One of the most interesting channels to search for SUSY is the direct pair-production of the \( \tilde{\tau} \)-lepton superpartner, \( \tilde{\tau} \). The \( \tilde{\tau} \) is with high probability the lightest of the scalar leptons, so one of the first SUSY particles that can be observed, and the signature of \( \tilde{\tau} \) pair production signal events is one of the most difficult ones, yielding to the “worst” and so most global scenario for the searches. Analysis performed at LEP set the current model-independent \( \tilde{\tau} \) limits, suffering from the low energy of this facility. Only under strong model assumptions, these limits are extended to higher masses by LHC studies. In this contribution we show the capability of the ILC, a future electron-positron collider with energy up to 1 TeV, for determining \( \tilde{\tau} \) exclusion/discovery limits in a model-independent way, including an overview of the current state-of-the-art. The determination of the “worst” scenario for \( \tilde{\tau} \) exclusion/discovery, taking into account the effect of the \( \tilde{\tau} \) mixing on \( \tilde{\tau} \) production cross-section and efficiency, is also presented. For selected benchmarks, the prospect for measuring masses and polarised cross-sections will be shown. The studies were done studying events passed through the full detector simulation and reconstruction procedures of the International Large Detector (ILD) concept at the ILC. The simulation included all SM backgrounds, as well as the machine induced ones.
1. Introduction and limits at other facilities

Two important conditions when searching for SUSY at future facilities are look for the lightest accessible particle in the SUSY spectrum and cover the most difficult scenario. Both of them are satisfied by the $\tilde{\tau}$. As a consequence of the mixing of both $\tilde{\tau}$ weak hyper-charge states, $\tilde{\tau}_L$ and $\tilde{\tau}_R$, it is expected that the lightest of its physical states, $\tilde{\tau}_1$, will be the lightest slepton. This mixing also points out to a lower cross-section: the strength of the $Z^0/\gamma$ $\tilde{\tau} \tilde{\tau}$ coupling depends on the $\tilde{\tau}$ mixing, reaching its minimum value when the coupling $\tilde{\tau}_1 \tilde{\tau} Z^0$ vanishes. A difficult experimental signature is due to the fact that its SM partner is unstable, decaying before it can be detected, and, as a further complication, some of its decay products are undetectable neutrinos. One can conclude that any other NLSP would be easier to find than the $\tilde{\tau}$ and, therefore, $\tilde{\tau}$ production studies might be seen as the way to determine the guaranteed discovery or exclusion reach for SUSY. $\tilde{\tau}$ studies are also theoretically motivated: the observed relic density could be accomodated with a light $\tilde{\tau}$ due to an enhanced $\tilde{\tau}$-neutralino coannihilation. Figure 1(a) shows the $\tilde{\tau}$ mass limits from LEP experiments [1], being the most model-independent ones. Depending on the mass difference between the $\tilde{\tau}$ and the neutralino, the minimum value of the $\tilde{\tau}$ mass ranges from 87 to 93 GeV. The limits are valid for any mixing and any value of the model-parameters not shown in the plot.

![Figure 1](image_url)

Figure 1: (a): 95% CL exclusion limits for $\tilde{\tau}$ pair production obtained combining data collected at the four LEP experiments with energies ranging from 183 GeV to 208 GeV. From [1]. (b): 95% CL exclusion and discovery potential for $\tilde{\tau}$ pair production at the HL-LHC, assuming $\tilde{\tau}_L\tilde{\tau}_L + \tilde{\tau}_R\tilde{\tau}_R$ production, $\tilde{\tau}_L\tilde{\tau}_L$ production or $\tilde{\tau}_R\tilde{\tau}_R$ production. From [3].

A $\tilde{\tau}$ mass below 26.3 GeV, for any mixing and any mass difference larger than the $\tau$ mass, is excluded by an analysis from the DELPHI experiment targeted at low mass differences [2].

The limits on the $\tilde{\tau}$ mass determined at the LHC are only valid under certain assumptions: ATLAS and CMS assume $\tilde{\tau}_R$ and $\tilde{\tau}_L$ to be mass-degenerate and without mixing. The future HL-LHC should provide an improvement on the $\tilde{\tau}$ limits. Indeed simulation studies have already been performed in both experiments [3, 4], providing upper limits for $\tilde{\tau}$ masses increased by about 300 GeV with respect to the ones from the previous studies, but still suffering from the same constraints. ATLAS limits for pure $\tilde{\tau}_R$ pair production, that could be considered the closest case to
the physical lightest \(\tilde{\tau}\) since it is likely to be the lightest of the two weak hyper-charge states and the one with the lower cross section, show no discovery potential (see figure 1(b)), only exclusion one. Neither discovery nor exclusion potential is shown for the scenario allowing \(\tilde{\tau}\)-neutralino co-annihilation.

2. Signal and background

This study assumes R-parity conservation, the \(\tilde{\tau}\) as the NLSP, and mass differences above the mass of the \(\tau\). Under these conditions, \(\tilde{\tau}\)’s will be produced in pairs via \(Z/\gamma\) exchange in the s-channel and they will decay to a \(\tau\) and an LSP. The \(\tau\) will decay before leaving any signal in the detectors while the LSP will leave the detector without being detected. The only detectable activity in the signal events is therefore the visible decay products of the two \(\tau\)’s. These signal events are then characterised by a large missing energy and momentum (due to invisible LSPs and neutrinos from both \(\tau\)-decays), large fraction of the detected activity in the central region of the detector (\(\tilde{\tau}\)’s are scalars), un-balanced transverse momentum, large angles between the two \(\tau\)-lepton directions and zero forward-backward asymmetry (direction of the \(\tilde{\tau}\) does not strongly correlate to that of the visible \(\tau\) after the decay). The main sources of background are SM processes with real or fake missing energy. They can be classified into “irreducible” and “almost irreducible” sources. The first are events with two \(\tau\)’s and neutrinos, i.e. real missing energy, being the main contribution \(ZZ\) events with one \(Z\) decaying to two neutrinos and the other to two \(\tau\)’s, and leptonic \(WW\) events, where both the \(W\)’s decays to \(\tau\) and neutrino. The second group of events are those looking after reconstruction very similar to two \(\tau\)’s and neutrinos, mainly events with two soft \(\tau\)-jets, with two other leptons plus true missing energy or with two \(\tau\)’s plus fake missing energy.

