

## Very high energy afterglow of binary neutron star mergers

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The joint detection of GW170817 and a short gamma-ray burst (GRB) has provided the first direct evidence that binary neutron star (BNS) merger produces GRB. Recently and unprecedentedly, very-high-energy (0.1–10 TeV) afterglow emission were reported from a few GRBs (e.g. MAGIC, H.E.S.S. and LHAASO observations), suggesting the prospects of multi-messenger detection of gravitational-wave counterparts with the next-generation gamma-ray detectors. We study GW-TeV joint detectability of BNS merger using a population model prescribing the distribution of common parameters (e.g. energetics, viewing angle) in both gravitational-wave and very-high-energy afterglow emission. We report the expected distributions of observables (distances, orientations, energetics and ambient densities) for detectable events and the joint GW-TeV detection rate for the CTA project.

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## 1. Introduction

The joint detection of the BNS merger GW170817 and a short gamma-ray burst (GRB) 170817A demonstrated the promise to identify and interpret high energy counterparts of gravitational-wave (GW) sources. GRBs have been observed to emit radiation beyond GeV energies with no clear cutoff [1], including short GRBs such as GRB 090510 [2, 3]. Recently, gamma-ray emission up to very-high-energy (VHE,  $> 0.1$  TeV) range has been discovered from several GRBs: 190114C and 160821B [4–6] by the MAGIC Telescope, 180720B and 190829A by H.E.S.S. [7, 8]. The VHE emission has been modeled with a synchrotron self-Compton (SSC) origin in forward shock afterglow [e.g., 9–11], while synchrotron or external IC origin are also suggested [e.g., 8, 12]. VHE search was performed for the GW170817 event starting 5 hours post-merger [13, 14] but no significant emission was found, which is likely due to the significant off-axis observation ( $\gtrsim 20^\circ$ ).

The prospects of GW follow-up observations with CTA has been explored in the literature, mainly by using the phenomenological extension of the high energy spectra of short GRBs [e.g., 15–18]. Therefore, considerations such as SSC component, off-axis observation (as in GW170817) are not discussed in detail by previous studies. In this proceeding paper, we will present a quantitatively modeling of CTA's GW follow-up detectability of VHE afterglow from BNS merger, taking into account the SSC emission component and off-axis observation.

## 2. Model

### 2.1 GW sensitivity model

The reach of GW interferometer is characterized by its horizon distance  $D_{\text{GW}}$  with  $D_{\text{GW}}^2 \equiv \mathcal{M}^{5/3} S_I$ , where  $\mathcal{M}$  is the chirp mass of the binary,  $S_I$  is a quantity solely depending on the sensitivity profile of the interferometer [19]. It is defined such that the signal from an optimally-located and oriented BNS at  $D_{\text{GW}}$  can produce a signal-to-noise ratio (SNR) of 8 by ideal matched filtering in the detector's data stream, corresponding to a  $5\sigma$  detection. The general SNR of a GW signal can be written as

$$\rho^2(d_L, \theta, \phi, \psi, \iota) = \rho_0^2 \frac{D_{\text{GW}}^2}{d_L^2} \Theta^2(\theta, \phi, \psi, \iota), \quad (1)$$

where  $d_L$  is the luminosity distance to the binary,  $\Theta^2$  represents the angular response pattern to the sky location of the source ( $\theta, \phi$ , inclinations  $\iota$ , polarization angles  $\psi$  relative to the detector) combining the antenna patterns with a global maximum of unity corresponding to an optimally positioned and oriented source. The explicit functional form of  $\Theta$  are given in [20]. We could define the GW visibility distance  $d_{\text{GW}}$  as

$$d_{\text{GW}} \equiv D_{\text{GW}} \Theta \quad (2)$$

$$D_{\text{GW}} = \max_{\theta, \phi, \psi, \iota} d_{\text{GW}}. \quad (3)$$

The detection criteria is then written as

$$d_L < d_{\text{GW}}. \quad (4)$$

## 2.2 VHE sensitivity model

The onset of VHE emission is expected to follow shortly ( $\sim 1$  s) after the gravitational waves from a BNS merger, but usually there is a delay time before the start of follow-up observations. Given the delay time  $t_{\text{delay}}$ , we determine a detection by CTA by the following criteria resembling the instrument exposure:

$$\langle \mathcal{F}|_{\text{jet}} \rangle \equiv \frac{1}{t_{\text{exp}}} \int_{t_{\text{delay}}}^{t_{\text{delay}}+t_{\text{exp}}} \mathcal{F}|_{\text{jet}} dt > \mathcal{F}|_{\text{CTA}}(t_{\text{exp}}) \quad (5)$$

