

1 Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

2 **Roberta Volpe on behalf of the Belle II Collaboration^{a,*}**

3 ^aPerugia University and INFN,

4 Via Pascoli, 06123 Perugia, Italy

5 E-mail: roberta.volpe@pg.infn.it

We use a 362 fb^{-1} sample of e^+e^- collisions at $\Upsilon(4S)$ resonance collected with Belle II detector at SuperKEKB collider to search for the rare decay $B^+ \rightarrow K^+ \nu \bar{\nu}$. The main strategy consists in exploiting the inclusive properties of the other B to suppress the background. Another analysis is based on a conventional hadronic reconstruction of the accompanying B meson and is used to corroborate the first strategy. Both the procedures have been validated with several control samples. A maximum likelihood fit is used to extract the branching ratio, which results in $[2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})] \times 10^{-5}$ for the main analysis and $[1.1_{-0.8}^{+0.9}(\text{stat})_{-0.5}^{+0.8}(\text{syst})] \times 10^{-5}$ for the support analysis. The combination of the two analyses gives a branching fraction of $[2.3 \pm 0.5(\text{stat})_{-0.4}^{+0.5}(\text{syst})] \times 10^{-5}$ which corresponds to the first evidence of the decay with 3.5 standard deviations and 2.7 standard deviations above the standard model expectation.

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*Speaker

7 1. Introduction

8 The decay $B^+ \rightarrow K^+ \nu \bar{\nu}$ occurs through the flavor-changing neutral current transition $b \rightarrow$
 9 $s \nu \bar{\nu}$. That is suppressed in the Standard Model (SM) because of the Glashow–Iliopoulos–Maiani
 10 mechanism, which makes it a rare process. The dominating contributions to the decay are the
 Feynman diagrams shown in figure 1

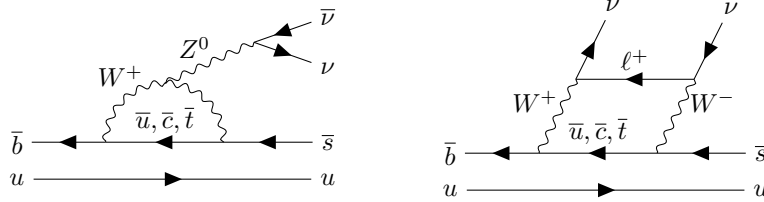


Figure 1: Dominating Feynman diagrams contributing to the $b \rightarrow s \nu \bar{\nu}$ transition.

11
 12 The SM prediction for the branching fraction is $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (5.58 \pm 0.37) \times 10^{-6}$ [1].
 13 The good theoretical precision, due to small hadronic uncertainties, makes this process an ideal
 14 environment to search for new physics. Indeed the branching fraction can be enhanced in models that
 15 predict high mass non-SM particles, as Leptoquarks [2]. Furthermore, new low-mass undetectable
 16 exotic particles (dark matter candidates or mediators of a dark sector) could be produced together
 17 with the kaon giving rise to a two-body or three-body decay with missing energy [3] [4]. Before the
 18 analysis described in this document, no evidence for a signal has been found and the experimental
 19 upper limit on the branching fraction was 1.6×10^{-5} at 90% of confidence level (CL) [5]. The main
 20 challenge for this search is the presence of two neutrinos, which precludes the full reconstruction
 21 of the event. In this work the signal B meson is produced in the $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^+B^-$ process
 22 and the accompanying B is used to obtain information on the event kinematics. Two analysis
 23 strategies have been exploited, the most performant one is the inclusive tagging analysis method
 24 (ITA), exploiting inclusive properties from the B -meson pair-produced along with the signal B
 25 and representing the main analysis. A support analysis, employing the well-established hadronic
 26 tagging analysis method (HTA), has been used as well. Both the strategies have been applied to
 27 the full dataset of e^+e^- collisions produced from 2019 to 2022 by the SuperKEKB collider [6] and
 28 collected by the Belle II experiment [7]. Data produced with a center-of-mass (c.m.) energy equal
 29 to the mass of the $Y(4S)$, on-resonance data, correspond to an integrated luminosity of 362 fb^{-1} .
 30 The Belle II detector is made of several sub-detectors arranged in a cylindrical structure, surrounded
 31 by a superconducting solenoid providing a 1.5 T magnetic field parallel to the cylindrical main axis.
 32 Starting from the inside, the tracking system is composed of: a silicon pixel detector, a double
 33 sided silicon strip detector, a central drift chamber (CDC). A time-of-propagation counter and an
 34 aerogel ring-imaging Cherenkov counter provide the identification of charged particles (PID) and
 35 an electromagnetic calorimeter (ECL) reconstruct photons and other neutral particles. In the flux
 36 return of the solenoid a system to identify muons and K_L mesons is installed. A detailed description
 37 of the $B^+ \rightarrow K^+ \nu \bar{\nu}$ analysis can be found in [8], this document summarizes the main features. A
 38 brief description of the reconstruction of the event is given in section 2, the background suppression
 39 approach is described in section 3 and the validation of efficiency and background estimation is
 40 summarized in 4. The signal extraction settings and results are given in sections 5 and 6 respectively.

