

# Probing lepton-flavor-violating processes in $e^+e^-$ colliders

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A scenario involving lepton-flavor-violating (LFV) interactions, either due to a LFV coupling of a scalar or a vector boson, is an intriguing beyond standard model (BSM) phenomenon. This LFV coupling in the presence of muons leads to a rich phenomenology including an extra contribution to muon anomalous magnetic moment. With the low-energy effective coupling  $\mathcal{L}_{\phi e\mu} = h_{e\mu}\phi\bar{e}(1+\gamma^5)\mu + \text{h.c.}$ , which turns electron into muon or vice versa through a scalar  $\phi$ , we first derive the  $(h_{e\mu}, M_\phi)$  parameter space that can account for experimental measurements of muon anomalous magnetic moment. We propose to probe such a parameter space or that with an even smaller  $h_{e\mu}$  by searching for background-free processes of same-sign, same-flavor final-state lepton pairs  $e^+e^- \rightarrow e^\pm\mu^\mp\phi \rightarrow e^\pm e^\pm\mu^\mp\mu^\mp$  at Belle II experiment. Assuming such final states are detected by Belle II, we further propose an effective method to discriminate between scalar and vector boson-mediated LFV interactions based on significant differences in their event kinematic distributions.

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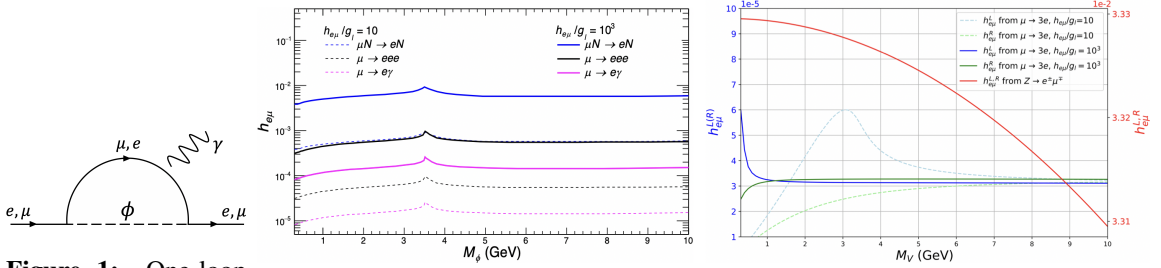
## 1. The lepton-flavor-violating scalar mediator

Various BSM theories involve LFV processes where charged leptons change flavor. LFV searches directly address new physics (NP) in flavor and generations, in which muon-related LFV processes offer potential solutions to the long-standing  $g_\mu - 2$  discrepancy. A model of a real scalar mediator  $\phi$  interacting with a pair of oppositely-charged, different-flavored  $e^\pm\mu^\mp$  is described as [1]

$$\mathcal{L}_{\phi e\mu} = \sum_{\ell=e,\mu,\tau} g_\ell \phi \bar{\ell}(1 + \gamma^5)\ell + h_{e\mu} \phi \bar{e}(1 + \gamma^5)\mu + h_{e\mu}^* \phi \bar{\mu}(1 - \gamma^5)e \quad (1)$$

where  $g_\ell$  and  $h_{e\mu}$  are lepton-flavor-conserving and LFV couplings, respectively. We assume vanishing flavor-diagonal terms, i.e., the Lagrangian contains only LFV  $e\mu$  terms. Using Feynman rules from eq. (1), processes  $e^+e^- \rightarrow e^\pm\mu^\mp\phi$  depend only on  $|h_{e\mu}|^2$  and allow for probing positive real LFV couplings. The one-loop contribution to the muon anomalous magnetic moment shown in figure 1 is evaluated as [2]  $\Delta a_\mu = (2x_a^2 \log(x_a/(x_a - 1)) - 1 - 2x_a)h_{e\mu}^2/(8\pi^2)$  with  $x_a = m_\phi^2/m_\mu^2$ .

## 2. Probing the LFV model at Belle II experiment



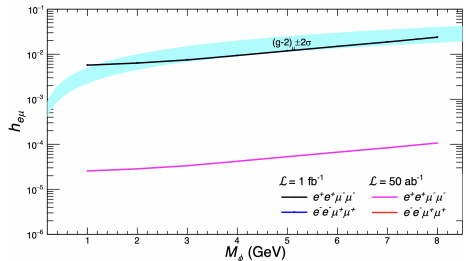
**Figure 1:** One-loop

contribution to  $a_\mu$  mediated by scalar  $\phi$ .

