL-LHC prospects as the inputs. Details of the precisions of observables and EFT framework can be found in Refs. [4, 15, 16], here we only present the important remarks and results. The Lagrangian used in this EFT framework is Lorentz invariant, gauge invariant, and CP conserving. Though this Lagrangian has 23 free parameters, it is possible to determine all these parameters simultaneously. The Higgs couplings can be extracted in a highly model-independent way in the sense that all models of new physics describable either by the addition of local operators to the SM EFT or by the addition of invisible and exotic Higgs decays are included. In the global fitting, not only the statistical uncertainties but also systematic uncertainties have been considered [4]. Figure 4 shows the results of global fitting. Already at $\sqrt{s} = 250$ GeV stage, many couplings are reached to $\sim 1\%$ precision.

In Figure 5, a comparison has been made between polarized beams and unpolarized beams. When we compare the results of “2 ab$^{-1}$ 250 GeV polarized” and of “5 ab$^{-1}$ 250 GeV unpolarized”, there are no drastic differences. In general, higher statistics always help to improve precision. However, beam polarization allows us to have more independent measurements and have better control of systematics. These facts give us more constraints in the global fitting, which is another factor of the improvement. The beam polarization is a very powerful tool, essentially compensates for a factor of 2.5 luminosity.

Finally, we compare the capabilities of the ILC for precision Higgs measurements to those of the HL-LHC, and it is shown in Figure 6. Since the assumptions for extracting Higgs couplings are different at the LHC and the ILC, we have included two additional assumptions in our EFT framework: assume no Beyond-Standard-Model decay of Higgs boson, and no anomalous couplings in $hWW$ and $hZZ$. Even with the scenario S1, HI-LHC plus ILC250, most of the couplings are reached $\sim 1\%$ precision, and we can robustly claim discovery of deviations from the SM of the

Figure 3: Left: the cross section as a function of $\lambda$ for $e^+e^- \rightarrow Zhh$ and for $e^+e^- \rightarrow \nu\bar{\nu}hh$, where values of both $\lambda$ and $\sigma$ are scaled to their SM values. Right: expected precisions of $\lambda$ when $\lambda$ deviates from its SM value. Taken from Ref. [4].
Figure 4: Projected Higgs boson coupling uncertainties for the ILC program at 250 GeV and an energy upgrade to 500 GeV, using the highly model-independent analysis. S1* is the results based on current full simulation, and S2* is the expected results assuming improvements in analysis techniques and tools [4]. Taken from Ref. [4].

size generally expected in new physics models.

4. Summary

In this contribution, we have discussed the capabilities of measuring Higgs couplings at the ILC with two examples. The key measurement of Higgs boson at lepton colliders is the measurement of $\sigma_{Zh}$ using the recoil technique. At the ILC, the mass of Higgs boson can be measured with the precision of 14 MeV, and the $\sigma_{Zh}$ can be determined with 0.7% precision. The measurement of trilinear Higgs self-coupling is also discussed. It is possible to determine the Higgs couplings in a highly model-independent way under the EFT framework at the ILC, and most of the couplings are reached $\sim 1\%$ precision even at $\sqrt{s} = 250$ GeV stage. The beam polarization is a very powerful tool, essentially compensates a factor of $\sim 2.5$ luminosity. A comparison has been made for the prospects with HL-LHC, there are huge improvements in many Higgs couplings by adding the ILC data set.

References


Figure 5: Projected Higgs boson coupling uncertainties for the ILC program at 250 GeV and an energy upgrade to 500 GeV, using the highly model-independent analysis. Taken from Ref. [4].

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Figure 6: Projected Higgs boson coupling uncertainties for the LHC and ILC using the model-dependent assumptions appropriate to the LHC Higgs coupling fit. HL-LHC S1 is the prospects by CMS, and S2 is ATLAS and CMS. HL-LHC plus ILC S1 is the result based on current full simulation, and S2 is the expected results assuming improvements in analysis techniques and tools \cite{4}. Taken from Ref. \cite{4}.

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