

NNLO+PS predictions for Higgs production through bottom-quark fusion

Christian Biello,^a Aparna Sankar,^{a,b,*} Marius Wiesemann^a and Giulia Zanderighi^{a,b}

^aMax-Planck-Institut für Physik,
Boltzmannstraße 8, 85748 Garching, Germany

^bPhysik-Department, Technische Universität München,
James-Frank-Strasse 1, 85748 Garching, Germany

E-mail: biello@mpp.mpg.de, aparna@mpp.mpg.de, marius.wiesemann@mpp.mpg.de,
zanderi@mpp.mpg.de

We present next-to-next-to-leading-order (NNLO) QCD corrections for Higgs production through bottom-quark annihilation ($b\bar{b}H$) matched to parton showers (NNLO+PS) using the `MiNNLOPS` technique. The `MiNNLOPS` method is adapted for the extra scale dependence due to the Yukawa coupling renormalized in the $\overline{\text{MS}}$ scheme. The computation has been carried out in the five flavour scheme (5FS) neglecting the bottom mass. Results are compared against fixed-order predictions at NNLO and resummed predictions at next-to-next-to-leading-logarithmic (NNLL) accuracy. We also present preliminary results within the four-flavour scheme (4FS) setup, reaching a new level of precision in the massive scheme.

31st International Workshop on Deep Inelastic Scattering (DIS2024)
8–12 April 2024
Grenoble, France

*Speaker

1. Introduction

The Higgs boson is a key part of the Standard Model (SM) of particle physics. Since its discovery a decade ago, measuring its properties has been a primary focus at the Large Hadron Collider (LHC). These measurements confirm the SM and explore new physics. While current measurements of Higgs couplings align with SM predictions, more precise measurements could reveal small deviations. Accurate simulations of all Higgs production and decay modes at the LHC are essential for detecting deviations from SM predictions. The $b\bar{b}H$ process, though having a lower rate, is significant for precision measurements and beyond-the-SM (BSM) scenarios. It is challenging to detect directly due to large backgrounds and reduced rates when tagging bottom quarks but is crucial as an irreducible background in Higgs-boson pair production searches, especially at the High-Luminosity LHC (HL-LHC).

Calculations of the $b\bar{b}H$ process use either a five-flavour scheme (5FS) with massless bottom quarks or a four-flavour scheme (4FS) with massive bottom quarks. Significant advancements have been made in 5FS calculations, particularly with third-order QCD cross sections [1]. Progress in 4FS calculations has been slower due to their complexity, though NLO+PS in QCD combined with electroweak (EW) corrections remain state-of-the-art [2, 3]. Matching of NNLO QCD calculations with parton showers (NNLO+PS) presents a significant challenge in collider theory. For the $b\bar{b}H$ process, the first matching was done at NLO in 4FS using the MC@NLO and POWHEG methods. Here, we present the first fully-differential NNLO QCD calculation matched to a parton shower using the MiNNLO_{PS} method [4, 5] within the POWHEG framework [6].

2. Theoretical framework

The MiNNLO_{PS} cross section for $b\bar{b} \rightarrow H$ production can be expressed through the standard POWHEG formula for HJ production with a modified content of the POWHEG \bar{B} function [7]:

$$d\sigma_{\text{H}}^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{HJ}} \bar{B}^{\text{MiNNLO}_{\text{PS}}} \times \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R_{\text{HJ}}}{B_{\text{HJ}}} \right\}, \quad (1)$$

where Φ_{HJ} is the HJ phase space. Δ_{pwg} is the POWHEG Sudakov form factor with a cutoff $\Lambda_{\text{pwg}} = 0.89$ GeV. $d\Phi_{\text{rad}}$ and $p_{T,\text{rad}}$ denote the phase space measure and transverse momentum of the real radiation relative to HJ production. POWHEG matches the fixed-order HJ calculation with a parton shower by generating the first additional radiation using the ratio of the tree-level matrix elements for HJJ (R_{HJ}) and HJ (B_{HJ}) productions. Subsequent radiations with smaller transverse momenta are generated by a Shower Monte Carlo.