41 2. Event reconstruction and basic selection

42 The trigger selection, based on number of tracks in the CDC or energy deposits in the ECL,
43 has an efficiency close to 100%. The two analysis strategies differ for the tagging method, while
44 the particle reconstruction is kept as similar as possible, the event reconstruction for the two is
45 summarized in the following.

46 For the ITA, the event reconstruction starts with the reconstruction of charged and neutral particles.
47 The charged particles are required to have a transverse momentum $p_T > 0.1$ GeV, to be within the
48 CDC acceptance and (for the ones not coming from a K_S candidate) to be close to the interaction
49 point, by requiring minimum longitudinal and transverse distances (impact parameters) from the
50 average interaction point of $|d_z| < 3.0$ cm and $d_r < 0.5$ cm, respectively. The K_S candidates
51 are reconstructed starting from two opposite sign tracks compatible to be pions originating from a
52 common vertex. The ECL deposits with $E > 0.1$ GeV, in the CDC acceptance and not matched
53 with tracks are considered as photons. In order to reject misreconstructed particles and cosmic
54 muons, each particle is required to have an energy $E < 5.5$ GeV. Particle identification likelihoods,
55 based on PID detectors and other detector information, are employed to identify the charged kaons.
56 The chosen requirement gives a 68% of efficiency for signal kaons and 1.2% of probability to
57 identify a pion as a kaon. Conditions are imposed on the event as follows. The total momentum
58 of all reconstructed particles is used to compute the missing momentum as its complement and
59 the polar angle of the missing momentum, θ , must be $17^\circ < \theta < 160^\circ$. The number of tracks in
60 the event, N_{trk} , is required to be $4 < N_{trk} < 10$, to reduce high multiplicity and low multiplicity
61 background contributions and the total energy of the event is required to be $E > 4$ GeV. One of the
62 most important quantity to select the signal kaon in an event is the mass squared of the neutrino
63 pair, which, in the ITA is computed as: $q_{rec}^2 = s^2 + M_K^2 - \sqrt{s}E_K^*$ where M_K is the known mass of
64 K^+ mesons and E_K^* is the reconstructed energy of the kaon in the c.m. system, assuming the signal
65 B at rest in the c.m. frame. The candidate with the lowest q_{rec}^2 is chosen. The Rest of the Event
66 (ROE) is composed of all the charged particles, photons and K_S not associated to the signal kaon.
67 The HTA starts with the reconstruction of a B meson (B_{tag}), through the Full Event Interpretation
68 (FEI) [9]. Requirements on the output of the FEI are used to reduce the background. In addition the
69 B_{tag} and signal kaon are required to have opposite charges and events with $N_{trk} > 12$ are rejected.
70 The kaon identification and the restrictions on missing momentum are the same as in the ITA. The
71 number of tracks, coming from the impact point and with at least 20 hits in the CDC, not associated
72 with the B_{tag} nor with the signal kaon, is required to be zero, all the other tracks are named *extra*
73 *tracks*. The photons not associated with B_{tag} nor with the signal kaon are named extra photons.
74 Moreover events are rejected if a K_S^0 -meson, π^0 -meson, or Λ -baryon candidate is reconstructed
75 from the extra tracks and photons.

76 For both the strategies, control samples from data are used to test the simulation of the detector
77 response and, when a difference with respect to data is found, correction factors are introduced with
78 corresponding systematic uncertainties. Here only the most important ones are mentioned. The
79 photon energy is corrected, moreover an additional correction is needed due to a contribution of
80 clusters mimicking photons but arising from neutral hadrons, charged hadrons and beam background
81 particles. For the ITA a multiplicative hadronic energy correction is inferred empirically using data,
82 while for the HTA a correction to the number of the selected extra photons is applied. The probability

83 to have incorrect identification of charged particles is different in data and MC. Correction factors
 84 and their uncertainties are applied to the simulation as functions of the particle's charge, momentum,
 85 and polar angle. The K_L^0 are reconstructed using only the ECL and the modeling of its response is
 86 studied by using $e^+ e^- \rightarrow \phi(\rightarrow K_L^0 K_S^0) \gamma$ events. The outcome is that the simulation overestimates
 87 the efficiency by 17% in the ITA. Corrections are applied to the ITA and a corresponding systematic
 88 uncertainty of 100% is applied both for the ITA and the HTA.

