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Indirect bounds on new physics for $R(D^{(*)})$

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The Standard Model prediction of the B_c lifetime is discussed, together with the dominant uncertainties and strategies on how to improve them. Furthermore, a new method to compute the B_c lifetime based on the operator product expansion is proposed. It relies on differences of B, D and B_c meson decay rates, in which the free-quark contributions cancel out, reducing the uncertainty of the theory prediction.

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1. Introduction

A precisely calculated B_c meson lifetime puts stringent constraints on New Physics models containing new scalars, for example, scalar Leptoquarks and Two-Higgs-Doublet models [6, 11]. These are interesting insofar they explain anomalies reported in R(D) and $R(D^*)$ measurements.

Beyond these anomalies, the $B_c = (\overline{b}c)$ meson is an interesting particle to study, since it contains two different heavy quarks. We expect it can be well described with Non-Relativistic QCD (NRQCD), in which an expansion in the heavy quark velocities v_b and v_c is carried out. Together with the operator production expansion (OPE) approach this has lead to the most precise theory prediction of the B_c lifetime [9, 10, 12]. Other, less systematic approaches include QCD Sum Rules [18] as well as Potential models [14], which lead to comparable results.

From the experimental point of view the lifetime of the B_c is very precisely measured to be $\tau_{B_c}^{exp} = 0.510(9)$ ps (averaged value of the LHCb [1, 2] and CMS [22] measurements), that is,

$$\Gamma_{B_c}^{\exp} = 1.961(35) \,\mathrm{ps}^{-1}\,,\tag{1}$$

for the corresponding total decay rate. This precision is however not matched by the theory prediction due to large uncertainties in the calculation that arise largely from neglecting higher order nonperturbative corrections, parametric uncertainties and difficulties accounting for the strange quark mass, among others. The main uncertainties stem however from the treatment of the masses of the quarks inside the B_c , and are inextricably tied to the perturbative expansion. To examine this in more detail, we studied in Refs. [3, 4] three different mass schemes in the B_c decay rate in the OPE approach; these, as well as the other sources of uncertainty, are discussed below.

2. Mass schemes

2.1 MS scheme

In the $\overline{\text{MS}}$ mass-scheme the on-shell (OS) masses of the \overline{b} and c quarks are expressed in terms of the renormalized $\overline{\text{MS}}$ masses via the following equation:

$$m_q = \overline{m}_q(\mu) \left[1 + \frac{\alpha_s(\mu)}{\pi} \left(\frac{4}{3} - \ln\left(\frac{\overline{m}_q(\mu)^2}{\mu^2}\right) \right) \right] + O(\alpha_s^2) \,. \tag{2}$$

In our computation we use the lattice results [7, 13, 19] for the $\overline{\text{MS}}$ masses, which lead to the following decay rate of the B_c :

$$\Gamma_{B_c}^{\overline{\text{MS}}} = (1.51 \pm 0.38)^{\mu} \pm 0.08 |^{\text{n.p.}} \pm 0.02 |^{\overline{m}} \pm 0.01 |^{m_s} \pm 0.01 |^{V_{cb}}) \text{ ps}^{-1}, \qquad (3)$$

where the third uncertainty is due to the $\overline{\text{MS}}$ masses. The other uncertainties will be discussed in the following section. The value in (3) is to be compared with the experimental value, Eq. (1).