where  $\mathcal{F}|_{\text{jet}} = \mathcal{L}|_{\text{jet}}/(4\pi d_L^2)$  is energy flux spectrum from a Gaussian jet afterglow,  $\mathcal{F}|_{\text{CTA}}$  is the CTA  $5\sigma$  differential sensitivity in the 0.1 – 10 TeV energy band. The CTA sensitivities are computed by the public Python package `ctool`<sup>1</sup> for an exposure time of  $t_{\text{exp}}$ . For compatibility with GW sensitivity model, we could similarly define the VHE visibility distance  $d$  as

$$d_{\text{EM}} \equiv \sqrt{\frac{\mathcal{L}|_{\text{jet}}}{4\pi \mathcal{F}|_{\text{CTA}}}} \quad (6)$$

$$D_{\text{EM}} \equiv \max_X d_{\text{EM}}, \quad (7)$$

where  $D_{\text{EM}}$  is the marginally detectable distance with optimized parameter  $X$  of the burst. The detection criteria then becomes

$$d_L < d_{\text{EM}}. \quad (8)$$

## 2.3 Joint detectability model

The GW-VHE joint detection rate of BNS events is estimated by the following equation:

$$\mathcal{R}_{\text{joint}} = \int_0^\infty P_{\text{joint}}(d_L) \frac{\mathcal{R}_{\text{BNS}}(z)}{1+z} \frac{dV}{dz} dz. \quad (9)$$

Here  $P_{\text{joint}}$  is the *averaged* detection probability for a source located at luminosity distance  $d_L(z)$ , i.e., the detectable fraction of a BNS population sampled from the assumed parameter space  $X$ . We define the joint GW-EM visibility distance as:

$$d_{\text{joint}} \equiv \min(d_{\text{GW}}, d_{\text{EM}}) \quad (10)$$

$$D_{\text{joint}} \equiv \max_X d_{\text{joint}}. \quad (11)$$

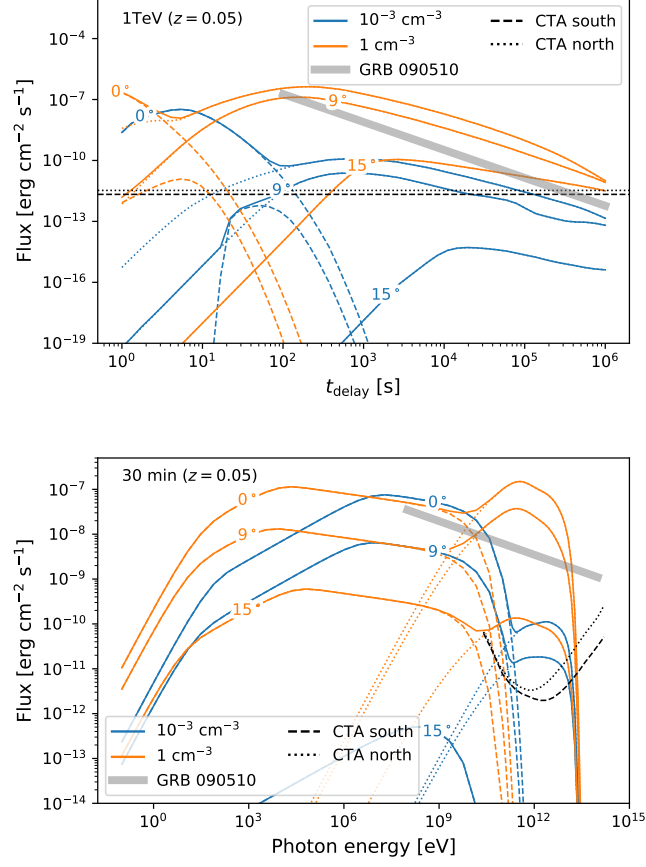
and we use a joint GW-EM detection criteria as:

$$d_L < d_{\text{joint}}. \quad (12)$$

Then the detectable probability is given by

$$P_{\text{joint}}(d_L) = \int_{d_L^2 < d_{\text{joint}}^2} dX. \quad (13)$$

<sup>1</sup><http://cta.irap.omp.eu/ctools/>



**Figure 1:** TeV light curves and multi-wavelength spectra from a simulated BNS merger event at  $z = 0.05$ , for various viewing angles and medium density. Contributions by synchrotron and SSC are indicated in dashed and dotted lines, respectively.  $5\sigma$  sensitivities of CTA sites are compared assuming 30 min exposure and  $20^\circ$  zenith. The spectral extension of GRB 090510 is shown for comparison [2].