89 3. Background suppression

90 Boosted Decision Tree (BDT) algorithms are built with several input variables: general event-
 91 shape variables, variables characterizing the kaon candidate, the kinematic properties of the ROE
 92 (for the ITA) and extra tracks and extra photons (for the HTA), the B_{tag} variables for the HTA.
 93 Furthermore for kaons that are identified as coming from D_0 and D^+ meson decays, variables
 94 describing the fit quality and kinematic properties of the resulting candidates are also included. The
 95 ITA uses a first BDT (BDT_1) as an event filter and a second classifier (BDT_2) for the final event
 96 selection. The most discriminant input variable of BDT_2 is the cosine of the angle between the
 97 momentum of the signal-kaon candidate and the thrust axis of the ROE computed in the c.m. frame.
 98 The HTA uses a single classifier, $BDTh$, and for it the most discriminant variable is the sum of
 99 extra-photon energy deposits in ECL, named E_{extra} . The multivariate classifiers are trained with
 100 simulated samples for signal and background. The output of the BDT_2 for the ITA and $BDTh$ for
 101 the HTA, are mapped into variables whose distributions are uniform for simulated signal events:
 102 $\eta(BDT_2)$ and $\eta(BDTh)$ respectively. For the ITA the selections $BDT_1 > 0.9$ and $\eta(BDT_2) > 0.92$
 103 define the signal region, which is further split in 3×4 bins of $\eta(BDT_2)$ and q_{rec}^2 . For the HTA
 104 the signal region is defined as $\eta(BDTh) > 0.4$ and is divided in 6 bins in $\eta(BDTh)$. After the full
 105 selection, for the ITA the signal efficiency is 8% with an expected purity of 0.8%, while for the
 106 HTA the signal efficiency is 0.4% with an expected purity of 3.7%.

107 4. Validation of the analysis

108 The optimization of the strategy and the training of the multivariate classifiers have been
 109 performed using simulated samples of signal and background. The modeling of the signal efficiency
 110 and the background estimation have been thoroughly validated using control samples data. When
 111 needed, corrections are applied and further validated. In this document only a few examples of
 112 validation approaches are given and only for the ITA. Similar methods have been used for the HTA
 113 validation.

114 4.1 Signal efficiency validation in the ITA

115 The agreement of the signal efficiency in data and simulation is validated with a sample selected
 116 as $B^+ \rightarrow K^+ J/\psi(\rightarrow \mu^+ \mu^-)$. For each event the muon pair is disregarded and the kaon is replaced
 117 by the kaon simulated in the signal events, to reflect the three-body topology of the signal signature.
 118 This signal-embedding procedure is performed for both data and $B^+ \rightarrow K^+ J/\psi$ simulation. Figure
 119 2 summarizes the results in the distributions of BDT_1 and BDT_2 . Good agreement is observed both
 120 before and after the signal embedding, resulting in a ratio of the efficiencies in data and simulation

121 of 1.00 ± 0.03 . The validation of the kaon identification is computed separately and is described in
 122 [8].

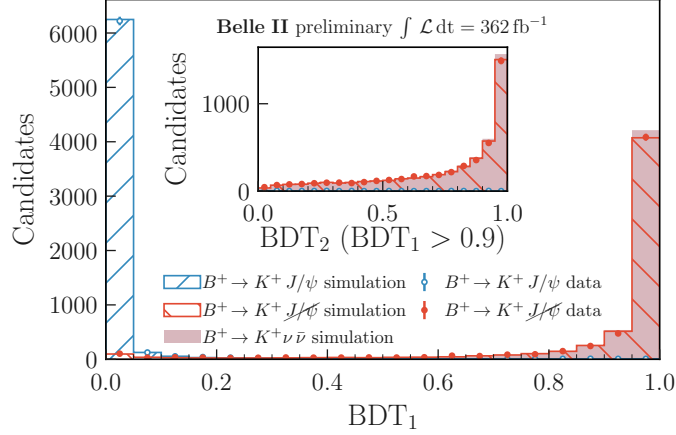


Figure 2: Distribution of the classifier output BDT_1 and BDT_2 for $BDT_1 > 0.9$. The simulation histograms are scaled to the total number of $B^+ \rightarrow K^+ J/\psi$ events selected in the data.

