

Beyond the Standard Model, guided by Lepton Universality

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We discuss the current status of lepton flavour universality observables in semileptonic charged and neutral current B meson decays. We recapitulate the current experimental situation. Assuming the current tensions with the SM are of beyond the Standard Model origin we present their implications for the effective theory couplings. Then we discuss general leptoquark models before finally focussing on the model with two scalar leptoquarks (R_2 and S_3) which have couplings connected by the underlying Grand Unified Theory framework. We present the viability of the model with regard to lepton flavour universality and present opportunities to search for this model in future high-intensity and high-energy experiments.

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1. Introduction

The Standard Model, our best theory describing the basic constituents and their interactions, has passed so far all the challenges posed by the numerous tests performed at high-energy and high-intensity experiments. The flavour sector of the Standard Model (SM) is the richest in number of parameters describing fermion masses and mixing parameters among them. The flavour and CP-violating effects have been confirmed by the B -factories to conform to the Cabibbo-Kobayashi-Maskawa (CKM) framework. We do know SM is superseded by some BSM model due to several shortcomings: unexplained neutrino masses, breakdown of the theory at the Planck scale, and possibly the lack of dark matter particle. There are also conceptual issues such as the electroweak hierarchy problem and puzzling hierarchies in masses and mixings. The measurements at future B -meson experiments can further challenge the flavour sector by making careful tests of the SM predictions.

The observables that test lepton flavour universality (LFU) have been essential in SM validation. Violation of a large flavour symmetry of the SM is confined to the Yukawa sector. According to the SM pattern of Yukawas lepton flavours are conserved and are treated universally by gauge bosons. Only Higgs Yukawas and masses separate charged lepton flavours. In LFU ratios we compare decay widths or cross sections which differ only in charged lepton flavour. The gauge and CKM factors cancel out in the ratio, whereas hadronic physics parameters entering processes, such as decay constants and form factors, cancel in processes with two body final states and the LFU ratio can be expressed as a function of particle masses. In processes with (≥ 3)-body kinematics the dependence on form factors is partially cancelled and vanishes in the limit where lepton masses can be neglected.

The persistent hints of violation of the LFU predictions in the SM have been reported in semileptonic B meson decays. In charged-current decay $B \rightarrow D^{(*)} \ell \nu$ the two ratios $R_{D^{(*)}} = \mathcal{B}(B \rightarrow D^{(*)} \tau \nu) / \mathcal{B}(B \rightarrow D^{(*)} \ell \nu)$, with $\ell = e, \mu$ have been measured by BaBar, Belle, while LHCb experiment measured $R_{D^{(*)}}$. The current world average (WA) of $R_{D^{(*)}}$ measurements by HFLAV [55] is based on experimental results [56, 57, 58, 59, 60, 61, 62, 63, 64] and exhibits more than 3σ tension of SM with the data:

$$\left. \begin{aligned} R_D^{\text{WA}} &= 0.340(27)(13) \\ R_{D^*}^{\text{WA}} &= 0.295(11)(8) \end{aligned} \right\} \text{Corr}(R_D^{\text{WA}}, R_{D^*}^{\text{WA}}) = -0.38, \quad \begin{aligned} R_D^{\text{SM}} &= 0.299(3), \\ R_{D^*}^{\text{SM}} &= 0.258(5). \end{aligned} \quad (1.1)$$

The above SM predictions refer to HFLAV average of results in [65, 66, 67, 68]. Here the large mass of the τ implies large LFU violation already in the SM. In rare semileptonic decays $B \rightarrow K \ell \ell$ where $\ell = e, \mu$ the SM contribution should respect LFU at $q^2 \gtrsim m_\mu^2$ and the ratios $R_{K^{(*)}} = \mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-) / \mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)$ are expected to be close to 1. The LHCb experiment measured $R_{K^{(*)}}$ at low invariant mass bin $[1.1, 6.0] \text{ GeV}^2$ of q^2 , R_{K^*} was measured also in the ultra low bin $[0.045, 1.1] \text{ GeV}^2$:

$$R_K^{\text{LHCb}} \Big|_{[1.1, 6] \text{ GeV}^2} = 0.846_{-0.054-0.014}^{+0.060+0.016} [69], \quad R_K^{\text{th}} \Big|_{[1.1, 6] \text{ GeV}^2} = 1.00 \pm 0.01 [70], \quad (1.2)$$

