

Differential N³LO QCD corrections to charged current production at the LHC

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Charged current Drell-Yan production at hadron colliders is a benchmark electroweak process. A recent measurement of the W boson mass by the CDF experiment displays a large deviation from the Standard Model prediction. To enable precision phenomenology for this process, we compute the third-order (N^3LO) QCD corrections to the rapidity distribution in W boson production and to the transverse mass distribution of its decay products. We study kinematic regions relevant for the LHC experiments and assess the numerical magnitude of uncertainties from electroweak input parameters and parton distribution functions.

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1. Introduction

Charged-current Drell-Yan production mediated by electroweak (EW) gauge bosons W^{\pm} is a fundamental process at hadron colliders [1]. Measurements of the inclusive and differential properties of W boson production have been performed at the Large Hadron Collider (LHC) and Fermilab Tevatron [2–9]. Electroweak parameters of the Standard Model (SM) such as the W boson mass, decay width, weak mixing angle, and parton distribution functions (PDFs) in the proton can be determined by precision measurements of charged-current Drell-Yan production. Recently a study by the CDF collaboration using a sample of approximately 4 million W bosons collected at the Tevatron reports the W boson mass $M_W = 80433.5 \pm 9.4$ MeV [10]. The result deviates by 7 standard deviations from the SM electroweak precision fit of $M_W = 80357 \pm 6$ MeV [11, 12], which is itself in good agreement of measurements by ATLAS [4] and LHCb [5] as well as the previous CDF result [2]. Direct measurements of the W boson mass have limited resolution due to missing energy of the neutrino in the final state charged lepton-neutrino system. Precise measurements of M_W are thus based on template fits to differential observables. Both the CDF [2, 10] and ATLAS [4] analyses include distributions of final state charged lepton transverse momentum and transverse mass of the lepton-neutrino system as fitting observables. The measured distributions are compared with theory predictions with various input values. The M_W parameter that achieves the best fit corresponds to the measured central value of W boson mass. The uncertainty associated with the measurement is a combination of statistic and systematic errors from both experimental analysis and theory predictions.

The accuracy of theory predictions in charged current Drell-Yan production directly impact measurements of the SM electroweak parameters. Rapid progress has been achieved in perturbative QCD with next-to-leading order (NLO, [13]) and next-to-next-to-leading order (NNLO, [14]) corrections available for a while. Fully differential NNLO QCD corrections [15–18] are routinely used in the experimental analysis of Drell-Yan production. The third order (N³LO) corrections in QCD were accomplished recently for inclusive cross sections [19] and for differential predictions [20]. QCD resummation of large logarithmic corrections has been combined with fixed order predictions [21–23] with up to next-to-next-to-leading logarithmic (N³LL) accuracy [24–26]. These QCD corrections for the charged current Drell-Yan process combine with NLO EW [27–29] and mixed QCD-EW corrections [30–34] to achieve theory predictions at high quantitative accruacy. Impact from the parton distribution functions (PDFs) on M_W determinations has been studied with NLO QCD plus parton shower corrections [35–38] or scaled to NNLO precision [39, 40].

In this study, we focus on the rapidity distribution of W boson production and the transverse mass distribution of its decay products, which we newly compute to N³LO in QCD. We identify characteristic changes at NNLO QCD accuracy in differential distributions caused by shifting EW input parameters such as M_W and Γ_W , implementing an alternative Breit-Wigner parametrisation between fixed and running decay width, and switching between choices of modern PDFs. We further compare the uncertainties from above analysis at NNLO to N³LO predictions in [20]. This work provides guidance for the estimation of theoretical uncertainties in future precision measurements of SM parameters associated with charged-current Drell-Yan production.

2. Implementation

Our prediction of the perturbative QCD corrections of charged-current Drell-Yan production up to NNLO is provided by the parton level event generator NNLOJET, which implements the antenna subtraction method [41–43]. The state-of-the-art differential N³LO correction is achieved through an established framework [20, 44–46] using the q_T -subtraction formalism [47]. It requires the combination of numerically robust NNLO Drell-Yan-plus-jet production evaluated at low transverse momentum cut-off [48, 49] with unresolved N³LO contributions including logarithmic divergent terms [50–56] predicted via Soft-Collinear Effective Theory (SCET) [57–61].