122

123 4.2 Background estimation and its validation in the ITA

124 For the ITA the background is composed of continuum events $q\bar{q}$ for the 40% and B -meson
 125 decay events for the 60%. The modeling of $q\bar{q}$ contribution is validated using the off-resonance
 126 data, which is a sample obtained with e^+e^- collisions at a c.m. energy 60 MeV below the mass
 127 of the $Y(4S)$. The moderate disagreement in shape is corrected with the procedure described in
 128 [10]. Among the B -meson decay contributions, the charged B^+B^- are the most important ones and
 129 can be separated in: (i) B -mesons hadronic decays involving D mesons and a kaon (38%); (ii)
 130 other hadronic B decays (14%); (iii) semi-leptonic B decays to charm-mesons that decay in turn to
 131 kaons (47%); (iv) leptonic decays (1%). Processes involving K_L mesons are particularly relevant
 132 because they are poorly known, in addition the detector response can be mis-modeled and K_L can
 133 fake missing energy. The decays of the kind $B \rightarrow D \rightarrow K_L^0 X$ are evaluated by using a control
 134 sample selected with a pion identification instead of the kaon identification. An excess of data
 135 over simulation is found and in order to evaluate it, the sample is separated in three contributions:
 136 the B decays involving $B \rightarrow D \rightarrow K_L^0 X$ decays, all the other B decays and the $q\bar{q}$. A fit to the
 137 q_{rec}^2 distribution is performed with the three fractions of the contributions as parameters and the
 138 estimated normalization factor for $B \rightarrow D \rightarrow K_L^0 X$ is found to be an increase in rate of $(30 \pm 2)\%$.
 139 Figure 3 (left) shows the post-fit data/simulation comparison for the q_{rec}^2 distribution. Applying
 140 the same normalization factor to other variables, a good agreement is found, in particular for the
 141 other main variable of the analysis $\eta(BDT_2)$, shown in 3(right).

142 The charmless hadronic B decays with K_L^0 mesons are scrutinised as well. Three-body $B^+ \rightarrow$
 143 $K^+ K_L^0 K_L^0$ decays are modeled using Dalitz spectra of $B^+ \rightarrow K^+ K_S^0 K_S^0$ decays measured by BaBar
 144 [11] and assuming equal probabilities for the two decays. The sPlot technique is applied to
 145 determine the distribution of the invariant $K_S^0 K_S^0$ mass after the background subtraction. The
 146 good data/simulation agreement is visible in figure 4 (left). Similar strategies are used to estimate

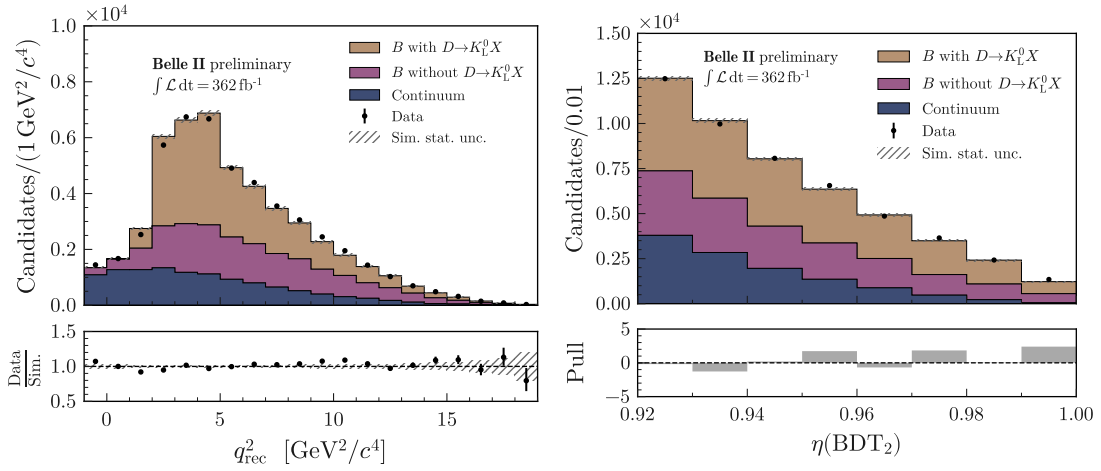


Figure 3: Post-fit data and simulation distributions of the pion enriched sample for q_{rec}^2 (left) and $\eta(BDT_2)$ (right).

