Data mining of cosmic-ray anisotropy observed with the Global Muon Detector Network

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Ground-based muon detectors are sensitive to anisotropies of cosmic rays at approximately 50 GeV and have been operated with great stability for over 10 years. The anisotropy is controlled by the space environment in various time scales and is an attractive target of data-driven approaches. We report on unsupervised machine-learning of anisotropy data accumulated by the Global Muon Detector Network (GMDN). It is expected to provide a comprehensive and statistical picture of cosmic-ray anisotropies free from biases such as data selections relying on a visual inspection.

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1. Introduction

Cosmic-ray anisotropy is an essential and attractive subject of cosmic-ray physics, interplanetary physics, and heliospheric physics as it is a manifestation of cosmic-ray propagation processes in the space environment. Diverse scientific phenomena in various time scales, such as interplanetary shocks (IP-shocks) and cyclic variations of the heliosphere, are involved in cosmic-ray anisotropy. A comprehensive study covering these variations is necessary to establish a statistical picture and approach a universal mechanism or physics behind the anisotropy. However, most of the previous works focus on a special subject, such as IP-shocks or an 11-year cycle variation of the heliosphere, separately. Such an approach can overlook a scientific finding because the space environment is a complex system where multiple phenomena evolve in parallel. Additionally, typical IP-shock studies are mainly case studies on limited events arbitrarily selected, while a small number of studies challenge establishing a statistical picture of IP-shock events[1–3].

Data mining is expected to be a powerful approach for an inclusive survey of diverse phenomena in anisotropy on a mathematical basis. It will lead to a statistically reliable picture and a discovery of a new profile of cosmic-ray anisotropy. This approach is also expected to be useful for reducing dimensions of anisotropy. Its multidimensional quantities interacting with each other via phase-space dynamics[4] have caused difficulty in establishing a physical interpretation of variation of anisotropy.

Global Muon Detector Network (GMDN) started its operation with two-hemisphere detectors at Nagoya (Japan) and Hobart (Australia) in 1992. SãoMartinho da Serra (Brazil) and Kuwait detectors were installed in 2006. GMDN achieved its initial completion in 2016 by expanding the Kuwait detector to a comparable detection area (25 m$^2$) with the Nagoya detector (36 m$^2$).

This study attempts an inclusive survey of anisotropy for both long- and short-term variations, based on unsupervised machine-learning. Harmonic components of anisotropy derived from GMDN data[5] are used as sample data. Preliminary results demonstrate the advantages of our approach.

2. Preparation of datasets

Muon counting-rate can be modeled in terms of spherical harmonics, as[6]

$$I_{i,j}(t) \approx \sum_{n=0}^{2} \sum_{m=0}^{n} \left( e_{n,i,j}^{mc}(t) \left( c_{ni,j}^{m} \cos m\omega t - s_{ni,j}^{m} \sin m\omega t \right) + e_{n,i,j}^{ms}(t) \left( s_{ni,j}^{m} \cos m\omega t + c_{ni,j}^{m} \sin m\omega t \right) \right)$$

where $I_{i,j}$ denotes our observable, deviation [%] of counting-rate recorded in the $j$-th directional channel of the $i$-th detector. Zero-level to take the deviation is set at an average counting-rate in each Bartels rotation (27-days period). We use 13-17 channels compiled in each detector and total 60 channels in GMDN 4 stations. $e_{n,i,j}^{mc}$ and $e_{n,i,j}^{ms}$ are expansion coefficients of spherical harmonics in the order $(n, m)$, representing cosmic-ray anisotropy. $c_{ni,j}^{m}$ and $s_{ni,j}^{m}$ are coupling coefficients expressing a response of $I_{i,j}$ to the anisotropy. They are derived by numerically calculating the geomagnetic and atmospheric propagation of cosmic rays with a specific rigidity, and then integrating them for
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the rigidity. \( t \) is universal time and \( \omega \) is the angular velocity of Earth’s rotation. \( \omega t_i = \omega t + \phi_i \) where \( \phi_i \) is a geographic longitude of the \( i \)-th detector. Anisotropy components \( \xi_{mc}^n \) and \( \xi_{ms}^n \) are derived by fitting the model function into observed deviation \( I_{i,j} \). The best-fitting procedure, including corrections for atmospheric variations, is described in [6, 7] and practically used in previous works[3, 8–10]. One modification in this preliminary analysis from the precedents is the integration upper limit, set at 200 GV for \( n > 0 \) components based on estimation by [11].

We performed the best-fitting for 60-channels data recorded every hour by GMDN from 2015 to 2022 and obtained 9 parameters each time, as listed below.