Our calculation for the charged-current Drell-Yan production is performed for LHC kinematics with center-of-mass energy at 13 TeV. The default EW parameters are based on the G_{μ} scheme with $M_Z = 91.1876 \text{ GeV}$, $\Gamma_Z = 2.4952 \text{ GeV}$, $G_F = 1.1663787 \times 10^{-5} \text{ GeV}^{-2}$ [12]. The CKM matrix is considered to be diagonal. For each perturbative QCD order, we apply the same PDFs with $\alpha_s(M_Z) = 0.118$. The central renormalisation (μ_R) and factorisation (μ_F) scales are chosen to be the invariant mass of final state Drell-Yan pair, $\mu_F = \mu_R = m_{\ell_V}$. To estimate theoretical uncertainties, we adopt the 7-point scale variation of μ_F and μ_R by a factor of two while enforcing $1/2 \le \mu_F/\mu_R \le 2$.

We compare normalized differential observables computed from the central member of four sets of NNLO PDFs: NNPDF3.1 [62], NNPDF4.0 [63], CT18 [64] and PDF2LHC21 [65]. To describe the decay of the W boson into a charged lepton and a neutrino, we implement leading order decay matrix element with a Breit-Wigner parametrisation of the W propagator. We use $M_W = 80.379$ GeV and $\Gamma_W = 2.085$ GeV reported by the Particle Data Group (PDG, [12]) as the default setup. No fiducial selection criteria is applied on the final state leptons. Two types of Breit-Wigner parametrisation are applied in this work. The default setup adopts the fixed-width parametrisation

$$BW(q^2) = -\frac{i}{q^2 - M_W^2 + iM_W\Gamma_W},$$
(1)

while measurements of gauge-boson masses are usually determined with a running width parametrisation

$$BW(q^2) = -\frac{i}{q^2 - M_W^2 + iq^2\Gamma_W/M_W},$$
(2)

where q^2 is the invariant mass of final state Drell-Yan pair. We present comparisons of the default setup, running width (label 'running Γ_W ') and fixed width (label 'fixed Γ_W ') where M_W and Γ_W are transformed from on-shell to pole mass scheme according to [66].

3. Results

We illustrate the impact of four modern PDFs on the W boson rapidity and transverse mass distributions in Fig. 1 and 2. The rapidity distributions of the Drell-Yan pairs from W⁺ and W⁻ decays are normalized by the corresponding total cross section in Fig. 1. Fixed order contributions with up to N³LO accuracy are illustrated with NNPDF3.1 PDFs. NNLO predictions with three additional PDFs (CT18, NNPDF4.0 and PDF4LHC21) are included for comparison. The bottom panels shows their ratio with respect to the central NNLO result from NNPDF3.1. The coloured



Figure 1: W boson rapidity distributions with NLO to N^3LO QCD corrections. The NNLO corrections are calculated with four sets of PDFs. The coloured bands represent theory uncertainties from 7-point scale variation. The bottom panels show the ratio with respect to NNLO with NNPDF3.1 PDFs.



Figure 2: W boson transverse mass distribution with NLO to N^3LO QCD corrections. The NNLO corrections are calculated with four sets of PDFs. The coloured bands represent theory uncertainties from 7-point scale variation. The bottom panel is the ratio with respect to NNLO for NNPDF3.1 PDFs.

bands represent theory uncertainties from the 7-point scale variation and the error bars indicate the numerical integration error at N³LO. We observe a relatively large impact on the shape of distributions from the choice of PDFs, well outside scale variation bands. For W^+ , the central rapidity region displays about -1.5% (-0.7%) deviation between CT18 (PDF4LHC21) and NNPDF3.1 PDFs, which gradually increases to +2.7% (+1.4%) towards the forward region. The impact of different PDF choices is stronger for W^- . The central rapidity region shows about -2.3% (-1.1%) deviation between CT18 (PDF4LHC21) and NNPDF3.1 PDFs, which increases to +2.5% (+1.5%) towards the forward region. Higher order QCD corrections at NNLO and N³LO only provide small changes to the shape of rapidity distributions of less than $\pm 0.5\%$ throughout the plotted region. We notice that NNPDF3.1 and NNPDF4.0 PDFs predictions for the normalized distributions agree within $\pm 0.5\%$.