$$R_{K^*}^{\text{LHCb}} \Big|_{[1.1, 6] \text{ GeV}^2} = 0.69_{-0.07}^{+0.11} \pm 0.03 [71], \quad R_{K^*}^{\text{th}} \Big|_{[1.1, 6] \text{ GeV}^2} = 1.00 \pm 0.01 [70], \quad (1.3)$$

$$R_{K^*}^{\text{LHCb}} \Big|_{<1.1 \text{ GeV}^2} = 0.66_{-0.07}^{+0.11} \pm 0.03 [71], \quad R_{K^*}^{\text{th}} \Big|_{<1.1 \text{ GeV}^2} = 0.983 \pm 0.014 [70]. \quad (1.4)$$

The two experimental errors are split into statistical and systematic one, and are also given in that order. All three results have systematic errors well under control and are consistently below the SM predictions. The combined significance of about 4σ .

The two LFU ratios are currently our only potential hints of flavour effects beyond the SM. In this talk we explore what are the implications of lepton flavour universality hints for BSM scenarios.

2. Effective theory view

The weak effective Lagrangian for semileptonic decays is an appropriate framework to parameterize general BSM effects in $R_{D^{(*)}}$. At renormalization scale $\mu = m_b$ the relevant interactions for $b \rightarrow c\tau\bar{\nu}_\tau$ transitions are:

$$\begin{aligned} \mathcal{L}_{\text{SL}} = \frac{4G_F V_{cb}}{\sqrt{2}} & \left[(1 + g_{V_L})(\bar{c}_L \gamma^\mu b_L)(\bar{\tau}_L \gamma_\mu \nu_{\tau L}) + g_{V_R}(\bar{c}_R \gamma^\mu b_R)(\bar{\tau}_L \gamma_\mu \nu_{\tau L}) \right. \\ & \left. + g_{S_L}(\bar{c}_R b_L)(\bar{\tau}_R \nu_{\tau L}) + g_{S_R}(\bar{c}_L b_R)(\bar{\tau}_R \nu_{\tau L}) + g_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\tau}_R \sigma^{\mu\nu} \nu_{\tau L}) \right]. \end{aligned} \quad (2.1)$$

Here we will assume that BSM in $R_{D^{(*)}}$ does not contribute to $b \rightarrow c\ell\bar{\nu}_\ell$. Using the form factors from the lattice [72, 73, 74], and using further theoretical [66] and experimental results [21] the authors of Ref. [22] presented compact numerical expressions for $R_{D^{(*)}}$:

$$\begin{aligned} \frac{R_{D^{(*)}}}{R_{D^{(*)}}^{\text{SM}}} = 1 + a_S^{D^{(*)}} |g_{S_R} + g_{S_L}|^2 + a_P^{D^{(*)}} |g_{S_R} - g_{S_L}|^2 + a_T^{D^{(*)}} |g_T|^2 \\ + a_{S_V}^{D^{(*)}} \text{Re}[g_{S_R} + g_{S_L}] + a_{P_V}^{D^{(*)}} \text{Re}[g_{S_R} - g_{S_L}] + a_{T_V}^{D^{(*)}} \text{Re}[g_T]. \end{aligned} \quad (2.2)$$

Values of coefficients $a_i^{D^{(*)}}$ can be found in [22] or [23]. Using these coefficients it was found in Ref. [24] that the tensor (real g_T) scenario fits the data best, followed by the left-handed scenario (real g_{V_L}). The same authors also studied various leptoquark (LQ) scenarios with a combination of scalar and tensor coupling and found two LQ scenarios that accommodate the data: real $g_{S_L} = -4g_T$, or imaginary $g_{S_L} = 4g_T$, where both relations hold at the LQ scale and are modified by QCD renormalization at the scale m_b . Additional information is available in the q^2 shapes of decay spectra as shown by Ref. [25]. Belle experiment also measured in $B \rightarrow D^* \tau \nu$ the polarization of τ and longitudinal polarization [26] of D^* and the latter observable $F_L^{D^*, \text{Belle}} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{sys})$ is somewhat below the SM value 0.46 ± 0.04 [27] as well as below most of BSM models that fit $R_{D^{(*)}}$ well [27]. Furthermore, it was shown that various LQ models could be separated one from another by more precise measurement of the τ polarization [28]. Scalar interactions g_{S_L}, g_{S_R} could also severely disturb the branching fraction $B_c \rightarrow \tau \nu$. The latter can be constrained from the LEP data [29, 30] and together with the known B_c lifetime provide relevant constraint on $g_{S_R} - g_{S_L}$ [31, 23]. Naive scale of NP from $R_{D^{(*)}}$ can be inferred to be few TeV if the effective interactions (e.g. g_{V_L}) are assumed to be of order 1. Such large BSM effects might also generate dangerous effects via radiative corrections in precisely measured lepton decays, see e.g. [32, 33].

