

## Leptoquark and vectorlike quark extended models as the explanation of $(g - 2)_\mu$ anomaly

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In minimal leptoquark (LQ) models, the  $R_2$  and  $S_1$  can be the solution to the  $(g - 2)_\mu$  anomaly because of the chiral enhancements. Here, we study the LQ and vectorlike quark (VLQ) extended models. In the one LQ and one VLQ extended models, the  $(g - 2)_\mu$  can receive the contributions from top and top partner  $T$  because of the  $t - T$  mixing. Besides the traditional  $R_2$  and  $S_1$  representations, we find that the  $S_3$  LQ can also explain the anomaly when including the  $(X, T, B)_{L,R}$  triplet at the same time. Moreover, we find that the LQ has the new decay channel  $T\mu$  in these models.

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## 1. Introduction

The muon magnetic moment is well predicted in the standard model (SM) of elementary particle physics, and the most accurate calculation is  $a_\mu^{\text{SM}} = 116591810(43) \times 10^{-11}$  [1]. Its deviation from the SM prediction can be a good probe to new physics. The  $(g - 2)_\mu$  anomaly is first reported by the E821 experiment at BNL [2]. Last year, the FNAL muon  $g - 2$  experiment announces the average result  $a_\mu^{\text{Exp}} = 116592061(41) \times 10^{-11}$  after combining the BNL and FNAL data [3], which shows the  $4.2\sigma$  discrepancy with  $\Delta a_\mu \equiv a_\mu^{\text{Exp}} - a_\mu^{\text{SM}} = (251 \pm 59) \times 10^{-11}$ . There are many interpretations on this anomaly regardless of theoretical and experimental uncertainties, or new physics. In our paper [4], we propose the simultaneous scalar LQ and VLQ extended models to explain this anomaly.

## 2. The LQ and VLQ extended models

For the mediator with mass scale  $\Lambda$  above TeV, we have the rough estimation  $m_\mu^2/(8\pi^2\Lambda^2) \lesssim 10^{-10}$ . Thus, the chiral enhancements are required to explain the  $(g - 2)_\mu$ . In the minimal LQ models, only the  $R_2$  and  $S_1$  representations can lead to the left and right-handed (non-chiral) couplings to muons at the same time. In fact, the chiral enhancements are induced by the up-type quarks [5].

There are seven typical VLQs, while we are interested in the five types with top partner  $T$  [6], namely, the singlet  $T_{L,R}$ , doublets  $(X, T)_{L,R}/(T, B)_{L,R}$ , and triplets  $(X, T, B)_{L,R}/(T, B, Y)_{L,R}$ . Here, the  $X, T, B, Y$  quarks carry the  $5/3, 2/3, -1/3, -4/3$  electric charges, respectively. Although the five scalar LQs and five  $T$  VLQs can result in twenty-five combinations totally, only some combinations can lead to the up-type quark chiral enhancements. In the following, we will study these combinations, which are named as "LQ + VLQ" <sup>1</sup>.

After the electroweak symmetry breaking, there are  $t - T$  and  $b - B$  mixings with the mixing angles denoted as  $\theta_{L,R}^t$  (also  $\theta_{L,R}$ ) and  $\theta_{L,R}^b$ . Hereafter, the  $\sin \theta_{L,R}$  and  $\cos \theta_{L,R}$  will be abbreviated as  $s_{L,R}$  and  $c_{L,R}$  (similar to the  $b$ ). For the mentioned VLQs, there is only one independent mixing angle except for the  $(T, B)_{L,R}$  with two independent mixing angles  $\theta_R^t$  and  $\theta_R^b$ . In our paper [4], we list the relevant input parameters and mixing angle identities. For the singlet and triplet VLQs, the  $\theta_L$  is chosen as the input mixing angle. For the doublet VLQs, the  $\theta_R$  is chosen as the input mixing angle [6]. In Tab. 1, we parametrize the couplings in front of the  $\bar{\mu}t(R_2^{5/3})^*$ ,  $\bar{\mu}T(R_2^{5/3})^*$ ,  $\bar{\mu}t^C(S_1)^*$ ,  $\bar{\mu}T^C(S_1)^*$ ,  $\bar{\mu}t^C(S_3^{1/3})^*$ , and  $\bar{\mu}T^C(S_3^{1/3})^*$  interactions. In Tab. 2, we also list the couplings in front of the  $\bar{\mu}b(R_2^{2/3})^*$ ,  $\bar{\mu}B(R_2^{2/3})^*$ ,  $\bar{\mu}b^C(S_3^{4/3})^*$ , and  $\bar{\mu}B^C(S_3^{4/3})^*$  interactions.