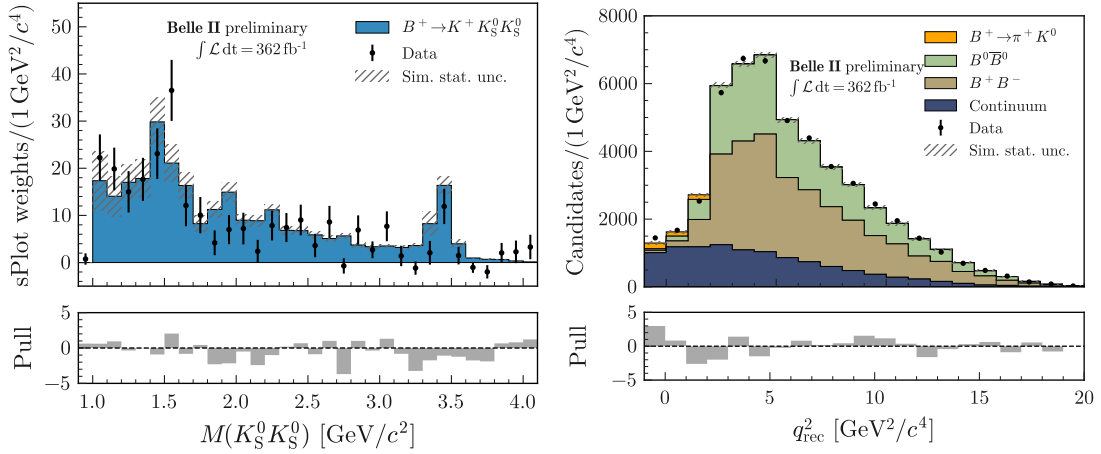


Figure 4: Left: Distribution of the invariant $K_S^0 K_S^0$ mass in background subtracted data. The simulated distribution is normalized to the number of BB events. The pull distribution is shown in the bottom panel. Right: q^2 distribution for data and MC obtained with the fit results to determine the branching fraction of the $B^+ \rightarrow \pi^+ K^0$ decay.

147 and validate the background contributions from $B^+ \rightarrow K^+ K_L^0 K_S^0$ and $B^+ \rightarrow K^+ n \bar{n}$. Validation
 148 procedures applied to other background contributions both for the ITA and the HTA are described
 149 in [8].

150 5. Signal extraction

151 Binned maximum likelihood fits are performed on data counts in the signal regions to extract
 152 the signal yield, both for the ITA and the HTA. For the ITA both on-resonance and off-resonance data
 153 are used, each one divided in 3×4 bins of $\eta(BDT_2)$ and q_{rec}^2 and the yields of the seven individual
 154 background categories ($B^+ B^-$, $B^0 \bar{B}^0$, $c\bar{c}$, $s\bar{s}$, $u\bar{u}$, $d\bar{d}$, $\tau^+ \tau^-$). The HTA uses only on-resonance data

and the signal region is divided in six bins of $\eta(BDT_h)$ and the background categories considered are BB (B^+B^- , $B^0\bar{B}^0$), $c\bar{c}$ and light quark pairs, while $\tau^+\tau^-$ can be neglected. The parameter of interest is μ , the signal branching fraction relative to its SM expectation, which is taken as the value 4.97×10^{-6} , excluding the long distance contribution from τ decays [1]. The systematic uncertainties are included in the likelihood as nuisance parameters. The most important ones are: the normalization of the $B\bar{B}$ background, the limited size of the simulated samples both for the ITA and the HTA. For the ITA another important contribution comes from the poor knowledge of some background contributions: $B^+ \rightarrow K^+ K_L^0 K_L^0$, $B \rightarrow D^{**}$. For the HTA another main contribution comes from the modeling of the extra photon multiplicity. Before extracting the result, an additional check for the ITA method has been performed by measuring the branching fraction of the $B^+ \rightarrow \pi^+ K^0$ decay. Similar signal extraction settings to the nominal analysis are used, the main differences are: the pion identification is used instead of kaon identification, the only on-resonance data are used, not all the systematic sources are considered. The measured value is $\mathcal{B}(B^+ \rightarrow \pi^+ K^0) = (2.5 \pm 0.5) \times 10^{-5}$, consistent with the PDG value. The post fit distribution of the q_{rec}^2 is shown in figure 4(right).

