

W boson mass in gauge-Higgs unification

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The CDF collaboration reported an anomaly of the W boson mass in 2022. We discuss the possibility to explain the anomaly in a gauge-Higgs unification model. We evaluate the W boson mass in the $SO(5) \times U(1)_X \times SU(3)_C$ gauge-Higgs unification in the Randall-Sundrum warped space. The muon decay proceeds by the exchange of not only the zero mode of the W boson but also Kaluza-Klein excited states at the tree level. We find that the anomaly can be explained by these effects in the gauge-Higgs unification model.

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1. Introduction

In 2022, the CDF collaboration reported on the mass of the W boson, $m_W^{\text{CDF}} = 80.4335 \pm 0.0094 \text{ GeV}$. [1] The predicted value in the Standard Model (SM) is $m_W^{\text{SM}} = 80.354 \pm 0.007 \text{ GeV}$. [2–4] The discrepancy between the two has triggered huge debates on possible new physics beyond the SM. The ATLAS collaboration also reanalyzed the data in 2011 and obtained $m_W^{\text{ATLAS}} = 80.360 \pm 0.016 \text{ GeV}$. [5] Although the experimental situation has not been settled yet, it is worth to examine models to find whether or not they can lead to a larger value for m_W than m_W^{SM} without conflicting with other observation at low energies.

2. Gauge-Higgs unification model

Gauge-Higgs Unification (GHU) models solve the hierarchy problem. The Higgs boson is a fifth-dimensional component of gauge fields, therefore it is protected from divergence by the gauge principle. And the interactions of the Higgs boson are also governed by the gauge principle. A realistic model of gauge-Higgs unification has been proposed. This model is based on the gauge-Higgs unification in the Randall-Sundrum (RS) warped space, which is described by the gauge group $SO(5) \times U(1)_X \times SU(3)_C$. This kind of higher-dimensional theory incorporates Kaluza-Klein (KK) excitation modes. These particles are constrained by collider experiments and the lower limit of the typical KK mass scale (m_{KK}) is 13 TeV by the LHC experiments. [6] Another important parameter is the Aharonov-Bohm (AB) phase (θ_H). In GHU models, the gauge symmetry is dynamically broken by the AB effect. The parameter is constrained theoretically and experimentally and the bound is $\theta_H \lesssim 0.1$.

KK excited states of the W and W_R gauge bosons contribute to the W boson mass. The relationship between the gauge couplings and the ratio of the W and Z boson masses, m_W/m_Z , changes even at the tree level. The dominant contributions come from large gauge couplings of left-handed leptons to the first KK excited states of the W boson, the change in the W couplings of the leptons (e and μ), and the change of the relation between the gauge couplings and the mass ratio m_W/m_Z .

3. The W boson mass

In the SM the Fermi constant G_μ determined from the μ -decay is given by [7]

$$\frac{G_\mu}{\sqrt{2}} = \frac{\pi\alpha}{2s_W^2} \frac{1}{m_W^2} (1 + \Delta r_{\text{SM}}^{\text{loop}}), \quad s_W^2 = 1 - \frac{m_W^2}{m_Z^2}, \quad (1)$$

where $\alpha^{-1} = 137.035999084(21)$, $G_\mu = 1.1663788(6) \times 10^{-5} \text{ GeV}^{-2}$ and $m_Z = 91.1876(21) \text{ GeV}$. [8] $\Delta r_{\text{SM}}^{\text{loop}}$ represents the sum of all loop corrections, which depends on α , m_W , m_Z , m_H , strong gauge coupling constant, and masses of quarks and leptons.