The central ingredient of the MiNNLO_{PS} method is the modified POWHEG \bar{B} function which is denoted as $\bar{B}^{\text{MiNNLO}_{\text{PS}}}$ in Eq. (1). The derivation of this function stems from transverse momentum resummation of color singlet production. $\bar{B}^{\text{MiNNLO}_{\text{PS}}}$ function is given by [4, 5]

$$\bar{B}^{\text{MiNNLO}_{\text{PS}}} = e^{-\tilde{S}(p_T)} \left\{ B \left(1 + \tilde{S}^{(1)} \right) + V + \int d\Phi_{\text{rad}} R + D^{(\geq 3)}(p_T) \times F^{\text{corr}} \right\}, \quad (2)$$

where Born B , virtual V and the real R contributions are calculated with strong coupling at p_T , transverse momentum of the Higgs. Here $e^{-\tilde{S}(p_T)}$ is the Sudakov form factor which regulates the

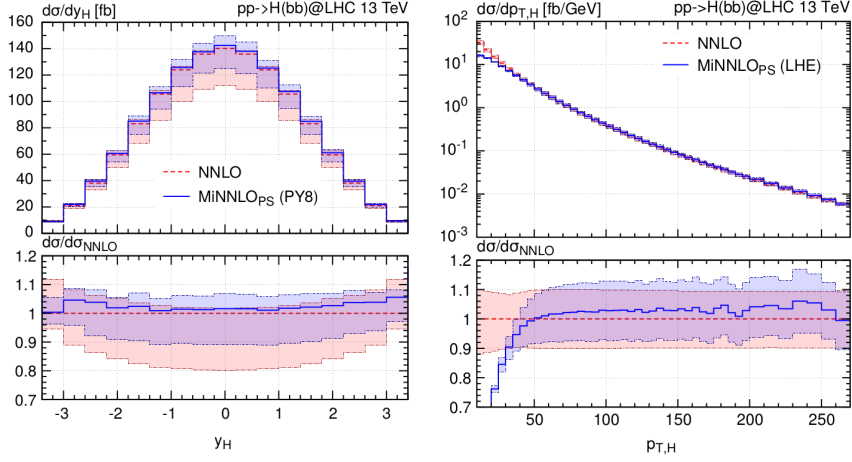


Figure 1: The left plots show the comparison of MiNNLO_{PS} predictions (blue, solid) with the NNLO results of Ref. [8] (red, dashed) for the rapidity distribution of the Higgs boson. The right plot shows the analytic $p_{T,H}$ spectrum up to α_s^2 from Ref. [9] (red, dashed) and our MiNNLO_{PS} prediction (blue, solid curve).

divergence of the $\bar{B}^{\text{MiNNLO}_{\text{PS}}}$ function for $p_T \rightarrow 0$ and $\tilde{S}^{(1)}$ is its first order expansion coefficient. $D^{(\geq 3)}(p_T)$ term multiplied with the spreading function F^{corr} contains the additional pieces which are necessary to attain the NNLO accuracy for the inclusive observables for the color singlet.

3. Phenomenological results for the 5FS

We present predictions for Higgs boson production via bottom-quark annihilation at the LHC (13 TeV), with a Higgs boson mass of 125 GeV. Using the 5FS approach with massless bottom quarks and a non-zero Yukawa coupling in the $\overline{\text{MS}}$ scheme, we employ the NNLO NNPDF40 parton distribution functions (PDFs) with $\alpha_s(m_Z) = 0.1189$ and assess theoretical uncertainties via a standard 7-point scale variation. For the simulations with parton shower, we use Pythia8 (PY8) with the A14 tune, excluding effects like hadronization, multi-parton interactions (MPI), and QED radiation.