The $R_{K^{(*)}}$ anomalies and related measurements in $b \rightarrow s\mu^+\mu^-$ transitions are described at low energies with

$$\mathcal{L}_{b \rightarrow s\ell\ell} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=7,9,10,S,P} C_i \mathcal{O}_i, \quad (2.3)$$

where the most relevant operators for the anomalies are

$$\begin{aligned}
\mathcal{O}_9 &= \frac{e^2}{16\pi^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu} \gamma_\mu \mu), \\
\mathcal{O}_{10} &= \frac{e^2}{16\pi^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu} \gamma_\mu \gamma^5 \mu), \\
\mathcal{O}_S &= \frac{e^2}{16\pi^2} (\bar{s}_L b_R) (\bar{\mu} \mu), \\
\mathcal{O}_P &= \frac{e^2}{16\pi^2} (\bar{s}_L b_R) (\bar{\mu} \gamma^5 \mu).
\end{aligned} \tag{2.4}$$

The fits of $R_{K^{(*)}}$ indicate that left-handed scenario, $C_9 = -C_{10}$, gives a very good description of the data, where we have assumed SM-like couplings to the electrons. Furthermore, if we include many available observables of the $b \rightarrow s\ell\ell$ transitions from Belle, BaBar, and LHCb in the global fit we find that NP couplings to electrons are indeed not necessary, whereas there is strong indication for non-zero C_9 [34]. The scale of generic NP model with order 1 flavour changing neutral current couplings to explain the $R_{K^{(*)}}$ is few 10's of TeV. The requirement of perturbative unitarity in $qq \rightarrow \ell\ell$ scattering give the upper bound on the scale of $R_{K^{(*)}}$ to be $\lesssim 10$ TeV and $\lesssim 100$ TeV for BSM explaining $R_{D^{(*)}}$ [35].

3. Leptoquark models

Here we focus on the LQ mediators with suitable properties for $R_{D^{(*)}}$ and/or $R_{K^{(*)}}$. The phenomenological advantage of LQs is that their natural tree-level contribution are semi-leptonic processes whereas their SM charges do not allow for tree-level contributions to neutral meson mixing amplitudes. The latter are major obstacle to Z' models that address $R_{K^{(*)}}$. The recent phenomenological evaluation of LQs with respect to their role in LFU observables, flavour constraints, Z-pole observables, high- p_T constraints was undertaken in [24] and confirmed that vector leptoquark U_1 in the representation $(3, 1, 2/3)$ is the only LQ that explains all observed LFU. The U_1 has been proposed before [36] and was later embedded in a necessary UV completion, based on Pati-Salam unified groups for each generation [37, 38, 39] or in the context of 4321 model [40], among others. Ref. [24] found no appropriate scalar LQ for both LFU anomalies. S_3 with purely left-handed couplings can accommodate $R_{K^{(*)}}$ while R_2 and S_1 are suitable for $R_{D^{(*)}}$. At loop level R_2 has the desired Lorentz structure of couplings to explain $R_{K^{(*)}}$ but the needed couplings are in tension with LEP and LHC constraints [41, 42]. Here we focus on scenarios with two scalar LQs. One possibility is to take S_1 and S_3 which is the route described in [43] while here we will entertain the possibility to employ pair of R_2 and S_3 LQs.

