## Charmless B decay measurements at Belle

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In this report, we summarize the recent charmless $B$ decay measurements at Belle. The studies are based on the Belle data sample of $711 \mathrm{fb}^{-1}$ or $121 \mathrm{fb}^{-1}$ collected at $\Upsilon(4 S)$ or $\Upsilon(5 S)$ resonance at the KEKB collider. Results of several decay modes are presented. In addition to their branching measurements, the structure in the two-body invariant mass are also investigated for some of the decay modes.

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## 1. Introduction

Charmless $B$ decays are suppressed in Standard Model (SM), and are also sensitive to physics beyond the Standard Model (BSM) within the loop of penguin amplitude. Precise measurements on them could be a good sensitivity test against the prediction by SM. The main experimental challenge is the signal rate which is about $10^{5}$ times smaller than the $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s, c)$ continuum processes. Reduction of combinatorial background is hence critical. Using a Belle data sample of $711 \mathrm{fb}^{-1}$ or $121 \mathrm{fb}^{-1}$ collected at $\Upsilon(4 S)$ or $\Upsilon(5 S)$ resonance with the Belle detector [1] at the KEKB asymmetric-energy $e^{+} e^{-}$collider [2], we report the studies of the following $B$ and $B_{s}^{0}$ decay modes: $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}, B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}[3], B^{+} \rightarrow K^{+} K^{-} \pi^{+}, B^{+} \rightarrow \pi^{+} \pi^{0} \pi^{0}, B_{s}^{0} \rightarrow \eta^{\prime} X_{s \bar{s}}$ [4], $B_{s}^{0} \rightarrow \eta^{\prime} \eta$ [5], and $B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0 \dagger}$. Their signal yields ( $N_{\text {sig }}$ ) are measured by one or multi-dimensional extended unbinned likelihood fit on data with different variables, and branching fractions are estimated by $\mathcal{B}=\frac{N_{\text {sig }}}{\epsilon \times N_{B}}$, where $\epsilon$ is the signal reconstruction efficiency and $N_{B}$ is the number of $B$ events $(772 \mathrm{M}$ for $B^{+}$or $B^{0}, 16.6 \mathrm{M}$ for $B_{s}^{0}$ ).
2. $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}$and $B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}$

Baryonic $B$ decays have various interesting features, such as the enhancement in the di-baryon low mass threshold [6], and the different angular distributions from different modes e.g. between $B^{+} \rightarrow p \bar{p} K^{+}$and $B^{+} \rightarrow p \bar{p} \pi^{+}$[7]. Signal $B$ candidate is identified by the energy difference $\Delta E \equiv E_{B}-E_{\text {beam }}$ and the beam-energy-constrained mass $M_{\mathrm{bc}} \equiv \sqrt{E_{\text {beam }}^{2} / c^{4}-\left|p_{B} / c\right|^{2}}$, where $E_{\text {beam }}$ is the beam energy, and $p_{B}$ and $E_{B}$ are the momentum and energy of the reconstructed $B$ meson, respectively. We use 2D fit with $\Delta E$ and $M_{\mathrm{bc}}$ to extract $N_{\text {sig }}$, and obtain $\mathcal{B}\left(B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}\right)=(0.83 \pm$ 0.17 (stat.) $\pm 0.17$ (syst.) $) \times 10^{-6}$ and $\mathcal{B}\left(B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}\right)=(4.58 \pm 1.17$ (stat.) $\pm 0.67$ (syst.) $) \times 10^{-6}$. The total measured $\mathcal{B}\left(B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}\right)$ is about a factor of 10 smaller than the predicted $\mathcal{B}\left(B^{+} \rightarrow\right.$ $p \bar{p} \rho^{+}$) from a theoretical calculation by generalized factorization method [8]. Figure 1 shows the $M_{\pi \pi}$ distribution. A $\chi^{2}$ fit is perform on $M_{\pi^{+} \pi^{0}}$ and we obtain $86 \pm 41$ events for $B^{+} \rightarrow p \bar{p} \rho^{+}$. Table 1 shows the signal yields in $M_{p \bar{p}}$ bins. Branching fraction of $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}$in the threshold enhancement region (the lowest bin) is estimated as $\left(0.35 \pm 0.13\right.$ (stat.) $\pm 0.07$ (syst.)) $\times 10^{-6}$, which is consistent with the LHCb result [9].


Figure 1: $M_{\pi^{+} \pi^{-}}$(left) and $M_{\pi^{+} \pi^{0}}$ (right) distributions of $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}$and $B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}$, respectively.

