



Telescope Array Combined Fit to Cosmic Ray Spectrum and Composition

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We present the result of fits of an astrophysical model of UHECR sources to the energy spectrum measured using the Telescope Array (TA) surface detectors and the composition data measured by TA fluorescence detectors in stereo mode. The astrophysical model consists of identical sources, uniformly distributed with a density which evolves with age, where groups of nuclei with varying fractions are accelerated producing a power law source with a rigidity-dependent cutoff. The model includes the propagation effects of photo-pion production, photo-nuclear disintegration and general energy loss from universal expansion. Comparison of model data with detector data in both the energy and the X_{max} distributions is done via a forward-folding description of detector effects. A prediction of the cosmogenic neutrino flux at Earth resulting from the cosmic rays produced in the model with these fit values is also presented. The predicted flux is considerably higher than other similar fits to Auger data have previously predicted.

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1. Introduction and Model

The origin of Ultra High Energy Cosmic Rays (UHECRs, $E > 10^{18}$ eV) remains undetermined despite a sample of tens of thousands of events collected by very large observatories around the world. UHECRs are believed to be of extragalactic origin, because of the observed anisotropy of arrival directions and the diffusion scale for magnetic field within the galaxy.

Employing a relatively simple model of UHECR sources we use Telescope Array (TA) measurements of the energy spectrum and the observed distributions of X_{max} , the depth in the atmosphere where extensive air showers reach their maximum size, to constrain possible UHECR source parameters.

The model we are employing is the same as that used by the Pierre Auger Observatory in a similar fit [1]. The source model assumes that UHECR sources are identical and uniformly distributed with a density which evolves as $(1 + z)^3$ for z < 1.5 and is constant for z > 1.5 [8]. Each source has a mix of five nuclei (H, He, N, Si, and Fe) that are accelerated to give spectra with identical power law slopes $(E^{-\gamma})$ and a rigidity-dependent exponential cutoff, R_{max} . The source parameters are therefore γ , R_{max} , and five fractions (which sum to unity). Cosmic rays generated at z > 1 cannot effect TA observations at the highest energies; however, cosmic rays from these distant sources contribute significantly to the predicted neutrino flux.

The model is constrained by the TA surface detector (SD) spectrum measurement (as presented at the 2017 ICRC [2]) and the TA Stereo Composition measurement (also from the 2017 ICRC [3]). We choose the TA SD spectrum because it has the largest set of statistics for a UHECR energy spectrum measured in the Northern Hemisphere. It is also different from the spectrum measured in the Southern Hemisphere with a higher energy for the final sharp break in the spectrum (60 EeV *cf.* 40 EeV). We choose the TA Stereo composition measurement because of its indifference to high energy particle interaction models.

The effects of propagation of nuclear species through the universe is done by the CRPropa model [4]. The CRPropa calculation was done using both the cosmic microwave background (CMB) and the Gilmore model [5] of the infrared background (IRB) to calculate photo-pion production, photo-nuclear disintegration and electron-positron pair-production. The cosmological parameters used were those determined by Planck in 2015 [6]. A 1-D propagation calculation was performed for a series of small ranges in z, "shells", with 462 shells logarithmically spaced between $z = 10^{-4}$ and z = 4. 20 thousand particles per 0.1 decade of energy of each source species were injected with an E^{-1} spectrum between the energies of 0.0316 EeV and (rigidity dependent) 3160 EV. Each "observed" nuclei was recorded and binned by atomic number. Thus for each input species, each possible output species and each shell, we create a 650×650 bin E_{out}/E_{in} histogram. (E_{in} is the injected energy, E_{out} is the energy at observation) These can be combined into big arrays, e.g., for Fe (A=56) we have a $56 \times 462 \times 650 \times 650$ array. As this gets to be an unruly size of data, we sum over the 462 z-shell bins weighted by the light-travel time across the shell (i.e. the thickness of the shell) and the density of sources in the shell (given by the z-dependent density assumption given above). Using the E_{out}/E_{in} histograms then we can put in any input (source) spectrum and get the expected "observed" spectrum of a particular nuclear type. The input spectrum is created according to the model given above.