4. R_2 and S_3 from Grand Unified Theory

The Yukawa couplings of R_2 and S_3 with the quarks and leptons in the mass basis can be

written as [44]

$$\begin{aligned} \mathcal{L}_{\text{Yuk}} = & (VY_R E_R^\dagger)^{ij} \bar{u}_{Li} \ell_{Rj} R_2^{\frac{5}{3}} + (Y_R E_R^\dagger)^{ij} \bar{d}_{Li} \ell_{Rj} R_2^{\frac{2}{3}} + (U_R Y_L U)^{ij} \bar{u}_{Ri} \nu_{Lj} R_2^{\frac{2}{3}} \\ & - (U_R Y_L)^{ij} \bar{u}_{Ri} \ell_{Lj} R_2^{\frac{5}{3}} + (Y_L U)^{ij} \bar{d}_{Li} \nu_{Lj} S_3^{\frac{1}{3}} - \sqrt{2} (V^* Y_L U)^{ij} \bar{u}_{Li}^C \nu_{Lj} S_3^{-\frac{2}{3}} \\ & + \sqrt{2} Y_L^{ij} \bar{d}_{Li}^C \ell_{Lj} S_3^{\frac{4}{3}} + (V^* Y_L)^{ij} \bar{u}_{Li}^C \ell_{Lj} S_3^{\frac{1}{3}}. \end{aligned} \quad (4.1)$$

Here Y_L, Y_R are the arbitrary LQ Yukawa matrices, $R_2^{(Q)}$ and $S_3^{(Q)}$ are LQ charge eigenstates of LQs. The unitary matrices $U_{L,R}, D_{L,R}, E_{L,R}$, and N_L rotate between mass and gauge basis of up-type quarks, down-type quarks, charged leptons, and neutrinos, respectively. $V \equiv U_L D_L^\dagger = U_L$ is the CKM matrix, $U \equiv E_L N_L^\dagger = N_L^\dagger$ is the PMNS matrix. The following numerical pattern is assumed for the Yukawa matrices:

$$Y_R E_R^\dagger = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_R^{b\tau} \end{pmatrix}, \quad U_R Y_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & y_L^{c\mu} & y_L^{c\tau} \\ 0 & 0 & 0 \end{pmatrix}, \quad (4.2)$$

where U_R is a rotation by angle θ between second and third generation. The parameters of the model are thus $m_{R_2}, m_{S_3}, y_R^{b\tau}, y_L^{c\mu}, y_L^{c\tau}$, and θ . In a low energy LQ setting there is no reason for the Yukawa couplings of S_3 to be related to the ones of R_2 . In our case we consider two leptoquarks within the $SU(5)$ based unification model where the scalar sector contains representations of dimension **45** and **50**. The SM fermions reside in $\bar{\mathbf{5}}_i$ and $\mathbf{10}_i$, with $i(=1,2,3)$ counting generations. All the low-energy operators of Eq. (4.1) can be generated with $SU(5)$ contractions $a^{ij} \mathbf{10}_i \bar{\mathbf{5}}_j \bar{\mathbf{45}}$, and $b^{ij} \mathbf{10}_i \mathbf{10}_j \mathbf{50}$, where a and $b(=b^T)$ are matrices in the flavour space. The former contraction couples $R_2 \in \mathbf{45}$ ($S_3 \in \mathbf{45}$) with the right-handed up-type quarks (quark doublets) and leptonic doublets, while the latter generates couplings of $R_2 \in \mathbf{50}$ with the quark doublets and right-handed charged leptons. To break $SU(5)$ down to the SM we use scalar representation **24** and write a term in the scalar potential $m \mathbf{45} \bar{\mathbf{50}} \mathbf{24}$. The two R_2 leptoquarks that reside in **45** and **50** then mix and allow us to have one light R_2 and one heavy R_2 in the spectrum, where the latter state completely decouples from the low-energy spectrum for large values of m [44]. LQs can be dangerous for proton decay if they couple to diquarks. The S_3 leptoquark would not couple to the diquark if $SU(5)$ contraction $c^{ij} \mathbf{10}_i \mathbf{10}_j \mathbf{45}$ was forbidden or suppressed. Furthermore, S_3 must not mix with any other LQ with diquark couplings. Both conditions can be met in a generic $SU(5)$ framework [45].