## 3. Contributions to the $(g - 2)_\mu$

In all of the mentioned models, there are top and  $T$  quark contributions with chiral enhancements. In the  $R_2 + \text{VLQ}$  models, there are also  $b$  and  $B$  quark contributions. In the  $S_1 + \text{VLQ}$  models, there are no  $b$  or  $B$  quark contributions. In the  $R_2/S_3 + (X, T, B)_{L,R}$  models, the  $b$  and  $B$  quark contributions are also chirally enhanced. For the models with  $X$  quark, the  $X$  quark only contributes in the  $S_3 + (X, T, B)_{L,R}$  model but without the chiral enhancements. For the  $R_2/S_1 + (T, B, Y)_{L,R}$  models, the  $Y$  quark does not contribute to  $(g - 2)_\mu$ .

<sup>1</sup>In our paper [4], we also investigate the one LQ and two VLQ extended models.

LQ	VLQ	$\overline{\mu_R}^i L$	$\overline{\mu_L}^i T$	$\overline{\mu_R}^i T_L$	$\overline{\mu_L}^i T_R$
$R_2$	$T_{L,R}$	$y_L^{R_2\mu T} c_L$	$y_R^{R_2\mu T} c_R - y_R^{R_2\mu T} s_R$	$y_L^{R_2\mu T} s_L$	$y_R^{R_2\mu T} s_R + y_R^{R_2\mu T} c_R$
	$(X, T)_{L,R}$	$y_L^{R_2\mu T} c_L$	$y_R^{R_2\mu T} c_R$	$y_L^{R_2\mu T} s_L$	$y_R^{R_2\mu T} s_R$
	$(T, B)_{L,R}$	$y_L^{R_2\mu T} c_L - y_L^{R_2\mu T} s_L$	$y_R^{R_2\mu T} c_R$	$y_L^{R_2\mu T} s_L + y_L^{R_2\mu T} c_L$	$y_R^{R_2\mu T} s_R$
	$(X, T, B)_{L,R}$	$y_L^{R_2\mu T} c_L$	$y_R^{R_2\mu T} c_R - y_R^{R_2\mu T} s_R$	$y_L^{R_2\mu T} s_L$	$y_R^{R_2\mu T} s_R + y_R^{R_2\mu T} c_R$
	$(T, B, Y)_{L,R}$	$y_L^{R_2\mu T} c_L$	$y_R^{R_2\mu T} c_R$	$y_L^{R_2\mu T} s_L$	$y_R^{R_2\mu T} s_R$
LQ	VLQ	$\overline{\mu_R}(t_R)^C$	$\overline{\mu_L}(t_L)^C$	$\overline{\mu_R}(T_R)^C$	$\overline{\mu_L}(T_L)^C$
$S_1$	$T_{L,R}$	$y_L^{S_1\mu T} c_R - y_L^{S_1\mu T} s_R$	$y_R^{S_1\mu T} c_L$	$y_L^{S_1\mu T} s_R + y_L^{S_1\mu T} c_R$	$y_R^{S_1\mu T} s_L$
	$(X, T)_{L,R}$	$y_L^{S_1\mu T} c_R$	$y_R^{S_1\mu T} c_L$	$y_L^{S_1\mu T} s_R$	$y_R^{S_1\mu T} s_L$
	$(T, B)_{L,R}$	$y_L^{S_1\mu T} c_R$	$y_R^{S_1\mu T} c_L - y_R^{S_1\mu T} s_L$	$y_L^{S_1\mu T} s_R$	$y_R^{S_1\mu T} s_L + y_R^{S_1\mu T} c_L$
	$(X, T, B)_{L,R}$	$y_L^{S_1\mu T} c_R$	$y_R^{S_1\mu T} c_L$	$y_L^{S_1\mu T} s_R$	$y_R^{S_1\mu T} s_L$
	$(T, B, Y)_{L,R}$	$y_L^{S_1\mu T} c_R$	$y_R^{S_1\mu T} c_L$	$y_L^{S_1\mu T} s_R$	$y_R^{S_1\mu T} s_L$
$S_3$	$(X, T, B)_{L,R}$	$-y_L^{S_3\mu T} s_R$	$y_R^{S_3\mu T} c_L$	$y_L^{S_3\mu T} c_R$	$y_R^{S_3\mu T} s_L$

Table 1: The  $LQ\mu t/T$  couplings in the LQ+VLQ models.