In the GHU model, on the other hand, the Fermi constant has additional factor.

$$\frac{G_\mu}{\sqrt{2}} = \frac{\pi\alpha}{2\sin^2\theta_W^0} \frac{\hat{g}_{\mu\nu\mu,L}^{W(0)} \hat{g}_{e\nu e,L}^{W(0)}}{m_{W(0)}^2} (1 + \Delta r_G) (1 + \Delta r_{\text{GHU}}^{\text{loop}}), \quad (2)$$

$\Delta r_{\text{GHU}}^{\text{loop}}$ represents the sum of loop corrections and we take $\Delta r_{\text{GHU}}^{\text{loop}} = \Delta r_{\text{SM}}^{\text{loop}} = 0.0383$. Δr_G is the new tree level contributions for the Fermi constant given by

$$\Delta r_G = \frac{1}{\hat{g}_{\mu\nu\mu,L}^{W^{(0)}} \hat{g}_{e\nu e,L}^{W^{(0)}}} \sum_{n=1}^{\infty} \left\{ \hat{g}_{\mu\nu\mu,L}^{W^{(n)}} \hat{g}_{e\nu e,L}^{W^{(n)}} \left[\frac{m_{W^{(0)}}}{m_{W^{(n)}}} \right]^2 + \hat{g}_{\mu\nu\mu,L}^{W_R^{(n)}} \hat{g}_{e\nu e,L}^{W_R^{(n)}} \left[\frac{m_{W^{(0)}}}{m_{W_R^{(n)}}} \right]^2 \right\}, \quad (3)$$

where $\hat{g}_{e\nu e,L}^{W^{(n)}}$ and $\hat{g}_{e\nu e,L}^{W_R^{(n)}}$ are the couplings of $W^{(n)}$ and $W_R^{(n)}$ to $e_L \nu_{eL}$, respectively. The right-handed couplings are very small and have been omitted. In GHU the W boson mass $m_W = m_{W^{(0)}}$ is determined by solving (2) and (3).

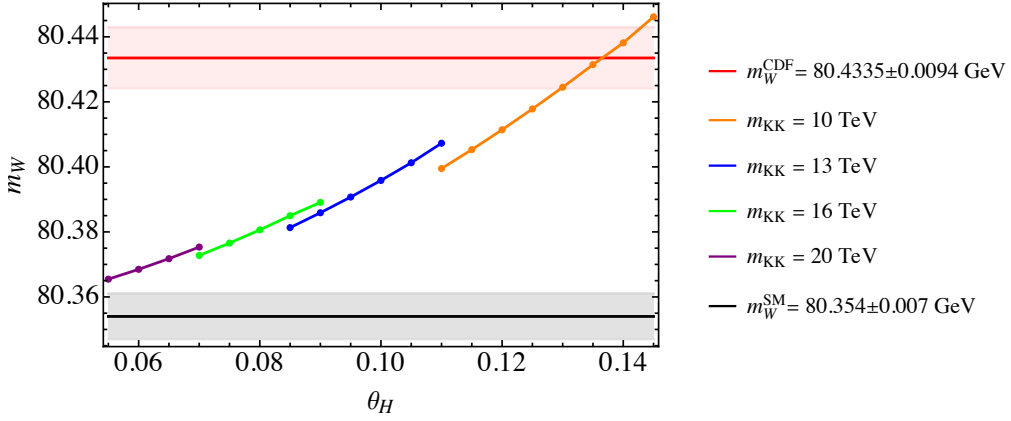


Figure 1: The W boson mass m_W in GHU is plotted as a function of θ_H with various m_{KK} . The constraint $m_{\text{KK}} \gtrsim 13$ TeV is obtained from the experimental data at LHC. The predicted m_W in GHU for $13 \text{ TeV} \leq m_{\text{KK}} \leq 20 \text{ TeV}$ lies between m_W^{SM} and m_W^{CDF} .

Fig. 1 shows the predicted values for m_W with different values of m_{KK} and θ_H . It is seen that m_W in GHU model becomes larger than m_W^{SM} , but is smaller than m_W^{CDF} for $13 \text{ TeV} \leq m_{\text{KK}} \leq 20 \text{ TeV}$. The GHU model in the RS space naturally predicts the W boson mass well above m_W^{SM} .

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