**Figure 2:** Constraints on LFV couplings mediated by (a) scalar and (b) vector portal scenarios.

Experimental constraints on a flavor-violating boson model depend on the relative strengths of  $g_\ell$  and  $h_{e\mu}$  couplings of bosons to leptons. These constraints arise by the effect of the  $Z - Z'$  mixing with  $Z'$  boson arising from an extra  $U(1)'$  symmetry. Existing constraints on LFV vector coupling can be derived after diagonalizing interactions of  $\hat{Z}$  and  $\hat{Z}'$  with charged leptons,  $\mathcal{L}_{\text{int}} = -\bar{\ell}_i \gamma^\lambda (\beta_{\ell_i \ell_j}^L P_L + \beta_{\ell_i \ell_j}^R P_R) \ell_j Z_\lambda - \bar{\ell}_i \gamma^\lambda (h_{\ell_i \ell_j}^L P_L + h_{\ell_i \ell_j}^R P_R) \ell_j Z'_\lambda$  where  $\beta$  ( $h$ ) $^{(L,R)}$  are left- (right-handed)  $Z$  and  $Z'$  couplings, respectively. Figure 2 shows exclusion regions in scalar  $\phi$  [3] and vector  $V$  [4] boson masses and LFV couplings for cases with ratios of  $h_{e\mu}$  to  $g_\ell$  being 10 and  $10^3$ .

The sensitivity to  $e\mu$  flavor-violating interactions is studied at Belle II, which is an energy asymmetric detector of 7 GeV  $e^-$  and 4 GeV  $e^+$ . Final-state same-sign lepton pairs in processes  $e^+e^- \rightarrow e^\mp\mu^\pm\phi \rightarrow e^\mp\mu^\pm\mu^\pm e^\mp$ , where  $\phi \rightarrow e^\mp\mu^\pm$ , are essentially BG free. Applying BG free with 95% CL and kinematical cuts [5] for final-state leptons, the upper bound on  $h_{e\mu}$  for  $e^+e^- \rightarrow e^\mp\mu^\pm\mu^\pm e^\mp$  is shown in figure 3. At  $\mathcal{L} = 1 \text{ fb}^{-1}$ , the Belle II limit on  $h_{e\mu}$  for  $1 \leq M_\phi/\text{GeV} \leq 8$  already touches the  $2\sigma$  parameter region

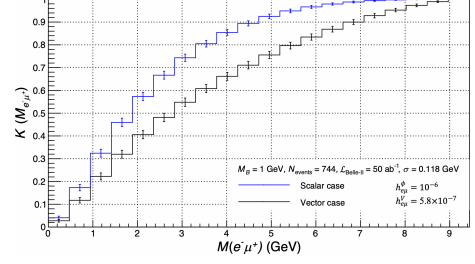


**Figure 3:** Constraints on  $h_{e\mu}$  of LFV searches at Belle II experiment.

avored by the  $g_\mu - 2$  anomaly. The sensitivity is inversely proportional to the square root of the luminosity. With a higher luminosity, one can probe the LFV model significantly below the favored parameter region for muon anomalous magnetic moment. In the case of observing the same-sign lepton pairs, it is possible to distinguish between scalar and vector LFV scenarios.

### 3. Discriminating scalar from vector boson portals in LFV processes.

The cumulative mass distribution as a function of the non-resonant  $e\mu$  invariant mass,  $K^i(M_{e^\mp\mu^\pm}) = \sum_i N_{e^\mp\mu^\pm B}^i / N_{e^\mp\mu^\pm B}^{\text{total}}$  [6] (with  $B = \phi, V$ ) is exploited to distinguish LFV scalar  $\phi$  from vector  $V$  models. Here,  $N_{e^\mp\mu^\pm B}^{i(\text{total})}$  represent the number of events in a certain  $i$  and the total mass range, respectively.  $K^i(M_{e^\mp\mu^\pm})$  is useful due to significant differences between peak event rates in different scenarios. Figure 4 shows the case of  $K(M_{e^-\mu^+})$  with statistical errors in binned histograms, each with a bin width of  $2\sigma$ , with  $\sigma$  the recoil mass resolution.



**Figure 4:** Cumulative mass distribution of  $e^+e^- \rightarrow e^-\mu^+B$  at  $M_B = 1$  GeV,  $\mathcal{L} = 50$   $\text{ab}^{-1}$ .

Quantitatively, the ordering  $K^\phi(M_{e^\mp\mu^\pm}) > K^V(M_{e^\mp\mu^\pm})$  is observed in this simulation. The function  $K^\phi(M_{e^\mp\mu^\pm})$  increases more rapidly in the middle range of  $M_{e^\mp\mu^\pm}$  due to the larger event rates of scalar LFV scenario in this mass range. Consequently, LFV scalar and vector boson scenarios can be distinguished at the Belle II detector.

### 4. Summary and conclusions

We study the Belle II sensitivity to the  $e\mu$  flavor-violating scalar boson model. The sensitivity to the LFV Yukawa coupling  $h_{e\mu}$  of processes  $e^+e^- \rightarrow e^\pm\mu^\mp\phi \rightarrow e^\pm e^\pm\mu^\mp\mu^\mp$  for  $\mathcal{L} = 1$   $\text{fb}^{-1}$  at Belle II can already approach the favorable parameter range accounting for the measured  $g_\mu - 2$  anomaly in the mass range of  $1 \leq M_\phi/\text{GeV} \leq 8$ . At high luminosity, we could potentially search for the NP. Particularly, the sensitivity for full Belle II luminosity of 50  $\text{ab}^{-1}$  to  $h_{e\mu}$  is still below the current LFV constraints. The cumulative mass distribution is proposed to distinguish between LFV scenarios involving scalar and vector bosons with statistical uncertainties taken into account.

### References

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