And the joint detection rate (ignoring cosmological evolution of BNS merger rate) is given by

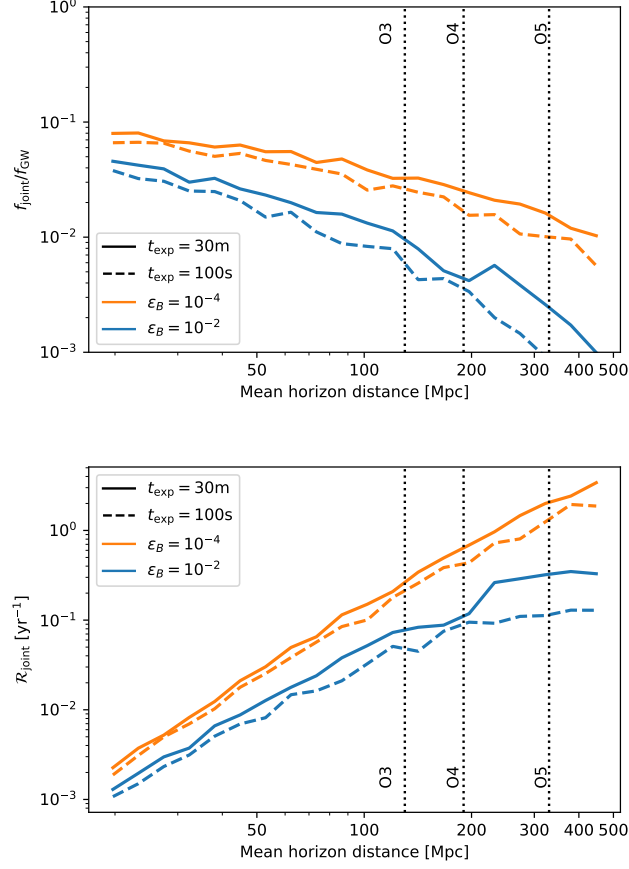
$$\mathcal{R}_{\text{joint}} \approx \frac{4\pi}{3} \mathcal{R}_{\text{BNS}} \langle d_{\text{joint}}^3 \rangle_X. \quad (14)$$

The fraction of GW events also detectable by follow-up EM observation can be found by:

$$\frac{f_{\text{joint}}}{f_{\text{GW}}} = \frac{\langle d_{\text{joint}}^3 \rangle_X}{\langle d_{\text{GW}}^3 \rangle_X}. \quad (15)$$

One can derive the distributions of the observables  $x$  in the jointly-detected population with prior distribution  $\mathcal{P}_x$ :

$$\mathcal{P}_x|_{\text{joint}} \equiv \frac{1}{\mathcal{R}_{\text{joint}}} \frac{d\mathcal{R}_{\text{joint}}}{dx} = \mathcal{P}_x \frac{\langle d_{\text{joint}}^3 \rangle_{X/x}}{\langle d_{\text{joint}}^3 \rangle_X}. \quad (16)$$



**Figure 2:** Upper: Jointly-detectable fraction within the GW detector reach. Lower: annual joint detection number versus GW detector reach. Local BNS merger rate of  $320 \text{ Gpc}^{-3} \text{ yr}^{-1}$  is assumed [21].

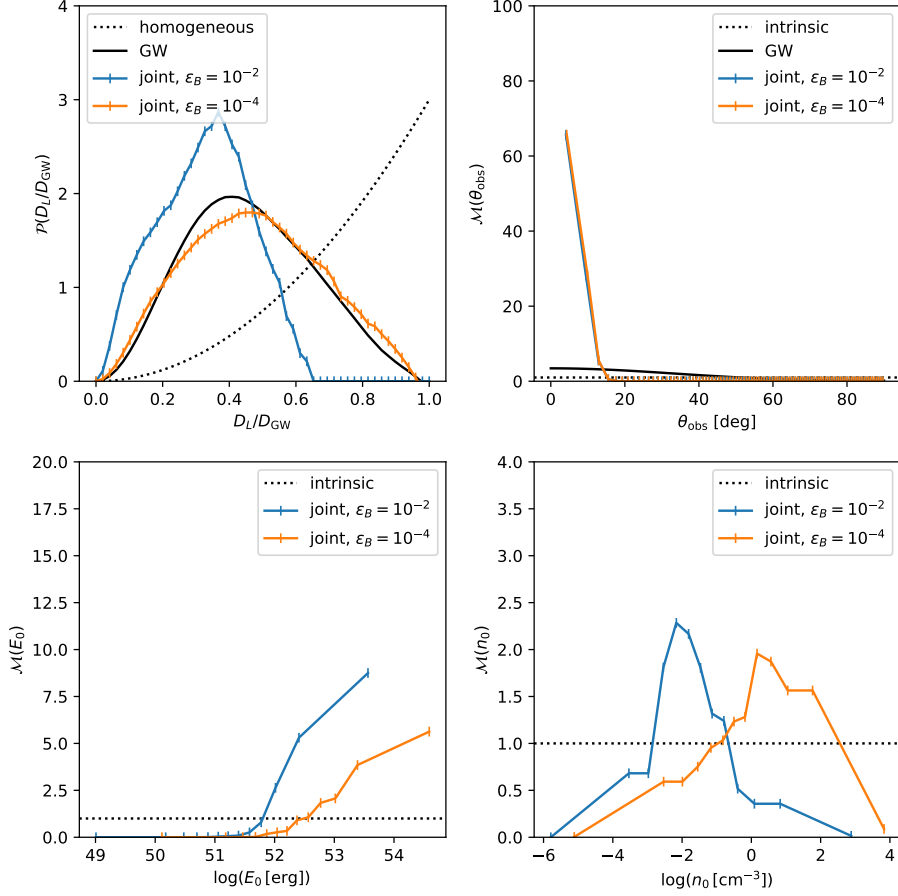
Here  $\langle \rangle_{X/x}$  is the integral average over parameter set  $X$  but leaving out  $x$  as variable. We could use the function  $\mathcal{M}_x$  defined as

