

Cosmic ray energy spectrum and composition measurements from the GRAPES-3 experiment: Latest results

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The Gamma Ray Astronomy at PeV EnergieS phase-3 (GRAPES-3) experiment is located at Ooty in India (11.4° N, 76.7° E and 2200 m above m.s.l.). It consists of a densely packed array of 400 plastic scintillator detectors and a large area muon telescope (560 m²). It measures cosmic rays from several TeV to over 10 PeV energies providing a substantial overlap with direct experiments, while covering the knee region. Shower parameters are reconstructed by fitting the observed particle densities with the NKG lateral distribution function (LDF). Relations between shower size and energy of primary cosmic rays are derived using air shower simulation with SIBYLL-2.3c and QGSJET-II-04 hadronic interaction models. These relations are used for obtaining the reconstructed energy spectrum and the Bayesian method is used for unfolding. In addition, precise measurements of the average nuclear composition are obtained by fitting muon multiplicity distributions (MMDs) for proton, helium, nitrogen, aluminium, and iron primaries with the MMDs measured by the muon telescope. Details of the analysis and preliminary results for the extracted energy spectrum and composition from a few tens of TeV to 10 PeV will be presented.

1. The GRAPES-3 Experiment

The GRAPES-3 (Gamma Ray Astronomy at PeV Energies Phase-3) experiment is located at Ooty (11.4° N, 76.7° E, 2200 m a.s.l.), India. The GRAPES-3 extensive air shower (EAS) array consists of 400 plastic scintillator detectors of 1 m² area each [1, 2] and a large area muon telescope. A schematic of the array is shown in Figure 1. Each scintillator detector is shown as filled square. The scintillator array covers an area of 25000 m². The scintillator detectors are arranged in hexagonal geometry, to ensure the uniform selection of the EAS over the array, with an inter-detector separation of 8 m. The 560 m² muon telescope consists of 3712 proportional counters (PRCs) each of length 600 cm and cross-section area of 10 cm × 10 cm. The PRCs are housed in 4 stations and each station has 4 modules. Each module has 4 orthogonal layers consisting of 58 PRCs in each layer [3]. It has an energy threshold of sec(θ) GeV for muons incident at zenith angle θ . A circular area of radius 50 m is used as the fiducial area for this analysis. The fiducial area (7850 m²) is shown by red dashed line. GRAPES-3 uses two level trigger. Level-0 trigger is a simple 3-line coincidence in 100 ns time window and level-1 trigger requires at least 10 detectors hit in 1 μ s time window [1].

Being a highly dense EAS array with an atmospheric overburden of ~ 800 g cm⁻², the GRAPES-3 experiment is capable of observing the primary cosmic rays (PCRs) from several TeV to over 10 PeV, providing a substantial overlap with direct experiments. GRAPES-3 muon telescope is sensitive to PCRs composition measurements through muon multiplicity distribution.

2. Reconstruction of shower axis and shower parameters

The relative arrival time of particles and the energy deposited by the particles in each scintillator detector were recorded for every triggered shower. The shower parameters were obtained by fitting a lateral distribution function namely Nishimura-Kamata-Greisen (NKG) to the observed particle densities in the detectors. The NKG function is given by:

$$\rho(r, s, N_e) = \frac{N_e}{2\pi r_0^2} \frac{\Gamma(4.5-s)}{\Gamma(s)\Gamma(4.5-2s)} \left(\frac{r}{r_0}\right)^{(s-2)} \left(1 + \frac{r}{r_0}\right)^{(s-4.5)} \quad \dots(1)$$

where N_e is the shower size, s is the shower age, r is the lateral distance from shower core (X, Y). r_0 is the Moliere radius, for GRAPES-3, $r_0 = 103$ m. Reconstruction of the shower direction is a two-step process. In the first step, the relative arrival time of the EAS measured by different detectors was used to reconstruct the arrival direction of EAS by fitting them with a plane front. In the second step, a more accurate shower arrival direction is measured by correcting it with shower size and shower age [4].