6. Results

The results for ITA of the the simultaneous fit to off-resonance and on-resonance data, together with the observed yields are illustrated in Figure 5. The signal strength is determined to be

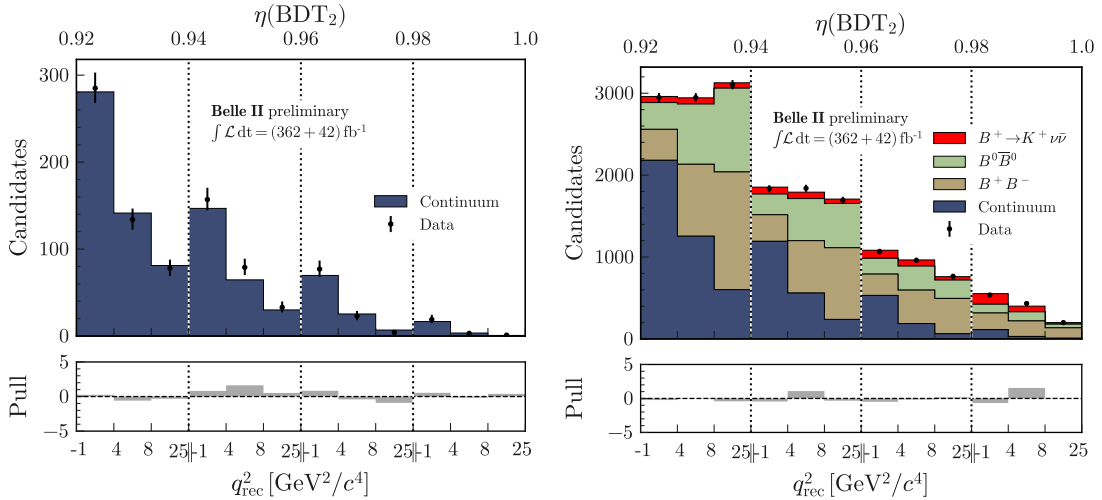


Figure 5: Observed yields and fit results in bins of the $\eta(BDT_2) \times q_{rec}^2$ space for the off-resonance (left) and the on-resonance (right) samples.

$\mu = 5.4 \pm 1.0(\text{stat}) \pm 1.1(\text{syst}) = 5.4 \pm 1.5$, corresponding to $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = [2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})] \times 10^{-5}$. By evaluating the profile likelihood for several μ values, we found the significance of the observed excess with respect to the background-only hypothesis, which is 3.5 standard deviations (σ) and the significance of the observed signal with respect to the SM expectation, which is 2.9σ . Figure 6 shows the post-fit distributions for $\eta(BDT_2)$ and q_{rec}^2 with a different binning with respect to the one used for the fit. The post-fit distributions are checked also considering only

179 events on the most signal-rich region, $\eta(BDT_2) > 0.98$. The distributions of $\eta(BDT_2) > 0.98$ and
 180 q_{rec}^2 for these events are shown in Figure 7.

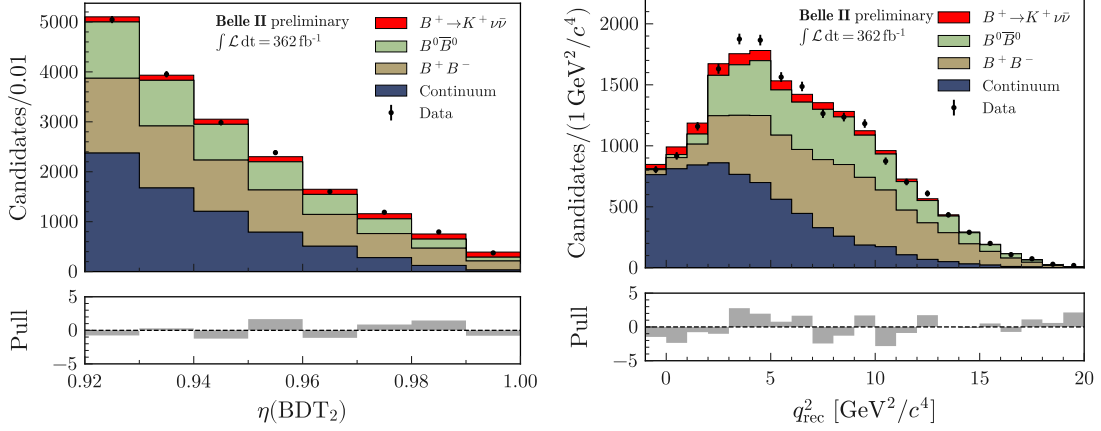


Figure 6: Observed yields and post-fit simulation data for the ITA, for $\eta(BDT_2)$ (left) and q_{rec}^2 (right).