2.2 Upsilon scheme

In this mass scheme, the OS mass of the \overline{b} quark is expressed in terms of the very precisely measured Upsilon 1S state, by using the relation [20, 21]



Figure 1: Scale dependence of the LO decay rates $\Gamma(b \rightarrow cud)$ (left panel) and $\Gamma(c \rightarrow sud)$ (right panel) in the $\overline{\text{MS}}$ scheme. The NLO (solid-blue) and LO (dashed-orange) calculations are shown, respectively. The LO calculation to which the term with the explicit factor of $\alpha_s \ln(\mu)$ in the NLO decay rate is added is shown in green, displaying cancellation of scale dependence at $O(\alpha_s)$. The NLO decay rate omitting the term with an explicit factor of $\ln(\mu)$ is given by the dotted-red line.

$$\frac{\frac{1}{2}m_{\Upsilon}}{m_b} = 1 - \frac{(\alpha_s C_F)^2}{8} \left\{ 1 + \frac{\alpha_s}{\pi} \left[\left(\ln \left(\frac{\mu}{\alpha_s C_F m_b} \right) + \frac{11}{6} \right) \beta_0 - 4 \right]^2 + \cdots \right\}, \tag{4}$$

where β_0 is the one-loop beta function factor of the strong coupling constant. A similar relation is used to express the charm quark mass in terms of the J/Ψ mass. We use the PDG values $m_{\Upsilon} = 9460.30(26)$ MeV and $m_{J/\Psi} = 3096.900(6)$ MeV [23], which gives a B_c decay rate of

$$\Gamma_{B_c}^{\text{Upsilon}} = (2.40 \pm 0.19)^{\mu} \pm 0.21 |^{\text{n.p.}} \pm 0.01 |^{m_s} \pm 0.01 |^{V_{cb}}) \text{ ps}^{-1},$$
(5)

where the uncertainties of m_{Υ} and $m_{J/\Psi}$ are completely negligible.

2.3 Meson scheme

As a third scheme we use the so-called meson scheme, where the OS quark masses are expressed in terms of the meson masses by use of the HQET relation

$$m_b - m_c = \overline{m}_B - \overline{m}_D + \frac{1}{2}\lambda_1 \left(\frac{1}{m_b} - \frac{1}{m_c}\right) + \cdots$$
(6)

where $\lambda_1 = -0.27 \pm 0.14$ [15], and $\overline{m}_B = \frac{1}{4}(3m_{B^*} + m_B)$ and $\overline{m}_D = \frac{1}{4}(3m_{D^*} + m_D)$ denote the spin and isospin-averaged meson masses. In this scheme we obtain

$$\Gamma_{B_c}^{\text{meson}} = (1.70 \pm 0.24)^{\mu} \pm 0.20 |^{\text{n.p.}} \pm 0.01 |^{m_s} \pm 0.01 |^{V_{cb}}) \text{ ps}^{-1},$$
(7)

where the obtained value is in rather good agreement with the measurement in Eq. (1).

3. Uncertainties

3.1 Scale dependence

The residual renormalization-scale dependence from truncating the loop expansion is the largest uncertainty in the B_c lifetime. It enters mainly through the OS mass replacements of the

quarks in the three different schemes, since these relations are only used at the one-loop level. The scale dependence is largest in the $\overline{\text{MS}}$ scheme, which is illustrated in Fig. 1: It depicts the scale dependence of the leading order (LO) quark decay rates $\Gamma(b \rightarrow cud)$ and $\Gamma(c \rightarrow sud)$.

To reduce the scale dependence in our results, higher order QCD corrections have to be incorporated in the calculation, both in the OS mass relations and in free-quark decay rates.

3.2 Non-perturbative uncertainties

Further uncertainties result from the NRQCD expansion in the quark velocities v_b and v_c , which has been truncated at $O(v^4)$. Furthermore, the non-perturbative (n.p.) parameters also have uncertainties which are incorporated in the n.p. uncertainty estimations in eqs. (3), (5) and (7). The main improvement in these uncertainties would be to include higher-order corrections in the velocity expansion. It would however also be favourable to have lattice results available for the n.p. parameters.

3.3 Parametric uncertainties

Additional uncertainties result from all the parameters that are involved in the calculation, the largest one stemming from the uncertainty of the CKM matrix element V_{cb} given in the last uncertainties of eqs. (3), (5) and (7). In the $\overline{\text{MS}}$ scheme also the $\overline{\text{MS}}$ -masses introduce a rather large uncertainty, which is shown in third uncertainty in Eq. (3).