- \( \xi_{0c}^0 \): Isotropic component of spherical harmonics representing the deviation of cosmic-ray density from average level.
- \( \xi_{1c}^0, \xi_{1c}^1, \) and \( \xi_{1s}^1 \): The 1st order harmonics, which represent uni-directional cosmic-ray flow and respectively correspond to \( z \)-, \( x \)- and \( y \)-components of the flow in this order.
- \( \xi_{2c}^0, \xi_{2c}^1, \xi_{2s}^1, \xi_{2c}^2, \) and \( \xi_{2s}^2 \): The 2nd order harmonics which represent bi-directional flow induced by spatial derivatives of the uni-directional flow and interplanetary magnetic field.

The best-fit parameters are obtained in the geocentric (GEO) coordinate system whose \( x \)-axis is fixed to 0 a.m. in local time (LT), and then transformed to the geocentric solar ecliptic (GSE) coordinate system. The available hours with a small number of inactive channels are 45132, therefore our dataset size is 9 parameters \( \times 45132 \) hours.

3. Methods and Results

3.1 Cluster analysis

We categorize the anisotropy data using unsupervised machine-learning. The anisotropy at each time derived in the previous section is expressed as a single point in the parameter space with 9 dimensions, corresponding to 9 components of the anisotropy. Each parameter in the dataset is standardized by the Z-score normalization for the whole period as a preprocessing. Then, 45132 points in the 9-dimensional space are grouped by the k-means clustering of Python scikit-learn library[12]. The number of clusters is set at 10, where the sum of squared errors of prediction is sufficiently decreased and the significant correlations with solar activity and IP-shocks discussed in the following sections appear. Each time in the dataset is provided with a cluster ID, 1, 2, 3,..., or 10, by this clustering. It is noted that the standardized parameters are restored to their original quantities after labeling the clusters, for scientific discussions in the following sections.

Figure 1 displays averages of the 0th- and 1st-order anisotropy components in the individual clusters. Standard errors of averages are not plotted because they are so small that it’s hard to see. Figure 1(a) shows averages of the 0th component, or density variation \( \xi_{0c}^0 \). Averages of the diurnal anisotropy, \( \xi_{1c}^1 \) and \( \xi_{1s}^1 \), are displayed in Figure 1(b1) which is a so-called harmonic dial, where the upward direction corresponds to 0 a.m. (midnight) direction in LT while the right side represents 6 a.m. (morning). It has to be noted that the LT expression is exact in the GEO coordinate system, but now it deviates slightly because we transformed the anisotropy components into the GSE coordinate system. Figure 1(b2) shows averages of north-south anisotropy, \( \xi_{1c}^1 \), along with
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Figure 1: Averages of the 0th- and 1st-order anisotropy components in the clusters grouped by k-means clustering. (a) Average density deviation $\xi_{0c}$ in each cluster from average level. (b1) Average vector of diurnal anisotropy ($\xi_{1c}$ and $\xi_{1s}$) in each cluster, presented in a harmonic dial. (b2) Average of north-south anisotropy, $\xi_{1c}$, in each cluster presented in a vector diagram with $\xi_{1c}$.

$\xi_{1c}$ in a vector diagram. Averages of the 2nd-order anisotropy ($\xi_{0c}$, $\xi_{1c}$, $\xi_{1s}$, $\xi_{2c}$, and $\xi_{2s}$) are displayed by intensity maps on spheres in Figure 2, because it cannot be expressed by a simple 2D or 3D vector.

The clusters 1, 3, 4, and 5 have enhanced deviations of density from the average level ($\xi_{0c} = 0$) in common. They also have relatively enhanced 1st-order (diurnal or north-south) and 2nd-order anisotropies. However, the polarities or directions of the enhancements are different from each other, possibly causing the grouping into different clusters. Clusters 7, 8, 9, and 10 have moderate or small magnitudes of the density deviation and 2nd-order anisotropy, but have comparable amplitudes of the 1st-order anisotropy with the clusters mentioned above (1, 3, 4, and 5). Remained clusters, 2 and 6, have negligible density deviations, but cluster 6 has a characteristic direction of the diurnal anisotropy while the 1st-order anisotropy of cluster 2 has a negligible amplitude.

Most of the average diurnal anisotropies of the clusters point in the range between 0 p.m. and 3 p.m. in Figure 1(b1), earlier LTs than ~6 p.m. expected by the picture of the diffusion-convection balance. This phase shift is known as a common feature in a period with the positive polarity of the solar dipole magnetic field[13] as it is in our analysis period (2015-2022).