LQ	VLQ	$\overline{\mu_R} b_L$	$\overline{\mu_L} b_R$	$\overline{\mu_R} B_L$	$\overline{\mu_L} B_R$
$R_2$	$T_{L,R}$	$y_L^{R_2\mu T}$	0	×	×
	$(X, T)_{L,R}$	$y_L^{R_2\mu T}$	0	×	×
	$(T, B)_{L,R}$	$y_L^{R_2\mu T} c_L^b - y_L^{R_2\mu T} s_L^b$	0	$y_L^{R_2\mu T} c_L^b + y_L^{R_2\mu T} s_L^b$	0
	$(X, T, B)_{L,R}$	$y_L^{R_2\mu T} c_L^b$	$-\sqrt{2}y_R^{R_2\mu T} s_R^b$	$y_L^{R_2\mu T} s_L^b$	$\sqrt{2}y_R^{R_2\mu T} c_R^b$
	$(T, B, Y)_{L,R}$	$y_L^{R_2\mu T} c_L^b$	0	$y_L^{R_2\mu T} s_L^b$	0
LQ	VLQ	$\overline{\mu_R}(b_R)^C$	$\overline{\mu_L}(b_L)^C$	$\overline{\mu_R}(B_R)^C$	$\overline{\mu_L}(B_L)^C$
$S_1$	$T_{L,R}$	0	0	×	×
	$(X, T)_{L,R}$	0	0	×	×
	$(T, B)_{L,R}$	0	0	0	0
	$(X, T, B)_{L,R}$	0	0	0	0
	$(T, B, Y)_{L,R}$	0	0	0	0
$S_3$	$(X, T, B)_{L,R}$	$-y_L^{S_3\mu T} s_R^b$	$\sqrt{2}y_R^{S_3\mu T} c_L^b$	$y_L^{S_3\mu T} c_R^b$	$\sqrt{2}y_R^{S_3\mu T} s_L^b$

Table 2: The  $LQ\mu b/B$  couplings in the LQ+VLQ models. The symbol “×” means no such interactions.

The complete contributions can be obtained from our paper [4]. Of course, they are dominated by the chirally enhanced contributions, because the non-chirally enhanced contributions are suppressed by the factor  $m_\mu/m_t(m_T) \leq 10^{-3}$ . Considering  $m_b \ll m_t \ll m_T \approx m_B$ , and  $s_{L,R} \ll 1$ , we show the approximate formulae of  $\Delta a_\mu$  in Tab. 3. In the  $R_2 + (X, T)_{L,R}/(T, B, Y)_{L,R}$  and  $S_1 + (X, T)_{L,R}/(X, T, B)_{L,R}/(T, B, Y)_{L,R}$  models, the  $T$  contributions are highly suppressed by the factor  $m_t s_{L,R}^2/m_T$ . In the  $R_2 + T_{L,R}/(T, B)_{L,R}/(X, T, B)_{L,R}$  and  $S_1 + T_{L,R}/(T, B)_{L,R}$  models, the  $T$  contributions are suppressed by the mixing angle  $s_{L,R}$ . In the  $S_3 + (X, T, B)_{L,R}$  model, the  $T$  and  $B$  quark contributions are dominated than top by the factor  $m_T/m_t$ .