[^1]Table 1: Fitted yields of $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}\left(0.6 \mathrm{GeV} / c^{2}<M_{\pi^{+} \pi^{-}}<1.22 \mathrm{GeV} / c^{2}\right)$ and $B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}\left(M_{\pi^{+} \pi^{0}}<\right.$ $1.3 \mathrm{GeV} / c^{2}$ ) in $M_{p \bar{p}}$ bins.

| $M_{p \bar{p}}\left(\mathrm{GeV} / c^{2}\right)$ | Yield of $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}$ | Yield of $B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}$ |
| :--- | :---: | :---: |
| $M_{p \bar{p}}<2.85$ | $26.1_{-9.1}^{+10.0}$ | $133.5_{-25.2}^{+266.6}$ |
| $2.85<M_{p \bar{p}}<3.128$ | $19.6_{-9.3}^{+10.2}$ | $12.3-9.7$ |
| $3.128<M_{p \bar{p}}$ | $29.1_{-13.1}^{+16.2}$ | $-3.8_{-13.8}^{+15.1}$ |

## 3. $B^{+} \rightarrow K^{+} K^{-} \pi^{+}$

Compared to previous measurement by Belle [10], $B^{+} \rightarrow K^{+} K^{-} \pi^{+}$result is updated with a re-optimized binning to study the property of the structure and localized $\mathcal{A}_{C P}$ at low $M_{K^{+} K^{-}}$region which were also observed in BaBar [11] and LHCb [12-14]. Signal yields and $\mathcal{A}_{C P}$ are extracted by using 2D fit with $\Delta E$ and $M_{\mathrm{bc}}$ within each $M_{K^{+} K^{-}}$bins, and Figure 2 shows the results. The structure at $M_{K^{+} K^{-}}<1.1 \mathrm{GeV} / c^{2}$ has an $\mathcal{A}_{C P}$ of $-0.90 \pm 0.17$ (stat.) $\pm 0.03$ (syst.) with a significance of $4.8 \sigma$. Helicity angle ( $\theta_{\text {hel }}$, defined as the angle between $B^{+}$and $K^{+}$in the $K^{+} K^{-}$rest frame) for signal events within $M_{K^{+} K^{-}}<1.1 \mathrm{GeV} / c^{2}$ is shown in Figure 3. The distribution is consistent with a coherent sum of spin-0 and spin-1 the most.


Figure 2: Differential branching fraction (left) and $\mathcal{A}_{C P}$ (right) distributions as a function of $M_{K^{+} K^{-}}$for $B^{+} \rightarrow K^{+} K^{-} \pi^{+}$.

## 4. $B^{+} \rightarrow \pi^{+} \pi^{0} \pi^{0}$

The major challenge in the $B^{+} \rightarrow \pi^{+} \pi^{0} \pi^{0}$ measurement is the shower leakage [15] due to two $\pi^{0}$ in the reconstruction, and the correlation between energy and other variables. e.g. between $\Delta E$ and $M_{\pi \pi}$. To handle those effects, we require the momentum to be greater $0.5 \mathrm{GeV} / c^{2}$ for all $\pi^{0}$ candidates. By a 3D fit with $\Delta E, M_{\mathrm{bc}}$, and a Neural-Network [16] output discriminant for continuum suppression [17], we obtain inclusive $\mathcal{B}\left(B^{+} \rightarrow \pi^{+} \pi^{0} \pi^{0}\right)=(19.0 \pm 1.5$ (stat.) $\pm 1.4$ (syst.) $) \times 10^{-6}$ and $\mathcal{A}_{C P}=(9.2 \pm 6.8($ stat. $) \pm 0.5($ syst. $)) \%$. We use the ${ }_{s} \mathcal{P}$ lot technique [18] to isolate signal on $M_{\pi \pi}$ distribution, and perform a 2D binned fit on the histogram to extract the signal model composition as shown in Figure 4. In addition to the $B^{+} \rightarrow \rho(770)^{+} \pi^{0}$ structure at low $M_{\pi^{+} \pi^{0}, \text { min }}$


Figure 3: The helicity angle distribution with applying efficiency correction and comparisons to different models, where the LHCb model is from Ref. [13].
region ${ }^{\dagger}$, and we also observe a new structure at $M_{\pi^{0} \pi^{0}}$ region, which is modeled by an incoherent sum of $f_{0}(980), f_{2}(1270)$, and $f_{0}(500)$. A combined branching fraction for this $\pi^{0} \pi^{0}$ structure is measured as $(6.9 \pm 0.9($ stat. $) \pm 0.6($ syst. $)) \times 10^{-6}$, which has a significance of $9.2 \sigma$. A large $\mathcal{A}_{C P}$ is seen at $M_{\pi^{0} \pi^{0}} \sim 1.4 \mathrm{GeV} / c^{2}$ as shown in Figure 5.


Figure 4: Projection of the fit result to ${ }_{s} \mathcal{W}$ eights $M_{\pi^{+} \pi^{0}, \min }-\mathrm{vs}-M_{\pi^{0} \pi^{0}}$ histogram.


Figure 5: ${ }_{s}$ Weights $\mathcal{A}_{C P}$ as a function of $M_{\pi^{0} \pi^{0}}$ for $M_{\pi^{+} \pi^{0}, \min }>1.9 \mathrm{GeV} / c^{2}$. The first few bins are combined due to low number of events.