For comparison with the spectrum we use this output directly. For comparison with the stereo

Energy Range	18.4 - 18.6	18.6 - 18.8	18.8 - 19.0	19.0 - 19.2	19.2 – 19.6	19.6 - 20.0
proton	21.8	19.0	17.6	16.3	16.4	16.4
Iron	17.8	16.8	14.8	13.2	13.0	12.8

Table 1: Table of X_{max} resolutions in g/cm². Energy ranges are given in $\log_{10}(E/\text{EeV})$

composition measurement we use the Gumbel [7] distribution to create X_{max} distributions for each nuclear type and energy. The parameters for the Gumbel distribution for given high-energy interaction models has been tabulated in [7]. We must then also apply a stereo X_{max} acceptance weighting to these distributions and smear according to the stereo X_{max} resolution. The X_{max} acceptance was calculated in the energy bins used and then fit to a model of a flat-top plateau, a breakpoint in X_{max} and an exponential fall-off in acceptance above the break point. It was found that a single value of the breakpoint and the exponential slope could be used to fit the acceptance in all energy bins. The X_{max} acceptance is shown in Figure 1. The stereo X_{max} resolution was calculated by comparing the generated and the reconstructed X_{max} values for simulated proton and iron primaries using in each energy band. This determination of the X_{max} resolution is the same as that determined from the stereo composition analysis [3]. The values for the X_{max} resolution used in this analysis are stated in Table 1. The X_{max} distribution resulting from the output of the Gumbel model and with the acceptance model applied, was then smeared using a single gaussian in X_{max} with a width given by logarithmic interpolation between the tabulated proton and iron resolutions based on the known primary nuclear mass. The sum of these X_{max} distributions for all the observed primary cosmic ray species was then compared to the observed X_{max} distribution.

For both the spectrum and composition analyses we use a binned log-likelihood comparison of events observed compared to events in the model. For the spectrum comparison the log-likelihood is based on the Poisson distributions, while for the X_{max} comparison, the log-likelihood is based on a multinomial distribution. Both log-likelihood comparisons are scaled to produce a χ^2 -like distribution in the limit of very large numbers of events. We refer to these as deviances, and sum the deviance from the spectrum and the deviance from the compositions analysis to determine an overall figure-of-merit for the model with given parameters.

2. Combined Fit Results

Our fits presented here use the QGSJetII-04 high-energy interaction model for the Gumbel /Xmax/ distributions and the Gilmore-12 IRB model. We scan the $\gamma -\log_{10}(R_{\text{max}}/\text{EV})$ plane, and for each pair allow the five source fractions to vary under the requirement that the fractions sum to unity. We first performed coarse scans, γ was scanned in 41 steps from -1.5 - 2.5 while $\log_{10} R$ was scanned in 41 steps from -0.5 - 3.5. To allow for systematic uncertainties in energy and X_{max} reconstruction, we shifted the measured energy and X_{max} of the data by various amounts, adding a χ^2 -penalty to the deviance to account for the shifts. The systematic uncertainty in the energy measurement was taken to be 22% while the systematic uncertainty in the X_{max} measurement was taken as 15 g/cm². The best fits were found with $\Delta \log_{10} E = -0.12 (1.4\sigma)$ and $\Delta X_{\text{max}} = +10 \text{ g/cm}^2 (0.67\sigma)$. We then performed a fine scan with these shift values, 401 steps for γ from -1.5 - 2.5,



Figure 1: Stereo X_{max} acceptance calculated from QGSJetII-04 simulations of iron and proton primaries. The acceptance is fit to a model with a plateau at small X_{max} , a break point in X_{max} , and an exponential decrease in acceptance with X_{max} above the break point. The fits were performed using a binned log-likelihood minimization. The break point and exponential slope were required to be the same for all energy bins.

301 steps for $\log_{10} R_{\text{max}}$ from 0 – 3. The deviance contours corresponding to $10-\sigma$ are shown in Figure 2. The best fit point is at (2.06, 2.26) with a total deviance D = 126.0 for 65 = 16 + 55 - 6 degrees-of-freedom. There is also a local minimum at the point (0.78, 1.20) with D = 200.5.

The details of the best fit point ($\gamma = 2.06$, $R_{\text{max}} = 182$ EV) are shown in Figures 3 and 4. The source fractions are: 0.0%, 99.2%, 0.0%, 0.0%, and 0.8% for H, He, N, Si, and Fe, respectively. The fit is dominated by the very large flux in TA above $10^{1.7}$ EeV which is above the model's prediction for a GZK-effect.