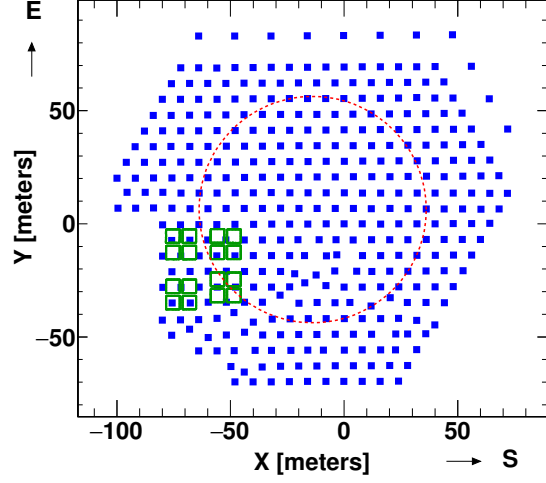


Figure 1: Schematic of GRAPES-3 EAS array. Plastic scintillator detectors (■), tracking muon telescope modules (□) and fiducial area (---) are shown.

3. Selection quality cuts and experimental data

To ensure the quality of the data used for the analysis, the following event selection criteria are used.

- Events with successful shower parameter reconstruction are used.
- Events with successful shower arrival direction reconstruction are used.
- The reconstructed cores must lie within the fiducial area. In this way, most of the improperly reconstructed EAS, due to EAS core landing near to the edge or outside the array can be avoided..
- The reconstructed age parameter (s) was restricted between 0.2 and 1.8.
- Zenith angle was restricted to 18° .
- Shower size (N_e) $> 10^4$, which corresponds to trigger efficiency greater than 90%.

Data collected by GRAPES-3 array during 1 January 2014 - 31 August 2016 was used for the analysis. The total live time of data collection is ≈ 926 days. The number of showers remaining after applying all the quality cuts are 3.2×10^7 from 2.5×10^9 .

4. MC Simulations

A detailed simulation study was done to calculate the efficiency and acceptance for the EAS detector array and energy calibration. Simulated EAS data for proton, Helium, Nitrogen, Aluminium, and Iron is produced by using CORSIKA (version 7.69) simulation package. The C, N, O, Al and Fe are used to represent light (C, N, O), medium (Mg, Al, Si) and heavy (Mn, Fe, Co) masses in primary cosmic rays (PCRs). For this analysis, data is generated with QGSJET-II-04 and FLUKA hadronic interaction models for high and low energy, respectively. Data were generated in the energy range of 1 TeV to 10 PeV and zenith angle range of $0^\circ - 45^\circ$, following a power law with a spectral index of -2.5. For the analysis, each shower was thrown in a circular area of radius 150 m from the center (-13.85 m, 6.29 m) of the GRAPES-3 EAS detector array with a random core position. Each shower was reused 10 times to improve the statistics, which makes the total number of showers to be 1.2×10^9 . The GEANT-4 package was used to simulate the scintillator detector response. A detailed GEANT-4 simulation is carried out to study the response of the secondary particles in the muon telescope. Due to the $\sec(\theta)$ GeV threshold of GRAPES-3 muon telescope for the secondaries incident at zenith angle θ , the soft component of the EAS is get filtered out. Therefore, for each triggered shower, the response of muon and hadron is measured in terms of PRC hits by using the GEANT-4 simulation. These PRC hits are used to count the muon tracks in the muon telescope.

5. Analysis

5.1 Efficiency and Acceptance

For each simulated element, the trigger (ϵ_T) and reconstruction efficiency (ϵ_R) is calculated as a function of primary energy. Total efficiency (ϵ_{tot}) was determined by the product of trigger and

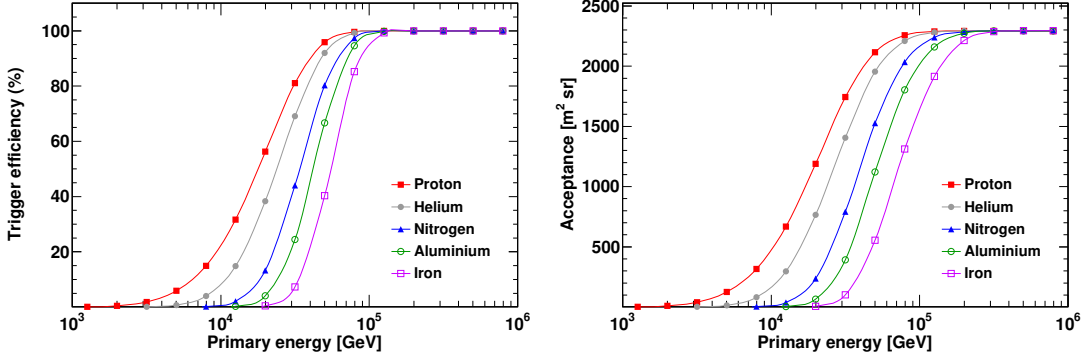


Figure 2: left: Trigger efficiency; right: acceptance as a function of primary energy for H, He, N, Al and Fe

reconstruction efficiency. Acceptance (A_{acc}) is represented as the product of the effective area and the effective viewing angle.