3.2 Long-term variation of occurrence rates of clusters

The number of hours labeled with each cluster is counted in each year and then transformed into a yearly occurrence rate of the cluster by dividing it by the total active hours in the year. As shown in
Figure 2: Average intensity maps of the 2nd anisotropy composed of $\xi_0 c^2$, $\xi_1 c^2$, $\xi_1 s^2$, $\xi_2 c^2$, and $\xi_2 s^2$ for individual clusters. Horizontal axes are GSE longitudes, and vertical axes are GSE latitudes.

Figure 3 we can find clear solar-activity dependences of the occurrence rates. The occurrence rates of clusters 3, 4, and 7 are high near the solar activity maximum (just before 2015) and then decrease to their minimum around the solar activity minimum (2019-2020). Contrarily, clusters 2, 6, and 9 have low occurrence rates near the solar maximum and increase up to the solar minimum. Cluster 1 may also have a similar trend with relatively small significance. The anisotropy vector simply averaged over time is proved to have its amplitude positively correlating with solar activity[13]. Our result is consistent with it overall, except for cluster 9 which has a relatively large amplitude of the 1st-order anisotropy while negatively correlating occurrence rate with solar activity.

It is also notable that clusters 1 and 3 have significant 2nd-order anisotropy with losses along the Parker spiral (9 a.m. and 9 p.m.), while clusters 4 and 5 have opposite-sense 2nd-order anisotropy with excesses along the Parker spiral as shown in Figure 2. The former pattern is proven as a dominant anisotropy arising from the geometry of the interplanetary magnetic field[4]. The latter pattern has been rarely reported, especially in terms of the long-term variation, but Figure 3 presents
Figure 3: Yearly occurrence rate of each cluster. Horizontal dashed lines denote average occurrence rates in the whole analyzed period (2015-2022).

these clusters exist with substantial occurrence rates. These aspects may indicate unrevealed mechanisms of cosmic-ray propagation.

Long-term variation of the heliosphere, or space climate, contains complex phenomena such as coronal mass ejections, coronal holes, corotating interaction regions, heliospheric current sheet, and sector structure. Investigating correlations of individual clusters with such phenomena may lead to a new finding overlooked in previous works based on a simple mean of anisotropy.

3.3 Occurrence rates of clusters around IP-shocks

Using an IP-shock list from CFA Interplanetary Shock Database[14], we investigate the temporal variation of the cluster occurrence rates before and after a shock arrival. 81 shock events are identified in Wind spacecraft data in our analysis period (2015-2022). Yearly numbers of the events are 25, 6, 12, 10, 9, 4, and 15 respectively in 2015, 2016, 2017, 2018, 2019, 2020, and 2021. The event number is roughly high around the solar maximum but does not necessarily vary with the sunspot number.

We extract anisotropy data with cluster ID in each period of several days centered on a shock arrival at the Wind spacecraft. Timestamps of the data are re-assigned by hours relative to the shock arrivals with polarities negative before shock arrivals and positive after them. Then the cluster data are summed up for every 6 hours before and after shock arrivals. A cluster occurrence rate every 6 hours for all 81 events is calculated. The number of hours accumulated in each 6-hour bin is ~400.
Figure 4 displays the occurrence rate for each cluster as a function of relative time to shock arrivals at the Wind spacecraft. Horizontal dashed lines are the average occurrence rates in the whole analyzed period (2015-2022) as well as Figure 4. It is notable that cluster 10 significantly enhances its occurrence rate, succeeding for ~1 day from just before shock arrivals. The occurrence rate of cluster 4 also increases from shock arrivals and keeps its enhancement over a few days. These 2 clusters, especially cluster 4, feature density depletions as shown in Figure 1(a). These enhancements are expected to represent Forbush decreases generally observed in IP-shock events. Cluster 4 is also accompanied by significant excesses along the Parker spiral (9 a.m. and 9 p.m.), as shown in Figure 2. An enhanced bi-directional flow along a magnetic field inside a coronal mass ejection is reported by [15]. Our result implies that such a bi-directional flow appears more frequently than expected. Cluster 4 also features the largest enhancement of the 1st-order anisotropy.

3.4 Conclusion

We demonstrated a data-mining approach for the study of cosmic-ray anisotropy. The k-means clustering reduces 9 components of anisotropy into one of 10 cluster labels each time, allowing us to survey and discover a statistical feature of anisotropy. The temporal evolution of the cluster label shows close correlations with solar activities and IP-shock events. Our preliminary results present multiple findings, such as the 2nd-order anisotropy pattern which was unproven but substantially...
exists, and statistical occurrence rates of anisotropy enhancements around IP-shocks. These results encourage further surveys for unrevealed mechanisms of cosmic-ray propagation which appears in anisotropy.

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