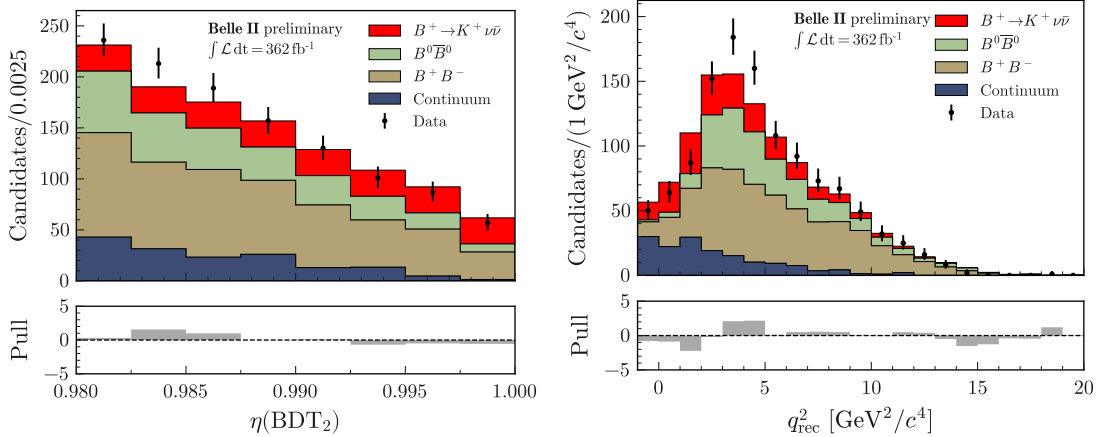


Figure 7: Observed yields and post-fit simulation data for the ITA, after requiring $\eta(BDT_2) > 0.98$, for $\eta(BDT_2)$ (left) and q_{rec}^2 (right).

181 The post-fit distribution of the fit variable $\eta(BDT_h)$ for the HTA is shown in figure 8(left) along
 182 with the post-fit distribution of q^2 . The fit results in a $\mu = 2.2^{+1.8}_{-1.7}$ (stat) $^{+1.6}_{-1.1}$ (syst) corresponding to
 183 $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = [1.1^{+0.9}_{-0.8}$ (stat) $^{+0.8}_{-0.5}$ (syst)] $\times 10^{-5}$. This result is compatible with the background-
 184 only hypothesis at 1.1σ and in agreement with the SM at 0.6σ .

185 Several consistency checks are performed to scrutiny the validity of the analysis: simulation
 186 and data events are divided into approximately same-size statistically independent samples based
 187 on different criteria. Quite good compatibility is observed between the split samples for the ITA
 188 and the HTA.

189 The results of the two analyses are compatible, with a difference in the signal strength of 1.2σ .
 190 Furthermore the overlap of the data sample is small, only 2% of the full ITA selected sample.
 191 Therefore, after the removal of the common events from the ITA sample, a combination of the

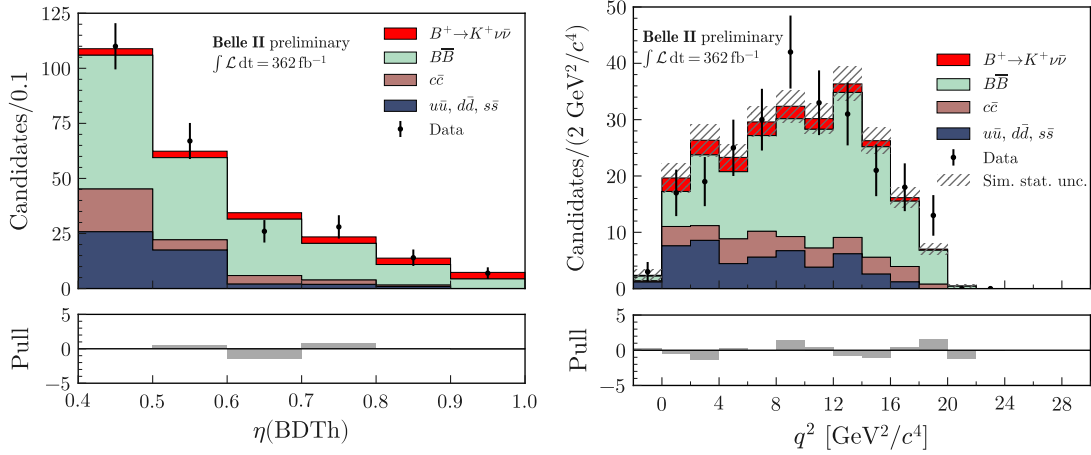


Figure 8: Observed yields and post-fit simulation data for the HTA, for $\eta(BDT_h)$ (left) and q_{rec}^2 (right)