$$A_{acc}(E_T) = \frac{\pi A}{2} \sum_{k=1}^{n_\theta} \varepsilon_{tot}(E_T, \theta_k) (\cos 2\theta_k - \cos 2\theta_{k+1}) \quad (1)$$

where A is the fiducial area, n_θ is the total number of angle bins and θ_k and θ_{k+1} are low and high edges of each angle bin, respectively. The trigger efficiency and acceptance of each simulated element is shown in Figure 2. The trigger efficiency is $>90\%$ at 50 TeV, 55 TeV, 60 TeV, 80 TeV and 100 TeV for H, He, N, Al and Fe, respectively. The acceptance is increased to $2300 \text{ m}^2 \text{ sr}$ at 100% efficiency for $\theta < 18^\circ$.

5.2 Elemental composition

The GRAPES-3 muon telescope is dedicated to measuring the number of secondary muons track/detected muons for each triggered shower. For a small number of incident muons, the estimate of the detected muons is reliable. With the increase in the energy of PCRs, the number of muons increases which leads to the overlapping of the muon tracks. Therefore, the number of detected muons is underestimated. This saturation effect is studied in each muon module (35 m^2) through simulations and the result of one module is displayed in Figure 3. For example, on average, ten incident muons actually get reconstructed as eight detected muons. To correct for the saturation, the saturation curve is modeled with a 3^{rd} order polynomial for detected muons ≥ 4 . This correction is applied to each triggered shower to get the correct estimate of the muon multiplicity. The muon multiplicity distributions (MMDs) for all simulated primaries, for $4.4 \leq \log(N_e) < 4.6$, are shown in Figure 3. For a given shower size, the mean value of MMD increases with the mass number of the PCRs which indicates that the MMD is sensitive to the composition of the PCRs.

The shape of muon multiplicity is well described with the negative binomial distribution (NBD), given in eq.2.

$$NBD(x; r, m) = \frac{\Gamma(x+r)}{\Gamma(x+1)\Gamma(r)} \left(\frac{r}{r+m}\right)^r \left(\frac{m}{r+m}\right)^x \quad (2)$$

where m is the mean value of MMD and r is a measure of the standard deviation of the distribution. Therefore, the normalized MMD of each simulated primary is fitted with NBD to

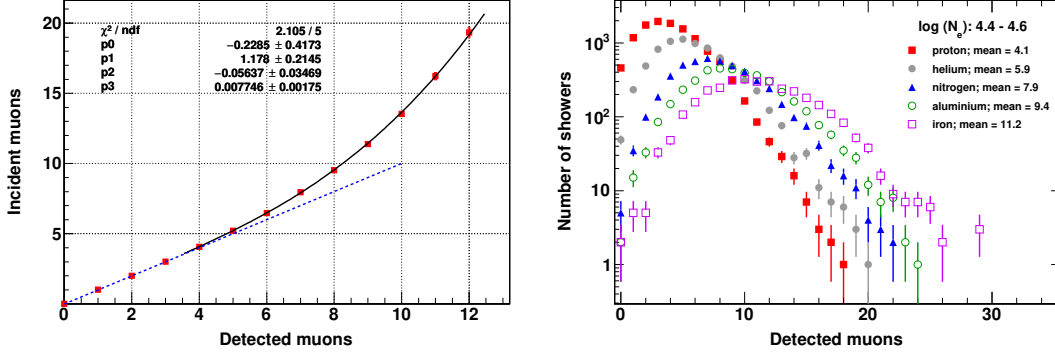


Figure 3: left: Muon saturation curve for one module of muon telescope, fitted with 3^{rd} order polynomial. right: Muon multiplicity distribution for all simulated primaries, for $4.4 \leq \log(N_e) < 4.6$