Employing the MiNNLO_{PS} method, we obtain an inclusive cross section of $0.509^{+2.9\%}_{-5.3\%}$ pb which is consistent with the NNLO prediction of $0.518^{+7.2\%}_{-7.5\%}$ pb from SusHi [10, 11]. We further validate our MiNNLO_{PS} generator by comparing the rapidity and transverse momentum distributions of the Higgs against the corresponding fixed-order results [8, 9] in Fig.1. Using the NNLO set of CT14 PDFs, we find good agreement in the rapidity distribution, as shown in Fig.1. For the $p_{T,H}$ spectrum, NNLO and MiNNLO_{PS} results agree at higher $p_{T,H}$ values. However, for $p_{T,H} \rightarrow 0$, MiNNLO_{PS} remains finite whereas NNLO diverges.

Fig.2 compares MiNNLO_{PS} predictions for the $p_{T,H}$ distribution, including parton showering effects from PYTHIA8, against the analytic resummation at NNLO+NNLL [9]. At large $p_{T,H}$, both results agree within the uncertainty band. However, at small $p_{T,H}$, MiNNLO_{PS} scale bands underestimate uncertainties compared to more accurate NNLO+NNLL, suggesting the need for further variations within the shower settings to study this effect.

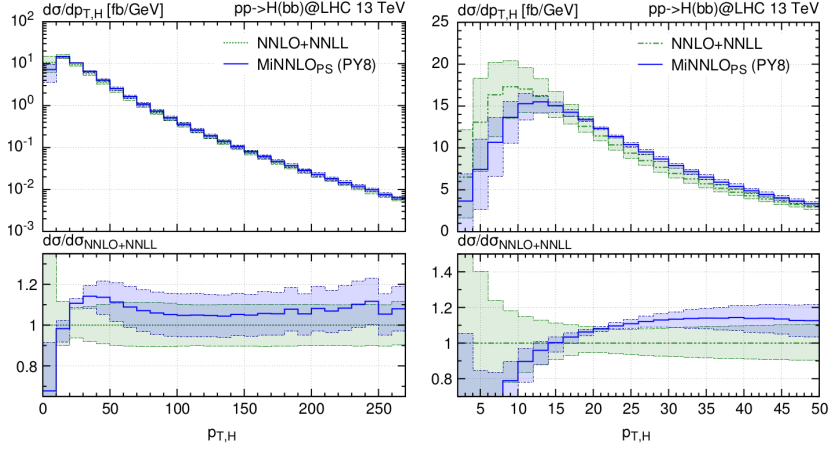


Figure 2: Predictions for the $p_{T,H}$ spectrum from our $\text{MiNNLO}_{\text{PS}}$ generator compared to the analytic resummation at NNLO+NNLL of Ref. [9] (green, double-dash-dotted curve).

4. Preliminary results for the 4FS

The 4FS implementation of the $\text{MiNNLO}_{\text{PS}}$ generator for $b\bar{b}H$ production presents greater complexity due to the higher final state multiplicity and the inclusion of massive colored final states. We provide preliminary results for the Higgs total cross section, employing the $\text{MiNNLO}_{\text{PS}}$ method for heavy-quark pair production plus a color singlet [12], accounting for the Yukawa scale dependence. While the two-loop amplitude for Higgs associated with massive bottom quarks is not known, we approximate it by applying a massification procedure [13, 14] to the massless amplitude [15], effectively capturing leading mass effects.

By setting the Higgs mass for the Yukawa scale and using a quarter of the transverse invariant mass for the strong couplings at the Born level, the NLO+PS generator predicts a cross-section of $0.381^{+20\%}_{-16\%}$ pb. This value is approximately 55% smaller than the NLO cross-section in 5FS, indicating the importance of collinear logarithmic contributions. On the other hand, $\text{MiNNLO}_{\text{PS}}$ predicts a cross-section of $0.464^{+14\%}_{-13\%}$ pb, which is much closer to NNLO 5FS values. This marks the first time that predictions from both schemes have shown agreement within the scale uncertainty.