LQ	VLQ	the approximate expressions of $\Delta\bar{a}_\mu$	coupling product order of $T$ compared to $t$
$R_2$	$T_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{R_2} (m_T^2/m_{R_2}^2) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*] s_L + (\frac{1}{4} + \log \frac{m_T^2}{m_{R_2}^2}) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*]$	$s_L$
	$(X, T)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{R_2} (m_T^2/m_{R_2}^2) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*] s_L s_R + (\frac{1}{4} + \log \frac{m_T^2}{m_{R_2}^2}) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*]$	$m_t s_R^2/m_T$
	$(T, B)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{R_2} (m_T^2/m_{R_2}^2) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*] s_R + (\frac{1}{4} + \log \frac{m_T^2}{m_{R_2}^2}) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*]$	$s_R$
	$(X, T, B)_{L,R}$	$\frac{m_T}{m_t} [f_{LR}^{R_2} (m_T^2/m_{R_2}^2) + 2\tilde{f}_{LR}^{R_2} (m_T^2/m_{R_2}^2)] \cdot \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*] s_L + (\frac{1}{4} + \log \frac{m_T^2}{m_{R_2}^2}) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*]$	$s_L$
	$(T, B, Y)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{R_2} (m_T^2/m_{R_2}^2) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*] s_L s_R + (\frac{1}{4} + \log \frac{m_T^2}{m_{R_2}^2}) \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu T})^*]$	$m_t s_L^2/m_T$
$S_1$	$T_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{S_1} (m_T^2/m_{S_1}^2) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*] s_L - (\frac{7}{4} + \log \frac{m_T^2}{m_{S_1}^2}) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*]$	$s_L$
	$(X, T)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{S_1} (m_T^2/m_{S_1}^2) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*] s_L s_R - (\frac{7}{4} + \log \frac{m_T^2}{m_{S_1}^2}) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*]$	$m_t s_R^2/m_T$
	$(T, B)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{S_1} (m_T^2/m_{S_1}^2) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*] s_R - (\frac{7}{4} + \log \frac{m_T^2}{m_{S_1}^2}) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*]$	$s_R$
	$(X, T, B)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{S_1} (m_T^2/m_{S_1}^2) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*] s_L s_R - (\frac{7}{4} + \log \frac{m_T^2}{m_{S_1}^2}) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*]$	$m_t s_L^2/m_T$
	$(T, B, Y)_{L,R}$	$\frac{m_T}{m_t} f_{LR}^{S_1} (m_T^2/m_{S_1}^2) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*] s_L s_R - (\frac{7}{4} + \log \frac{m_T^2}{m_{S_1}^2}) \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu T})^*]$	$m_t s_L^2/m_T$
$S_3$	$(X, T, B)_{L,R}$	$\frac{m_T}{m_t} [f_{LR}^{S_3} (m_T^2/m_{S_3}^2) + 2\tilde{f}_{LR}^{S_3} (m_T^2/m_{S_3}^2)] \cdot \text{Re}[y_L^{S_3\mu T} (y_R^{S_3\mu T})^*] s_L + (\frac{7}{4} + \log \frac{m_T^2}{m_{S_3}^2}) \text{Re}[y_L^{S_3\mu T} (y_R^{S_3\mu T})^*] s_R$	$m_T/m_t$

**Table 3:** In the third column, we show the approximate formulae of the  $\Delta a_\mu$ . In the fourth column, we show the order of the multiplication of left and right-handed  $T$  LQ Yukawa couplings with respect to the top quark. In the above, we redefine  $\Delta a_\mu$  as  $m_\mu m_t \Delta\bar{a}_\mu / (4\pi^2 m_{LQ}^2)$ .

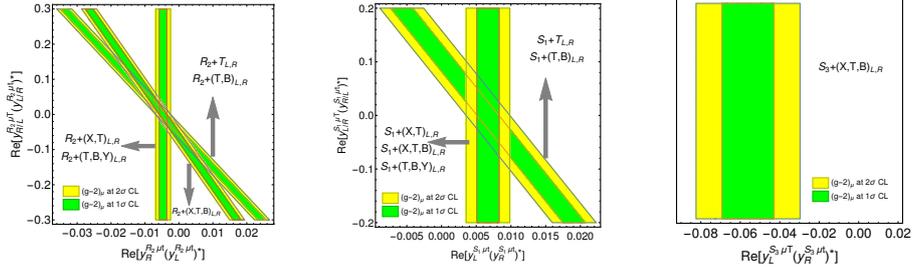
#### 4. Numerical analysis

We choose the input parameters as  $m_\mu = 105.66\text{MeV}$ ,  $m_b = 4.2\text{GeV}$ , and  $m_t = 172.5\text{GeV}$  [7]. For the VLQ parameters, the main constraints are from direct search [8, 9] and electro-weak precision observables [6, 10], which require the VLQ mass to be  $\mathcal{O}(\text{TeV})$  and the input mixing angle to be less than 0.1. For the LQ mass, the direct search requires it to be above TeV [11, 12]. Then, we adopt the mass parameters to be  $m_T = 1\text{TeV}$  and  $m_{LQ} = 2\text{TeV}$  by default. The input mixing angle is set as  $s_L = 0.05$  (singlet and triplet VLQs) and  $s_R = 0.05$  (doublet VLQs). In Fig. 1, we show the regions allowed at  $1\sigma$  (green) and  $2\sigma$  (yellow) CL, respectively.