The details of the fit for the secondary minimum ($\gamma = 0.78$, $R_{\text{max}} = 15.8$ EV) are shown in Figures 5 and 6. The source fractions are: 61.0%, 37.4%, 1.5%, 0.1%, and 0.003% for H, He, N, Si, and Fe, respectively.

3. Neutrino Flux Prediction

Using CRPropa one can also simulate the production of neutrinos from the propagation of cosmic rays. We performed this calculation while generating the shell model of the cosmic rays for our model. We can then predict the cosmogenic neutrinos produced during the propagation of the cosmic rays used to fit the Telescope Array data. We produced cosmic rays from source distances beyond what is relevant for fitting the cosmic ray spectrum, but which will contribute to the neutrino flux. For these distances, 1 < z < 4, we used the van Vliet et al.[8] prescription for the evolution of the sources, which is $(1 + z)^m$ for z < 1.5, and constant for z > 1.5. The predicted flux is shown in Figure 7, and includes the sum of muon and electron neutrino and anti-neutrinos.

The higher cutoff energy of the TA cosmic ray spectrum thus open the possibility that there will be a considerable flux of cosmogenic neutrinos, a flux which is in the range of planned neutrino detectors such as ARIANNA-200.



Figure 2: A plot of the deviance contours corresponding to $10-\sigma$ for Telescope Array data using QGSJetII-04 as the high-energy interaction model and the Gilmore-12 IRB model, $\Delta \log_{10} E = -0.12$ and $\Delta X_{\text{max}} = +10$ g/cm² (0.67 σ). The best fit point is $\gamma = 2.06$, $\log_{10}(R_{\text{max}}/\text{EV}) = 2.26$ ($R_{\text{max}} = 182$ EV). This point had source fractions: 0.0%, 99.2%, 0.0%, 0.0%, and 0.8% for H, He, N, Si, and Fe, respectively. The local minimum at $\gamma = 0.78$, $\log_{10}(R_{\text{max}}/\text{EV}) = 1.20$ ($R_{\text{max}} = 15.8$ EV) has source fractions: 97.1%, 0.0\%, 0.0\%,



Figure 3: *Left:* The observed event energy distribution and the model predictions for *observed* species the best fit point. The fit gives a predominantly H at observation, despite no H at the source. There are 16 bins contributing to the degrees-of-freedom in the fit. *Right:* The observed and predicted energy flux spectra (multiplied by E^3) for the best fit.



Figure 4: The observed X_{max} distributions in bins of energy along with the predicted X_{max} distributions from the model the best fit. The colors of the observed elemental group predictions is the same as in Figure 3. There are a total of 55 non-empty data bins contributing to the degrees-of-freedom



Figure 5: *Left:* The observed event energy distribution and the model predictions for *observed* species in the secondary minimum. *Right:* The observed and predicted energy flux spectra (multiplied by E^3) for the secondary minimum.



Figure 6: The observed X_{max} distributions in bins of energy along with the predicted X_{max} distributions from the model in the secondary minimum. The colors of the observed elemental group predictions is the same as in Figure 3.



Figure 7: The predicted cosmogenic neutrino flux predicted from the source model of cosmic rays fit in this paper. Note that units are GeV and GV to align with neutrino astronomy conventions. The prediction from our best fit model is shown in red. We sampled fits from the scan around the $1-\sigma$ contour to get generate an uncertainty band for the predicted flux. While the source is mostly helium, the high rigidity cutoff implies that many of the spalated protons and neutrons are still above the GZK-threshold energy and can thus contribute to the cosmogenic neutrino flux. The prediction of the neutrino flux from the secondary minimum is also shown, in magenta.

4. Discussion

From the fit results shown of the Telescope Array spectrum and stereo composition data, a number of different interpretations of source compositions could be drawn. Not all of these source compositions are astrophysically plausible, e.g., predominantly He with no H; or predominantly H with no He nor N but a little Fe. The best fit for the TA data overall shows that one might expect predominantly H at observation although no H was accelerated at the source. This is quite different from the interpretation gleaned from the combined fit to the Auger data, which showed a moderately soft spectrum at the source contributing to a progressively heavier set of dominant species at observation. Since the Auger and TA spectrum data are consistent in this range except for the very highest energies, this difference in interpretation is very dependent on shape of the spectrum in the very high energy region.

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