[^2]5. $B_{s}^{0} \rightarrow \eta^{\prime} X_{s \bar{s}}, B_{s}^{0} \rightarrow \eta^{\prime} \eta$, and $B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}$

As $B$ decays with $\eta^{\prime}$ in the final state have been observed firstly by CLEO [19, 20], we have found some special properties in this particle and decays involving it. $\eta^{\prime}$ mass is higher than the expectation from symmetry considerations [21]. Measurements of $\mathcal{B}\left(B \rightarrow \eta^{\prime} X_{s}\right)$ [23-25] also show unexpected enhancement compared with SM prediction [22]. Any new observation on decays with $\eta^{\prime}$ could provide further information to understand its property.

We report the first measurement on $B_{s}^{0} \rightarrow \eta^{\prime} X_{s \bar{s}}$ based on a semi-inclusive method [4]. Simulation of $X_{s \bar{s}}$ fragmentation is performed with PYTHIA 6 [26] with a flat mass distribution. $X_{s \bar{s}}$ candidates are reconstructed with two kaons ( $K^{+} K^{-}$or $K^{ \pm} K_{S}^{0}$ with $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$) and up to four pions with at most one $\pi^{0} . \eta^{\prime}$ candidates are reconstructed with $\pi^{+} \pi^{-} \eta$ and $\eta \rightarrow \gamma \gamma . N_{\text {sig }}$ is extracted by a 1 D fit on $M_{\mathrm{bc}}$ with $-0.12 \mathrm{GeV}<\Delta E<0.05 \mathrm{GeV}$ in $M_{X_{s \bar{s}}}$ bins. As none of the bins shows significant yield, we set an upper limit on $\mathcal{B}\left(B_{s}^{0} \rightarrow \eta^{\prime} X_{s \bar{s}}\right)$ as $1.4 \times 10^{-3}$ at $90 \%$ confidence level (C.L.).

Branching fraction and $C P$ asymmetry of $B_{s}^{0} \rightarrow \eta^{\prime} \eta$ decay could be affected by various BSM scenarios [28]. Along with the results of other $B_{d, s}^{0} \rightarrow \eta \eta, \eta^{\prime} \eta, \eta^{\prime} \eta^{\prime}$ modes, measurement on $B_{s}^{0} \rightarrow \eta^{\prime} \eta$ is helpful to extract $C P$-violating parameters from $\mathrm{SU}(3) / \mathrm{U}(3)$ symmetry [29]. $N_{\text {sig }}$ of $B_{s}^{0} \rightarrow \eta^{\prime} \eta$ is extracted by 3D fit with $\Delta E, M_{\mathrm{bc}}$, and $M_{\eta^{\prime}}$. We obtain $2.7 \pm 2.5$ events and set upper limits of $f_{s} \times \mathcal{B}\left(B_{s}^{0} \rightarrow \eta^{\prime} \eta\right)$ and $\mathcal{B}\left(B_{s}^{0} \rightarrow \eta^{\prime} \eta\right)$ as $1.3 \times 10^{-5}$ and $6.5 \times 10^{-5}$ at $90 \%$ C.L., respectively, where $f_{s}$ is the fraction of $B_{s}^{(*) 0} \bar{B}_{s}^{(*) 0}$ in $b \bar{b}$ events and its world average is $0.201 \pm 0.031$ [27].
$B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}$ decay contains contributions from gluonic and electroweak penguin amplitudes, such that it is sensitive to BSM physics [28] which can affect both decay rate and $C P$ asymmetries. $N_{\text {sig }}$ of $B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}$ is extracted by 3 D fit with $\Delta E, M_{\mathrm{bc}}$, and $M_{\eta^{\prime}}$. We obtain $-3.21 \pm 1.85$ events and set upper limits of $f_{s} \times \mathcal{B}\left(B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}\right)$ and $\mathcal{B}\left(B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}\right)$ as $1.64 \times 10^{-5}$ and $8.16 \times 10^{-5}$ at $90 \%$ C.L., respectively.

## 6. Summary

We report the results of several charmless $B$ decays using Belle data collected at $\Upsilon(4 S)$ or $\Upsilon(5 S)$ resonance. In addition to branching fraction measurement, we also look into the distribution of two-body invariant mass of $B^{0} \rightarrow p \bar{p} \pi^{+} \pi^{-}, B^{+} \rightarrow p \bar{p} \pi^{+} \pi^{0}, B^{+} \rightarrow K^{+} K^{-} \pi^{+}$, and $B^{+} \rightarrow \pi^{+} \pi^{0} \pi^{0}$ to study their decay structure. We do not observe significant signal yield for $B_{s}^{0} \rightarrow \eta^{\prime} X_{s \bar{s}}, B_{s}^{0} \rightarrow \eta^{\prime} \eta$, and $B_{s}^{0} \rightarrow \eta^{\prime} K_{S}^{0}$, and upper limits on branching fraction are estimated at $90 \%$ C.L.. In near future, larger data set from Belle II [30] can further improve the measurement on these decay modes.

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[^1]:    ${ }^{\dagger}$ Throughout this paper, inclusion of charge-conjugate decay modes is always implied.

[^2]:    ${ }^{\ddagger} M_{\pi^{+} \pi^{0}, \text { min }}$ refers to the smaller of two $M_{\pi^{+} \pi^{0}}$ values in a reconstructed $B$ candidate.