At high scale $\Lambda = m_{R_2}$ the Wilson coefficients for the charged current processes are:

$$g_{S_L}(\Lambda) = 4 g_T(\Lambda) = \frac{y_L^{c\tau} y_R^{b\tau^*}}{4\sqrt{2} m_{R_2}^2 G_F V_{cb}}. \quad (4.3)$$

This is the only flavour of charged current semileptonic process affected by R_2 . The $R_{K^{(*)}}$ anomaly is accounted for through left-handed tree-level contributions of S_3 to the vector and axial-vector Wilson coefficients [46]

$$\delta C_9 = -\delta C_{10} = \frac{\pi v^2}{\lambda_l \alpha_{\text{em}}} \frac{\sin 2\theta (y_L^{c\mu})^2}{2m_{S_3}^2}. \quad (4.4)$$

Here the mixing angle enters as $\sin 2\theta$, originating from the matrix U_R , and plays an important role in suppressing effect in $R_{K^{(*)}}$ relative to the one in $R_{D^{(*)}}$. The 1σ interval $C_9 = -C_{10} \in$

$(-0.85, -0.50)$ has been obtained by performing a fit to R_K , R_{K^*} , and $\mathcal{B}(B_s \rightarrow \mu\mu)$. The left-handed (weak triplet) nature of the S_3 LQ imply contributions to both neutral and charged current semileptonic processes. Among the charged current observables the LFU ratios $R_{D^{(*)}}^{\mu/e} = \mathcal{B}(B \rightarrow D^{(*)}\mu\bar{\nu})/\mathcal{B}(B \rightarrow D^{(*)}e\bar{\nu})$ impose severe constraints on S_3 couplings. We have also considered $\mathcal{B}(B \rightarrow \tau\bar{\nu})$ and the kaon LFU ratio $R_{e/\mu}^K = \Gamma(K^- \rightarrow e\bar{\nu})/\Gamma(K^- \rightarrow \mu\bar{\nu})$. The $b \rightarrow s\nu\bar{\nu}$ constraints are not taken as inputs as constraints. Instead we predict $R_{\nu\nu}^{(*)}$ and compare it to experimental bounds, $R_{\nu\nu} < 3.9$ and $R_{\nu\nu}^* < 2.7$ [47]. The loop-induced neutral-current constraints affect both LQ's couplings. We have taken into account the $B_s - \bar{B}_s$ mixing frequency, which is modified by the S_3 box-diagram, proportional to $\sin^2 2\theta [(y_L^{c\mu})^2 + (y_L^{c\tau})^2]^2 / m_{S_3}^2$, and the upper limit on lepton flavour violating τ decays $\mathcal{B}(\tau \rightarrow \mu\phi)$, $\mathcal{B}(\tau \rightarrow \mu\gamma)$. The Z-boson couplings to leptons measured at LEP [48] are also modified at loop level by both LQs.

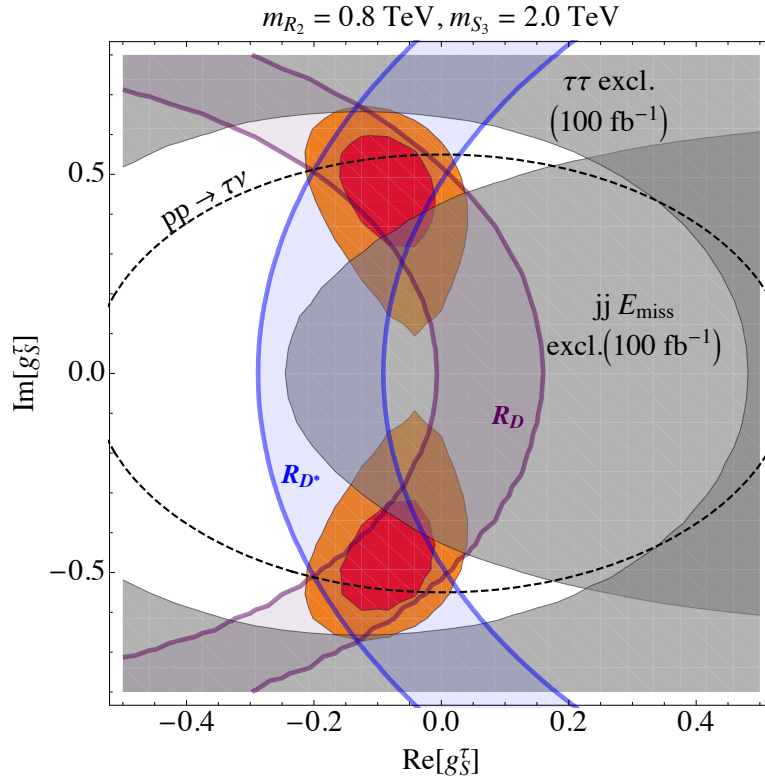


Figure 1: Results of the flavour fit in the g_{S_L} plane, scalar coupling entering the transition $b \rightarrow c\tau\nu\tau$. The $1\sigma(2\sigma)$ fitted regions are rendered in red (orange). Separate constraints from R_D and R_{D^*} to 2σ accuracy are shown by the blue and purple regions, respectively. The LHC exclusions are depicted by the gray regions. Dashed circle denotes the $pp \rightarrow \tau\nu$ constraint.