192 two analyses is performed with a profile likelihood fit, incorporating correlations between common
 193 systematic uncertainties. The combined result for the signal strength is $\mu = 4.6 \pm 1.0(\text{stat}) \pm$
 194 $0.9(\text{syst}) = 4.6 \pm 1.3$ corresponding to :

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = [2.3 \pm 0.5(\text{stat})_{-0.4}^{+0.5} (\text{syst})] \times 10^{-5} = (2.3 \pm 0.7) \times 10^{-5} \quad (1)$$

195 This results in a significance with respect to the background-only hypothesis of 3.5σ and in a 2.7σ
 196 above the SM expectation.

197 Figure 9(left) show the values of the quantity $-2 \log L$, with L the likelihood, as a function of
 198 μ , for the ITA, the HTA and combined analyses. The value for each scan point is determined by
 199 fitting the data, where all parameters but μ are varied.

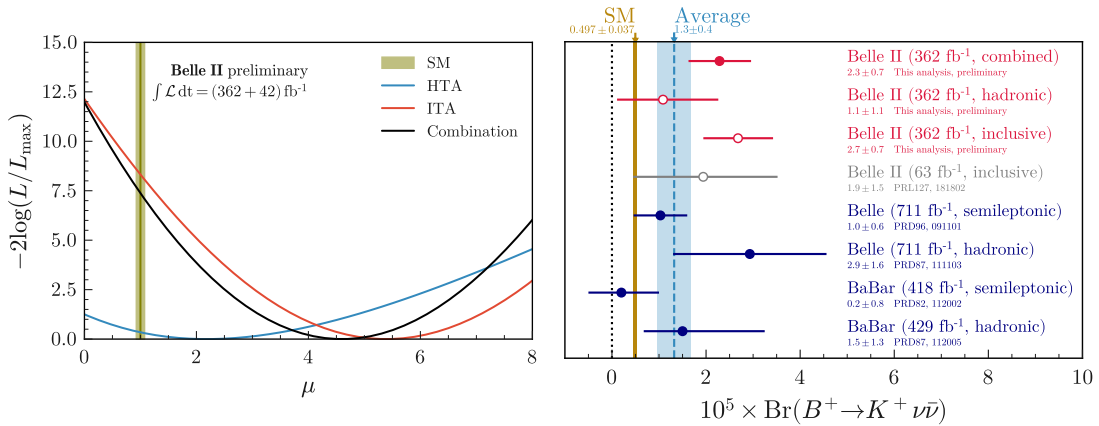


Figure 9: $-2 \log L$ for several values of μ , for the ITA, the HTA and combined analyses (left). Branching ratio measurements obtained in this work, the ones given by previous experiments, and the SM value (right).

200 Figure 9 (right) shows a comparison of the measurements for $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})$ obtained in
 201 this work with the previous results by other experiments and the value predicted by the SM. The
 202 weighted average is computed assuming symmetrized and uncorrelated uncertainties, excluding the

203 superseded measurement of Belle II (63 fb^{-1} , Inclusive) and the uncombined results of Belle II
204 shown as open data points. For the ITA the result is in agreement with the previous measurement
205 obtained with hadronic and inclusive tagging methods. A tension with previous semi-leptonic
206 measurement is observed, 2.3σ with BaBar measurement and 1.8σ with Belle. The HTA result is
207 in agreement with all the previous measurements.

208 7. Summary

209 A search for the rare decays $B^+ \rightarrow K^+ \nu \bar{\nu}$ is carried out with data corresponding to an integrated
210 luminosity of 362 fb^{-1} , collected by the Belle II experiment. Two analysis strategies have been
211 employed, the ITA with high sensitivity and the HTA, which is less performant but consists in
212 a well-established approach. The combination of the two analyses yields a branching fraction of
213 $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (2.3 \pm 0.7) \times 10^{-5}$, providing the first evidence of the decay with a significance
214 of 3.5 standard deviations and giving an excess of 2.7 standard deviations over the SM expectations.

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