3. Analysis and limits

According to the H-20 running scenario for the ILC500 [5], an integrated luminosity of 1.6 ab\(^{-1}\) at \(\sqrt{s} = 500\) GeV for each of the beam polarisations, \(P(e^-, e^+) = (+80\%, -30\%)\) and \(P(e^-, e^+) = (-80\%, +30\%)\), was assumed in the study. The “worst” scenario for \(\tilde{\tau}\) exclusion/discovery was analysed taking into account the effect of the \(\tilde{\tau}\) mixing on \(\tilde{\tau}\) production cross-section and efficiency. Figure 2(a) shows the signal over background significance as a function of the mixing angle for each polarisation. The final significance was computed weighting the contribution of both polarisations by the likelihood ratio statistic. Figure 2(b) plots the results, showing a rather uniform sensitivity to all mixing angles. For the smallest mass differences, the critical ones, a mixing angle around 53°, corresponding to the lowest cross-section for unpolarised beams, can be taken as the worst case for the ILC conditions.

Cuts for separating signal from background have been designed taking into account the signal signature and the main background sources. The first group of cuts are those in properties that the \(\tilde{\tau}\)-events must have, meaning cuts in missing energy, visible mass, maximum total momentum and maximum momentum of the jets. An algorithm for \(\tau\)-identification was also applied. A second group of cuts is based on those properties that the \(\tilde{\tau}\)-events might have, but the background events will rarely have, allowing to set cuts requiring high missing transverse momentum \((P_{T\text{miss}})\), large acoplanarity \(\theta_{acop}\), large angle to the beam, and large value of the variable \(\rho\), calculated by first
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Figure 2: (a): Signal over background significance as a function of the $\tilde{\tau}$ mixing angle for both main ILC polarisations. (b) Signal over background significance weighting both polarisations using the likelihood-ratio static in the H-20 ILC conditions.

Figure 3 shows the significance obtained with and without cuts together with the results from the SGV fast simulations [5] (without overlay tracks). For the case with the smallest mass difference, shown in figure 3(a), there is a strong reduction of the significance when adding overlay tracks. For the larger mass-difference ((figure 3(b)) the degradation is slight. In both cases the overlay removal ameliorates the sensitivity.

Figure 4 [5] shows the projection of the limits in the $M_{\tilde{\tau}}$-$\Delta M$ plane, together with the limits from LEP and the projected HL-LHC ones (to be taken with care due to the high model dependence). Extrapolation of the ILC limits for the scenarios with centre-of-mass energy 250 GeV and 1 TeV is also shown. One can observe that for the ILC exclusion and discovery limits are very close to each other and to the ILC kinematic limit. The region for mass differences below the mass of the $\tau$
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Figure 3: Number of sigmas for a $\tilde{\tau}$ with mass 240 GeV and different mass-differences. The plot assumes H-20 ILC scenario combining both polarisations using the likelihood-ratio statistic. Blue lines correspond to the case with all the tracks and the red ones after rejecting tracks not satisfying the cuts described in the text. The green curves correspond to the study without overlay tracks.

is shown for completeness, even if it was not included in this study.

For specific benchmarks the $M_{\tilde{\tau}}$ was computed based on the end-point of the spectrum from $\tau$ decays and on the $\tilde{\tau}$ cross-sections, achieving per mil-level precision on the measurements. $\tau$ polarisation and $\tilde{\tau}$ mixing angle were also computed based on the spectrum of the $\tau$ decays and $\tilde{\tau}$ cross-sections and masses, respectively. Percent level precision was reached in those cases [6].

4. Outlook and conclusions

The ILC is presented as a promising scenario for SUSY studies. At this future facility $\tilde{\tau}$-pair production could be excluded/discovered up to a few GeV below the kinematic limit, even in the worst scenario and without model dependencies.

Well motivated regions of the SUSY parameter space, that would most probably not be covered by the HL-LHC, could be studied.

The effect of the overlay particles, that can no be neglected, is however mitigated applying optimized tracks.

If the $\tilde{\tau}$ exists in the kinematic range of the ILC, precision measurements of $\tilde{\tau}$ properties could be measured at a few percent level.

References

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Figure 4: $\tilde{\tau}$ limits in the $M_{\tilde{\tau}}-\Delta M$ plane. ILC results from the current studies are shown together with limits from LEP and LHC. The region with mass differences below the mass of the $\tau$ is also shown with LEP and LHC results, even if it is not covered by this study. In addition, the extrapolation of the ILC current results to the ILC 250 GeV and 1 TeV running scenarios is show.


[3] [ATLAS], “Prospects for searches for staus, charginos and neutralinos at the high luminosity LHC with the ATLAS Detector”, ATL-PHYS-PUB-2018-048.

[4] [CMS], “Search for supersymmetry with direct stau production at the HL-LHC with the CMS Phase-2 detector”, CMS-PAS-FTR-18-010.