Taking into account the aforementioned flavour observables we have performed a fit for parameters $y_R^{b\tau}$, $y_L^{c\mu}$, $y_L^{c\tau}$ and θ , while fixing the masses to $m_{R_2} = 0.8$ TeV and $m_{S_3} = 2$ TeV. The opposite sign of interference terms in R_D and R_{D^*} require complex Wilson coefficient g_{S_L} (Fig. 1), where we have put the complex phase in $y_R^{b\tau}$. The SM is excluded at 3.6σ , the best fit point provides a good agreement with $R_{D^{(*)}}$ and $R_{K^{(*)}}$. Note that the required large imaginary part in $y_R^{b\tau}$ could be in principle tested in the future experiments measuring neutron EDM [49]. The best fit point is

consistent with the LHC constraints [44] superimposed in gray on the same plot. The $pp \rightarrow \tau\nu$ constraint in the effective theory approximation excludes the region outside dashed circle [50] in Fig. 1.

The consistency of model with low energy data requires that $\mathcal{B}(B \rightarrow K\mu\tau)$ is bounded and at 1σ we obtain $1.1 \times 10^{-7} \lesssim \mathcal{B}(B \rightarrow K\mu^\pm\tau^\mp) \lesssim 6.5 \times 10^{-7}$, whereas related decay modes are predicted to be $\mathcal{B}(B \rightarrow K^*\mu\tau) \approx 1.9 \times \mathcal{B}(B \rightarrow K\mu\tau)$ and $\mathcal{B}(B_s \rightarrow \mu\tau) \approx 0.9 \times \mathcal{B}(B \rightarrow K\mu\tau)$. Another important prediction is a $\gtrsim 50\%$ enhancement of $\mathcal{B}(B \rightarrow K^{(*)}\nu\nu)$, which will be further tested at Belle 2. Remarkably, these two observables are highly correlated (Fig. 2). Furthermore, we derive a lower bound on $\mathcal{B}(\tau \rightarrow \mu\gamma)$, just below the current experimental limit, $\mathcal{B}(\tau \rightarrow \mu\gamma) \gtrsim 1.5 \times 10^{-8}$.

Finally, our description of $R_{D^{(*)}}$ anomaly requires relatively light LQ states, not far from the TeV scale, and these LQs are necessarily accessible at the LHC, as we discuss in Ref. [44].

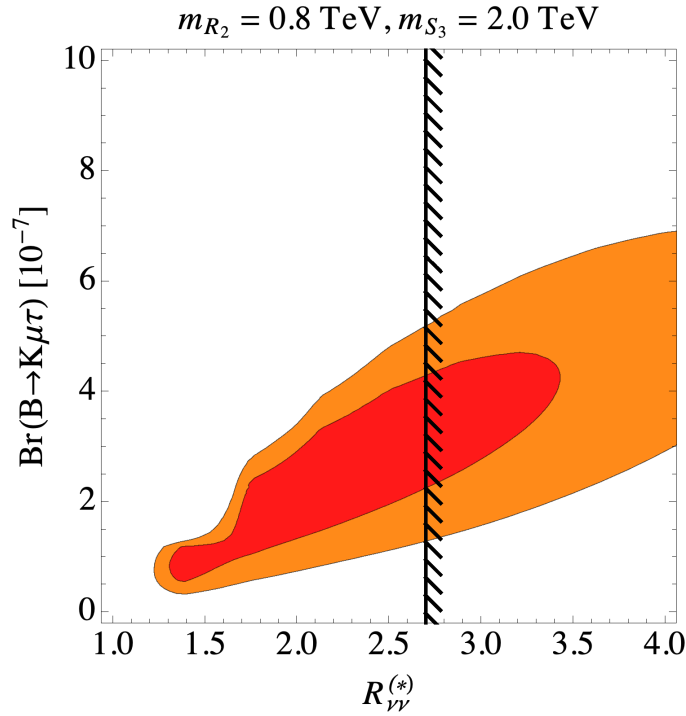


Figure 2: Predicted $\mathcal{B}(B \rightarrow K\mu\tau)$ is plotted against predicted $R_{\nu\nu} = \mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})/\mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})^{\text{SM}}$ for the 1σ (red) and 2σ (orange) regions of Fig. 1. The black line denotes the current experimental limit, $R_{\nu\nu}^* < 2.7$ [47].