$$\mathcal{M}_x \equiv \frac{\mathcal{P}_x|_{\text{joint}}}{\mathcal{P}_x} = \frac{\langle d_{\text{joint}}^3 \rangle_{X/x}}{\langle d_{\text{joint}}^3 \rangle_X} \quad (17)$$

to indicate how the distribution  $\mathcal{P}_x$  has changed under the GW-VHE joint observational bias.

### 3. Result and discussion

We use the Monte Carlo approach to evaluate GW-VHE joint detectability, by generating a large population ( $> 10^5$ ) of BNS merger afterglow. Each event is defined by its random parameters, including short GRB parameters  $X_{\text{sGRB}} = E_0, \Gamma_0, \theta_j, n_0, \epsilon_e, \epsilon_B, p$  drawn from the distributions given by a decade of short GRB observations [22] and inclination parameters  $X_{\text{incl}} = \theta, \phi, \iota, \psi$  drawn from uniform distribution. Note that the shock electron and magnetic field parameters  $\epsilon_e = 0.1$  and  $\epsilon_B = 0.01$  are fixed in [22] due to their degeneracy with burst energy  $E_0$  and density  $n_0$  when



**Figure 3:** Upper left panel shows the luminosity distance distribution. **Other** panels show the observational bias indicator for viewing angle (upper right), isotropic energy (lower left) and CBM density (lower right) respectively, defined in (17) as the ratio of observed distribution  $\mathcal{P}|_{\text{joint}}$  to intrinsic distribution  $\mathcal{P}$ . Observational assumptions are 15-min delay and 30-min exposure.

reproducing the same synchrotron afterglow data, but they indicated that when choosing a value as low as  $\epsilon_B = 10^{-4}$ , the median of fitted  $E_0$  and  $n_0$  both increase by a factor of  $\approx 10$  compared to the  $\epsilon_B = 0.01$  assumption. With such distribution, we tend to estimate a much brighter SSC component from the population, as the ratio of SSC to synchrotron luminosity scales with  $\epsilon_e/\epsilon_B$  [23]. Therefore, we additionally study an alternative BNS population with a choice of  $\epsilon_B = 10^{-4}$  by manually scaling up  $E_0$  and  $n_0$  distribution by a factor of 10.

In Figure 1 we demonstrate TeV light curves and spectra powered by a Gaussian jet, taking into account attenuation by EBL absorption, compared with the extrapolated template of short GRB 090510 [2] that has been frequently used in previous CTA studies [e.g., 15–18]. We show two ambient densities are shown for typical values in old stellar populations ( $n = 10^{-3} \text{ cm}^{-3}$ ) and in star forming regions ( $n = 1 \text{ cm}^{-3}$ ), respectively.

In Figure 2, we estimate the follow-up detectable fraction and the annual detection rate as a function of GW sensitivity (horizon distance). We find  $f_{\text{joint}}/f_{\text{GW}} \lesssim 1\%$  for current and future sensitivities, and we estimate the joint detection rate by LIGO-CTA to be  $\sim 0.1 - 2$  per year. This is

an optimistic estimate since we do not take into account the duty cycle of the instruments. Assuming a fiducial duty cycle of 15% for CTA yields a smaller detection rate of  $\sim 0.015 - 0.3$  per year.

In Figure 3, we show the probability density distribution of luminosity distance  $d_L$  to the sources, as well as the observational bias indicator  $M_x$  for viewing angle  $\theta_{\text{obs}}$ , isotropic equivalent energy of the jet center  $E_0$  and circumburst medium density  $n_0$  defined in (17).

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