5. Conclusions

We presented the NNLO QCD matching with parton shower for Higgs production via bottom fusion using the $\text{MiNNLO}_{\text{PS}}$ technique. Our analysis covers predictions in the 5FS and discusses ongoing investigations in the 4FS [16], showing promising preliminary findings.

References

- [1] C. Duhr, F. Dulat and B. Mistlberger, *Higgs Boson Production in Bottom-Quark Fusion to Third Order in the Strong Coupling*, *Phys. Rev. Lett.* **125** (2020) 051804 [1904.09990].

- [2] M. Wiesemann, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni and P. Torrielli, *Higgs production in association with bottom quarks*, *JHEP* **02** (2015) 132 [[1409.5301](#)].
- [3] D. Pagani, H.-S. Shao and M. Zaro, *RIP $Hb\bar{b}$: how other Higgs production modes conspire to kill a rare signal at the LHC*, *JHEP* **11** (2020) 036 [[2005.10277](#)].
- [4] P.F. Monni, P. Nason, E. Re, M. Wiesemann and G. Zanderighi, *MINNLO_{PS}: a new method to match NNLO QCD to parton showers*, *JHEP* **05** (2020) 143 [[1908.06987](#)].
- [5] P.F. Monni, E. Re and M. Wiesemann, *MINNLO_{PS}: optimizing $2 \rightarrow 1$ hadronic processes*, *Eur. Phys. J. C* **80** (2020) 1075 [[2006.04133](#)].
- [6] C. Biello, A. Sankar, M. Wiesemann and G. Zanderighi, *NNLO+PS predictions for Higgs production through bottom-quark annihilation with MINNLO_{PS}*, *Eur. Phys. J. C* **84** (2024) 479 [[2402.04025](#)].
- [7] P. Nason, *A New method for combining NLO QCD with shower Monte Carlo algorithms*, *JHEP* **11** (2004) 040 [[hep-ph/0409146](#)].
- [8] R. Mondini and C. Williams, *Bottom-induced contributions to Higgs plus jet at next-to-next-to-leading order*, *JHEP* **05** (2021) 045 [[2102.05487](#)].
- [9] R.V. Harlander, A. Tripathi and M. Wiesemann, *Higgs production in bottom quark annihilation: Transverse momentum distribution at NNLO+NNLL*, *Phys. Rev.* **D90** (2014) 015017 [[1403.7196](#)].
- [10] R.V. Harlander, S. Liebler and H. Mantler, *SusHi: A program for the calculation of Higgs production in gluon fusion and bottom-quark annihilation in the Standard Model and the MSSM*, *Comput. Phys. Commun.* **184** (2013) 1605 [[1212.3249](#)].
- [11] R.V. Harlander and W.B. Kilgore, *Higgs boson production in bottom quark fusion at next-to-next-to leading order*, *Phys.Rev.* **D68** (2003) 013001 [[hep-ph/0304035](#)].
- [12] J. Mazzitelli, V. Sotnikov and M. Wiesemann, *Next-to-next-to-leading order event generation for Z-boson production in association with a bottom-quark pair*, [2404.08598](#).
- [13] A. Mitov and S. Moch, *The Singular behavior of massive QCD amplitudes*, *JHEP* **05** (2007) 001 [[hep-ph/0612149](#)].
- [14] G. Wang, T. Xia, L.L. Yang and X. Ye, *On the high-energy behavior of massive QCD amplitudes*, *JHEP* **05** (2024) 082 [[2312.12242](#)].
- [15] S. Badger, H.B. Hartanto, J. Kryś and S. Zoia, *Two-loop leading-colour QCD helicity amplitudes for Higgs boson production in association with a bottom-quark pair at the LHC*, *JHEP* **11** (2021) 012 [[2107.14733](#)].
- [16] C. Biello, J. Mazzitelli, A. Sankar, M. Wiesemann and G. Zanderighi, *NNLO+PS predictions for $b\bar{b}H$ production in the four-flavour scheme*, [in preparation](#).