5. Summary and outlook

Hints of lepton universality violation inconsistency in $R_{K^{(*)}}$ and $R_{D^{(*)}}$ with the SM have triggered a gold rush in the flavour community that resulted in many proposed models. Leptoquarks are one possibility which are probably phenomenologically most suited to the observed puzzles which all dwell in leptoquarks' natural habitat of semileptonic processes. The U_1 vector leptoquark accommodates all observed lepton universality anomalies and has to be accompanied with its own mass generation mechanism stemming from the UV. We have proposed a two scalar LQ model that accommodates the observed LFU ratios in B -meson decays and is compatible with other low energy

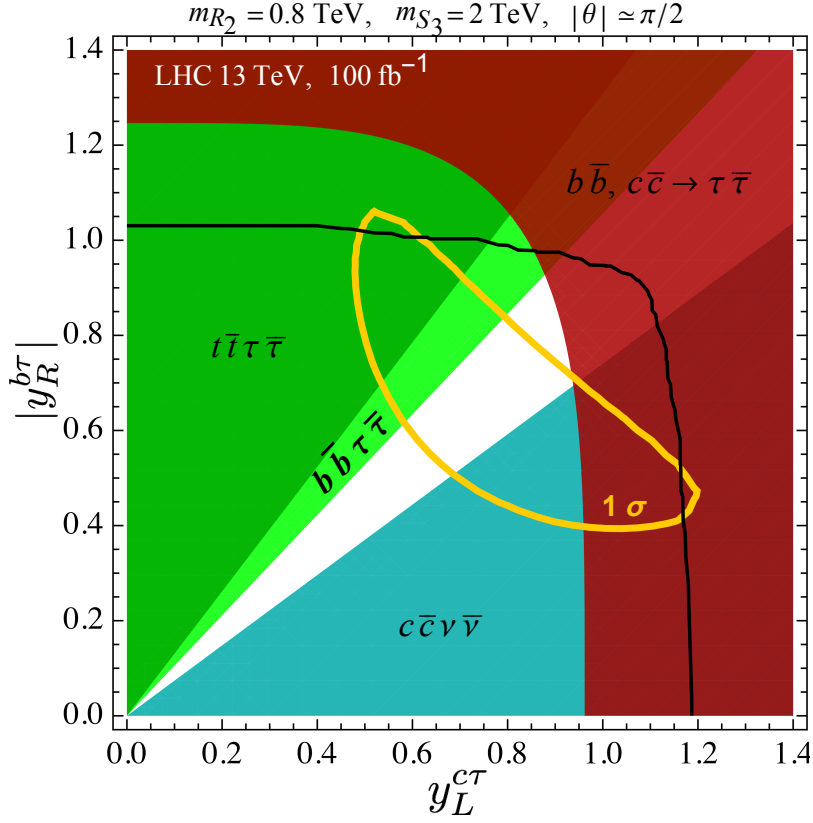


Figure 3: Most important LHC limits for each LQ process at a projected luminosity of 100 fb^{-1} . The red region is excluded by the high- p_T di-tau search by ATLAS [51], the green and turquoise exclusion regions come from LQ pair production searches by CMS [52, 53, 54]. The region of Yukawa couplings above the black line is excluded due to their non-perturbative values below the GUT scale (see [44] for more details). The yellow contour denotes the 1σ region of the fit to the low-energy observables.

constraints as well as with direct searches at the LHC. The model has an $SU(5)$ origin that relates Yukawa couplings of the two LQs through a mixing angle. The model remains perturbative up to the unification scale. We propose signals of the two light LQs at the LHC and spell out predictions for several flavour observables. We predict and correlate $\mathcal{B}(B \rightarrow K\mu\tau)$ with $\mathcal{B}(B \rightarrow K^{(*)}\nu\nu)$, as well as derive a lower bound for $\mathcal{B}(\tau \rightarrow \mu\gamma)$, which should be in reach of the Belle 2 experiment.

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