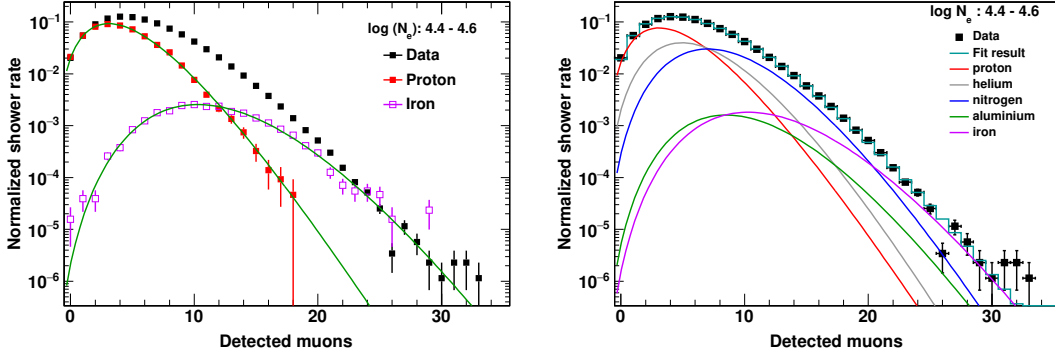


Figure 4: left: Muon multiplicity of H and Fe fitted with the negative binomial distribution, plotted along with experimental data. right: χ^2 minimization of normalized MMD for simulated primaries with observed normalized MMD; for $4.4 \leq \log(N_e) < 4.6$

avoid statistical fluctuations. The fit results for proton and iron along with observed MMD, for $4.4 \leq \log(N_e) < 4.6$, are shown in Figure 4. The distribution of proton and iron are scaled such that the tails of distribution overlap with the observed MMD. The low multiplicity of observed MMD is well described by the proton while higher multiplicity is well described by the iron. But to describe the middle range of the observed MMD, primaries of intermediate mass number are required. The relative abundance of each simulated primary is measured by minimizing the χ^2 of normalized MMD function of each simulated primary with normalized observed MMD.

$$\chi^2 = \sum_i \frac{(d_i - \sum_j a_j n_{ji})^2}{\epsilon_i^2} \quad (3)$$

where d_i and ϵ_i is the content and uncertainty of the i^{th} bin, respectively, of the normalized observed MMD. n_{ji} is the value of normalized MMD function of j^{th} simulated primary in the i^{th} bin of data. a_j is relative abundance of j^{th} primary.

The MMD for Al and Fe overlap substantially, for this analysis, they were combined by assuming a ratio of Al/Fe = 0.8 based on a direct experiment [5]. Since the abundance ratio Al/Fe was fixed, effectively the number of independent primaries was reduced to 4. TMinuit is used for

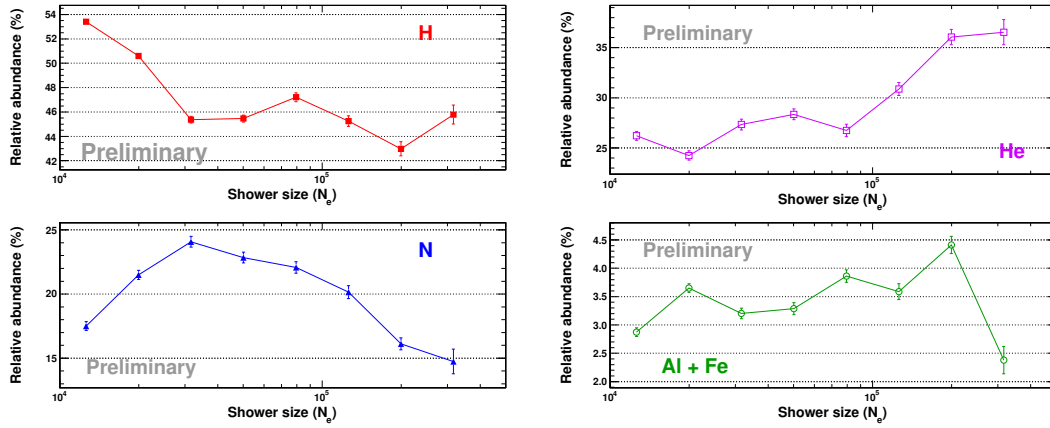


Figure 5: Relative abundance of all the simulated primaries; H, He, N and Al+Fe

the minimization of χ^2 . The fit results of χ^2 minimization for $4.4 \leq \log(N_e) < 4.6$ is shown in Figure 4.