#### 5. LQ Phenomenology at hadron colliders

In the minimal  $R_2/S_1$  models, the LQ decay final states are SM quark and lepton. In the LQ+VLQ models, there are new LQ decay channels. Here, we will study the  $R_2^{5/3} \rightarrow t/T\mu^+$  and  $S_1/S_3^{1/3} \rightarrow \bar{t}/\bar{T}\mu^+$  decay channels<sup>2</sup>. Considering  $m_t \ll m_T$  and  $s_{L,R} \ll 1$ , we show the approximate expressions of  $\Gamma(\text{LQ} \rightarrow T\mu)/\Gamma(\text{LQ} \rightarrow t\mu)$  in Tab. 4. Then, we find that the  $T\mu$  decay channel is important in the  $R_2 + T_{L,R}/(T, B)_{L,R}/(X, T, B)_{L,R}$ ,  $S_1 + T_{L,R}/(T, B)_{L,R}$ , and

<sup>2</sup>For the other LQs, the decay channels can be  $R_2^{2/3} \rightarrow b/B\mu^+$ ,  $S_3^{4/3} \rightarrow \bar{b}/\bar{B}\mu^+$ , and  $S_3^{-2/3} \rightarrow \bar{X}\mu^+$ .



**Figure 1:** The allowed region in the plane of  $\text{Re}[y_{R/L}^{R_2\mu T} (y_{R/L}^{R_2\mu t})^*] - \text{Re}[y_R^{R_2\mu T} (y_L^{R_2\mu t})^*]$  (left,  $R_2 + \text{VLQ}$ ) and  $\text{Re}[y_{L/R}^{S_1\mu T} (y_{R/L}^{S_1\mu t})^*] - \text{Re}[y_L^{S_1\mu T} (y_R^{S_1\mu t})^*]$  (middle,  $S_1 + \text{VLQ}$ ). The right is for the  $S_3 + (X, T, B)_{L,R}$  model.

$S_3 + (X, T, B)_{L,R}$  models. For the LQ production, there are pair, single, and off-shell channels.

LQ	VLQ	the approximate expressions of $\Gamma(\text{LQ} \rightarrow T\mu)/\Gamma(\text{LQ} \rightarrow t\mu)$	suppress or not
$R_2$	$T_{L,R}$	$(1 - \frac{m_T^2}{m_{R_2}^2})^2  y_R^{R_2\mu T} ^2 / ( y_L^{R_2\mu t} ^2 +  y_R^{R_2\mu t} ^2)$	No
	$(X, T)_{L,R}$	$(1 - \frac{m_T^2}{m_{R_2}^2})^2  y_R^{R_2\mu T} ^2 s_R^2 / ( y_L^{R_2\mu t} ^2 +  y_R^{R_2\mu t} ^2)$	$s_R^2$
	$(T, B)_{L,R}$	$(1 - \frac{m_T^2}{m_{R_2}^2})^2  y_L^{R_2\mu T} ^2 / ( y_L^{R_2\mu t} ^2 +  y_R^{R_2\mu t} ^2)$	No
	$(X, T, B)_{L,R}$	$(1 - \frac{m_T^2}{m_{R_2}^2})^2  y_R^{R_2\mu T} ^2 / ( y_L^{R_2\mu t} ^2 +  y_R^{R_2\mu t} ^2)$	No
	$(T, B, Y)_{L,R}$	$(1 - \frac{m_T^2}{m_{R_2}^2})^2  y_L^{R_2\mu T} ^2 s_L^2 / ( y_L^{R_2\mu t} ^2 +  y_R^{R_2\mu t} ^2)$	$s_L^2$
$S_1$	$T_{L,R}$	$(1 - \frac{m_T^2}{m_{S_1}^2})^2  y_L^{S_1\mu T} ^2 / ( y_L^{S_1\mu t} ^2 +  y_R^{S_1\mu t} ^2)$	No
	$(X, T)_{L,R}$	$(1 - \frac{m_T^2}{m_{S_1}^2})^2  y_L^{S_1\mu T} ^2 s_R^2 / ( y_L^{S_1\mu t} ^2 +  y_R^{S_1\mu t} ^2)$	$s_R^2$
	$(T, B)_{L,R}$	$(1 - \frac{m_T^2}{m_{S_1}^2})^2  y_R^{S_1\mu T} ^2 / ( y_L^{S_1\mu t} ^2 +  y_R^{S_1\mu t} ^2)$	No
	$(X, T, B)_{L,R}$	$(1 - \frac{m_T^2}{m_{S_1}^2})^2  y_R^{S_1\mu T} ^2 s_L^2 / ( y_L^{S_1\mu t} ^2 +  y_R^{S_1\mu t} ^2)$	$s_L^2$
	$(T, B, Y)_{L,R}$	$(1 - \frac{m_T^2}{m_{S_1}^2})^2  y_R^{S_1\mu T} ^2 s_L^2 / ( y_L^{S_1\mu t} ^2 +  y_R^{S_1\mu t} ^2)$	$s_L^2$
$S_3$	$(X, T, B)_{L,R}$	$(1 - \frac{m_T^2}{m_{S_3}^2})^2  y_L^{S_3\mu T} ^2 /  y_R^{S_3\mu t} ^2$	No