Figure 3: Normalized W transverse mass distribution with NLO to NNLO corrections (top panel), with different M_W values from PDG, CDFII and L3 (middle panel) and with different Γ_W with PDG central value and $\pm 1\sigma$ uncertainties (bottom panel). All distributions are compared to the NNLO result with running decay width and PDG central values. Positive (negative) charged current results are in the left (right) panels. The colored bands represent theory uncertainties from 7-point scale variation.

In Fig. 2 we present the normalized transverse mass distributions of charged current decay products. We observe similar higher order QCD corrections between W^+ and W^- both having the dominant change to the shape of distributions from NLO to NNLO with about +1.6% around 40 GeV and -1% around the M_W threshold. Different choices of PDFs are consistent within numerical error at NNLO accuracy through out the plotted transverse mass region. A small negative shift about -0.4% caused by CT18 and PDF4LHC21 with respect to NNPDF3.1 (also NNPDF4.0) PDFs appears at m_T^W around 100 GeV where NNLO predictions from all four PDFs are still consistent within scale uncertainty band. The N³LO QCD correction (in left panel of Fig. 2) agree well with NNLO predictions from various PDFs choices in the bulk of the distribution. It starts to have a minimum overlap in scale variation band from NNLO for m_T^W below 15 GeV.

We illustrate in Fig. 3 the impact of changes to the EW input parameters on the transverse mass distributions of charged current Drell-Yan production. Instead of the default setup, here we apply the Breit-Wigner parametrisation with running decay width described in eq. (2). Comparing the top panels of Fig. 3 to the bottom panels of Fig. 2, we find excellent agreement between the two Breit-Wigner parametrisations. We also confirm by comparing NNLO results between running Γ_W (in blue) and fixed Γ_W (in red) in the top-left panel of Fig. 3 that the two parametrisations can be transformed from one to the other according to [66]. In the middle panels of Fig. 3, we alter the M_W on-shell mass input value from the SM electroweak fit of $M_W = 80.379$ GeV to the measured results recently reported by CDFII at 80.433 GeV [10] and to the L3 result of 80.27 GeV [67]. The weak

mixing angle $\sin^2 \theta_W$ is a derived value in our calculation, which at tree-level is $(1 - (M_W/M_Z)^2)$. The comparison aims to quantify the relative impact of input M_W values larger or smaller than the SM electroweak fit benchmark at NNLO QCD accuracy. Below 60 GeV, the three chosen M_W input values yield mutually consistent results for the normalised transverse mass distribution. We observe a strong input parameter sensitivity at the peak of the distribution around M_W . Below the M_W threshold, the distribution for the CDFII value is about 0.5% smaller than the electroweak fit benchmark and is about 3.5% larger right beyond the threshold. This difference gradually reduce towards 100 GeV at about 0.7%. The largest deviation between the two distributions reaches about 14 times the scale variation uncertainty. We observe a large and negative shift beyond the threshold for the L3 input parameter, amounting to 7% which is about twice the difference obtained for the CDFII input parameter. In the bottom panels of Fig. 3, we alter the Γ_W decay width input value within the PDG uncertainty of ± 42 MeV. The impact to the normalised transverse mass distributions is minimal below 75 GeV and is stabilised at $\pm 2\%$ beyond the threshold compared to the benchmark distribution from the central PDG value. The resulting $\pm 2\%$ deviation corresponds to about $\pm 9 \sigma$ of the scale variation uncertainty. Fig. 3 also demonstrates that the differences between fixed-width and running-width schemes are minimal.

4. Conclusions

In this talk, we have presented predictions for normalised differential distributions in the charged current Drell-Yan production up to third order in perturbative QCD. We supplement our work in [20] to quantify the impact of PDF variations and electroweak input parameter schemes on the rapidity and transverse mass distributions in the charged current Drell-Yan process. We find nontrivial modifications to the shape of the normalised rapidity distributions at the level of $\pm 2.5\%$ in central and forward regions due to different choices of modern PDFs. Their impact is much larger than that of the N³LO QCD contributions. We compare transverse mass distributions with relative changes in the input EW parameters with both running and fixed width parametrisation. Excellent agreement is observed around and beyond the M_W threshold between the two parametrisations. The shape of the transverse mass distribution is very sensitive to the input values of M_W and Γ_W is largest, exceeding by far the uncertainty from missing higher order contributions on the theory predictions. Our findings provide the theory input to future precision measurements of SM parameters associated with charged-current Drell-Yan production.

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