6. Results

The measured relative abundance are shown in Figure 5. The relative abundance of proton is decreasing from 53% at shower size $10^{4.1}$ to 44% at shower size $10^{5.3}$. The relative abundance of helium is increasing from 26% at shower size $10^{4.1}$ to 36% at shower size $10^{5.3}$. The relative abundance of nitrogen is first increasing from 17% at shower size $10^{4.1}$ to 24% at shower size $10^{4.3}$ and then decreasing to 16% at shower size $10^{5.3}$. The combined relative abundance of aluminium and iron is increasing from 3% at shower size $10^{4.1}$ to 4% at shower size $10^{5.3}$. The relative abundance is used to decouple the observed shower size distributions into elemental shower size distribution for the shower size range $10^{4.0}$ to $10^{5.6}$. A detail study is done to get energy distribution from the shower size distribution. For this work, the energy distribution of simulated primaries is studied for a given shower size bin. In the interesting range of shower size (where efficiency is greater than 90%), the energy distribution, in a given shower size bin, can be approximate to a Gaussian. So, with the help of a Gaussian random number generator, the distribution of energy is generated for a given shower size. The differential cosmic-ray spectrum (dI/dE) is obtained as follows:

$$\frac{dI}{dE} = \frac{1}{T_{obs}} \left(\frac{N}{\Delta E \cdot A_{acc}} \right)_i \quad (4)$$

where subscript i denotes the i^{th} energy bin, N is the number of EAS, ΔE is the width of energy bin, A_{acc} is acceptance for the i^{th} energy bin and T_{obs} is the live time of the data. The measured preliminary elemental spectrum of proton and helium is shown in Figures 6 and 7, respectively. The statistical error bars are smaller than the marker size. The flux of the measured proton spectrum in this work is consistent with CREAM I+ III and NUCLEON KLEM (within error) at lower energy and consistent with KASCADE (QGSJET-01) at higher energy. Similarly, the measured Helium consistent with CREAM I+ III and NUCLEON KLEM (within error) at lower energy.

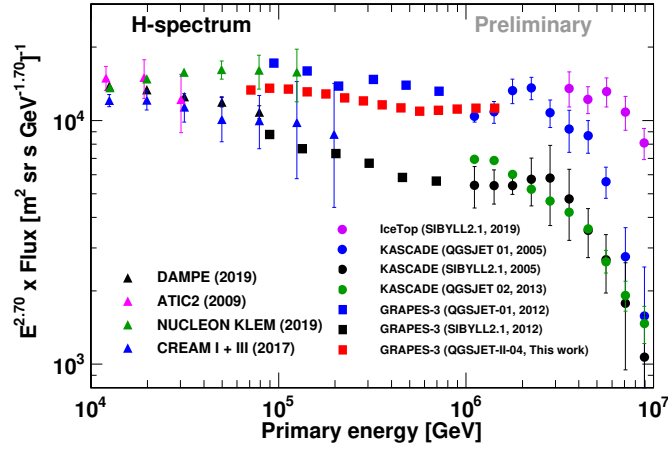


Figure 6: Elemental spectrum of proton; compared with other experiments

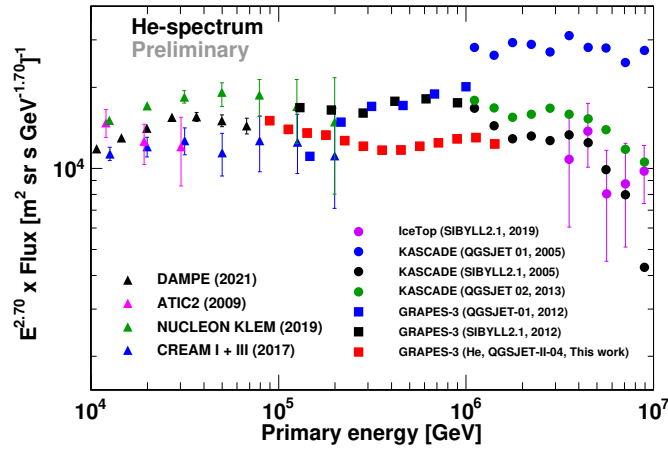


Figure 7: Elemental spectrum of helium; compared with other experiments

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