**Table 4:** In the third column, we list the approximate formulae of  $T\mu$  partial decay width over  $t\mu$  in the LQ+VLQ models. In the fourth column, we show the order of  $\Gamma(\text{LQ} \rightarrow T\mu)$  compared to the  $\Gamma(\text{LQ} \rightarrow t\mu)$ .

What is more, the  $T$  quark can decay into the  $bW, tZ, th$  final states further. Thus, it will lead to the characteristic multi-top and multi-muon signals at hadron colliders.

## 6. Summary and conclusions

We explain the  $(g - 2)_\mu$  anomaly in the LQ and VLQ extended models. In the  $R_2 + (X, T)_{L,R}/(T, B, Y)_{L,R}$  and  $S_1 + (X, T)_{L,R}/(X, T, B)_{L,R}/(T, B, Y)_{L,R}$  models, it is dominated by the top quark contributions. In the  $R_2 + T_{L,R}/(T, B)_{L,R}/(X, T, B)_{L,R}$  and  $S_1 + T_{L,R}/(T, B)_{L,R}$  models, both the top and  $T$  quark contributions are important. In the  $S_3 + (X, T, B)_{L,R}$  model, it is dominated by the  $T$  and  $B$  quark contributions. In addition to the conventional  $t\mu$  decay channel, the LQ can also

decay into  $T\mu$  final states, which can become important in the  $R_2 + T_{L,R}/(T, B)_{L,R}/(X, T, B)_{L,R}$ ,  $S_1 + T_{L,R}/(T, B)_{L,R}$  models, and  $S_3 + (X, T, B)_{L,R}$  models.

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## References

- [1] T. Aoyama et al. The anomalous magnetic moment of the muon in the Standard Model. *Phys. Rept.*, 887:1–166, 2020.
- [2] G. W. Bennett et al. Final Report of the Muon E821 Anomalous Magnetic Moment Measurement at BNL. *Phys. Rev. D*, 73:072003, 2006.
- [3] B. Abi et al. Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm. *Phys. Rev. Lett.*, 126(14):141801, 2021.
- [4] Shi-Ping He. Leptoquark and vectorlike quark extended models as the explanation of the muon  $g - 2$  anomaly. *Phys. Rev. D*, 105(3):035017, 2022. [Erratum: *Phys.Rev.D* 106, 039901 (2022)].
- [5] I. Doršner, S. Fajfer, A. Greljo, J. F. Kamenik, and N. Košnik. Physics of leptoquarks in precision experiments and at particle colliders. *Phys. Rept.*, 641:1–68, 2016.
- [6] J. A. Aguilar-Saavedra, R. Benbrik, S. Heinemeyer, and M. Pérez-Victoria. Handbook of vectorlike quarks: Mixing and single production. *Phys. Rev. D*, 88(9):094010, 2013.
- [7] P. A. Zyla et al. Review of Particle Physics. *PTEP*, 2020(8):083C01, 2020.
- [8] Albert M Sirunyan et al. Search for vector-like quarks in events with two oppositely charged leptons and jets in proton-proton collisions at  $\sqrt{s} = 13$  TeV. *Eur. Phys. J. C*, 79(4):364, 2019.
- [9] Morad Aaboud et al. Combination of the searches for pair-produced vector-like partners of the third-generation quarks at  $\sqrt{s} = 13$  TeV with the ATLAS detector. *Phys. Rev. Lett.*, 121(21):211801, 2018.
- [10] Chien-Yi Chen, S. Dawson, and Elisabetta Furlan. Vectorlike fermions and Higgs effective field theory revisited. *Phys. Rev. D*, 96(1):015006, 2017.
- [11] Albert M Sirunyan et al. Search for leptoquarks coupled to third-generation quarks in proton-proton collisions at  $\sqrt{s} = 13$  TeV. *Phys. Rev. Lett.*, 121(24):241802, 2018.
- [12] Georges Aad et al. Search for pair production of scalar leptoquarks decaying into first- or second-generation leptons and top quarks in proton-proton collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector. *Eur. Phys. J. C*, 81(4):313, 2021.