3.4 Strange quark mass

In the spectator *c*-decays a non-vanishing strange quark mass reduces the decay rate by about 7% in the three different mass schemes. The introduced uncertainty when neglecting m_s in the \bar{b} -quark decay can be estimated naively by considering the factor $(m_c/m_b)^2 \sim 0.1$, multiplied by the corresponding decay rate and a factor of 7%. In the *c*-quark decays the parametric uncertainty resulting from $\bar{m}_s(2 \text{ GeV})$ leads to an uncertainty of $\Delta\Gamma_c \sim 0.01 \text{ ps}^{-1}$.

4. Novel determination of Γ_{B_c}

To reduce the rather large uncertainties in the theory prediction, which mainly result from the scale dependence, we will adopt a novel method to compute the B_c decay rate, first described in [5]. The idea is to make use of the non-perturbative expansion of the decay rate not only for the B_c meson, but also for the *B* and *D* mesons, by considering the combination

$$\Gamma(B) + \Gamma(D) - \Gamma(B_c) = \Gamma^{n.p.}(B) + \Gamma^{n.p.}(D) - \Gamma^{n.p.}(B_c) + \Gamma^{\text{WA+PI}}(B) + \Gamma^{\text{WA+PI}}(D) - \Gamma^{\text{WA+PI}}(B_c), \qquad (8)$$

	B^0, D^0	B^+, D^0	B^{0}, D^{+}	B^+, D^+
$\Gamma_{B_c}^{\text{meson}}$	3.03 ± 0.54	3.04 ± 0.54	3.38 ± 0.98	3.39 ± 0.99
$\Gamma_{B_c}^{\overline{\text{MS}}}$	2.97 ± 0.42	2.98 ± 0.40	3.19 ± 0.80	3.19 ± 0.82

Table 1: Results obtained using the novel approach discussed in sec. 4 in the meson and \overline{MS} scheme, using four different combinations of *B* and *D* mesons.

where the rates on the left-hand side are given by

$$\Gamma(H_Q) = \Gamma_Q^{(0)} + \Gamma^{n.p.}(H_Q) + \Gamma^{\text{WA+PI}}(H_Q) + O(\frac{1}{m_Q^4}),$$
(9)

for a meson H_Q with heavy quark Q and where WA and PI stand for Weak Annihilation and Pauli Interference contributions. On the right-hand side of Eq. (8) the LO quark decay rates $\Gamma_Q^{(0)}$ drop out, since they are independent of meson states. Therefore the largest source of scale dependence vanishes, which reduces the error of the result. In order to determine the B_c decay rate Eq. (8) can be applied for either charged or neutral B and D mesons, resulting in four different ways to compute $\Gamma(B_c)$. The results using these four different combinations are given in Tab. 1.

The results from this novel approach are in tension with the experimental result in Eq. (1). Several reasons can be put forward to explain this disparity: 1. The uncertainties from NLO corrections to Wilson coefficients and free quark decay rates might be underestimated; 2. Eye-graph contributions, neglected in lattice computations of matrix elements that we use [8], but estimated to be small using HQET sum rules [17]; 3. Unexpectedly large contributions from higher dimension operators in the $1/m_Q$ expansion [16]; 4. Violation of quark-hadron duality. A thorough analysis of these is in order to determine the reason for the discrepancy between the results and experiment.

5. Summary

We have presented an updated analysis of the B_c decay rate, following the OPE approach. Three different mass schemes have been studied, which all lead to results in agreement with experiment and with each other. Furthermore an analysis of the theory uncertainties has been presented, where the scale-dependence makes up most of the total uncertainty.

We discussed a novel method to determine Γ_{B_c} based on differences of *B*, *D* and *B_c* decay rates that allows to reduce the scale-dependence uncertainty. The results deviate significantly from the experimental value, and we presented various possible reasons for this discrepancy.

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