

# Electroweak Corrections to Double Higgs Production at the LHC

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We report the results for the complete next-to-leading order electroweak corrections to  $p p \rightarrow HH$  at the Large Hadron Collider. The dominant gluon-gluon fusion channel is considered. Results for the total and differential cross sections are presented.

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## 1. Introduction

The discovery of the Higgs boson [1, 2] opens a new frontier in exploring electroweak (EW) symmetry breaking and the Standard Model (SM). A key focus at the Large Hadron Collider (LHC) is understanding Higgs self-interactions, which are crucial for probing the structure of the Higgs potential. Higgs boson pair production, directly linked to the Higgs trilinear coupling  $\lambda_{HHH}$ , provides a unique window into this domain. While current LHC data begin to constrain  $\lambda_{HHH}$  [3–5], deviations from the SM prediction could imply modifications to the Higgs potential.

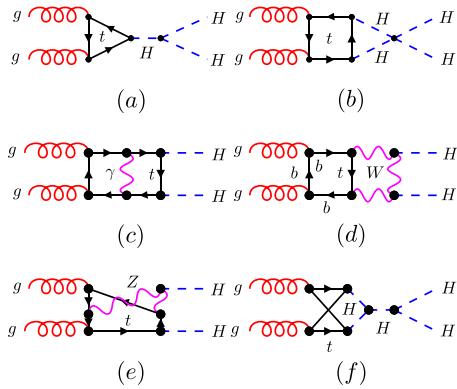
The dominant production mode for Higgs pairs at the LHC is gluon-gluon fusion, a loop-induced process in the SM. This makes precise theoretical predictions challenging, requiring advanced techniques beyond leading order (LO). Significant progress has been made, including next-to-leading order (NLO) QCD calculations [6–9], the incorporation of soft-gluon resummation and parton shower effects [10–13], and even next-to-next-to-next-to-leading order ( $N^3\text{LO}$ ) QCD corrections within the heavy top-quark limit [14, 15].

Different from QCD corrections, the Higgs self-couplings receive corrections from high order electroweak (EW) corrections. In addition, EW corrections, driven by Sudakov logarithms [16, 17], are particularly significant at high energies. However, calculating NLO EW corrections for  $gg \rightarrow HH$  is exceptionally complicated, as it involves two-loop diagrams with multiple mass scales. Previous attempts [18–23] have provided partial results.

In this proceeding, we present a complete computation of NLO EW corrections to  $gg \rightarrow HH$ , accounting for all two-loop diagrams and mass effects. Our results aim to enhance the precision of theoretical predictions, addressing a long-standing goal in the community [24–28].

## 2. Calculation

NLO EW corrections for  $gg \rightarrow HH$  include only virtual contributions, due to the prohibition of  $gg \rightarrow HH\gamma$  by the Furry Theorem. The two-loop Feynman diagrams and amplitudes are generated using FeynArt [29], with representative diagrams shown in Fig. 1.



**Figure 1:** Representative Feynman diagrams for  $gg \rightarrow HH$  at LO (a) and NLO EW corrections (b-f).

LO squared matrix elements are obtained with the help of `MadGraph5` [30], and LO events are generated using `Parni` [31]. NLO results are obtained by reweighting the LO events. Specifically, NLO amplitudes are expressed as linear combinations of scalar integrals using `CalcLoop` [32], categorized into 3 (116) integral families for 1-loop (2-loop) contributions. These are further reduced to master integrals with `Blade` [33]. Master integrals are numerically solved via differential equations with respect to the Mandelstam variables  $\hat{s}$  and  $\hat{t}$ , using boundary conditions from `AMFlow` [34].

To simplify computations, we set  $\epsilon = \pm 1/1000$  in our calculation. This can avoid Laurent expansions and reducing resource demands, as proposed in Refs. [34]. The results based on both  $\epsilon = \pm 1/1000$  can be used to check divergence cancellations and further mitigate the error caused by the finite  $\epsilon$  effect.

### 3. Results

The total cross sections for the gluon-gluon fusion channel of  $pp \rightarrow HH$  at LO and NLO are presented in Tab. 1, where three different renormalization/factorization scales are used. The scale dependence of the strong coupling  $\alpha_s$  is the primary source of the observed  $\sim 20\%$  uncertainties at both LO and NLO. In contrast, the  $\mathcal{K}$ -factor remains stable with different  $\mu$  choices. The consistent NLO EW correction, ranging from  $-4.6\%$  to  $-4.2\%$ , indicates that higher-order EW effects contribute only a few per mille to the total cross section.

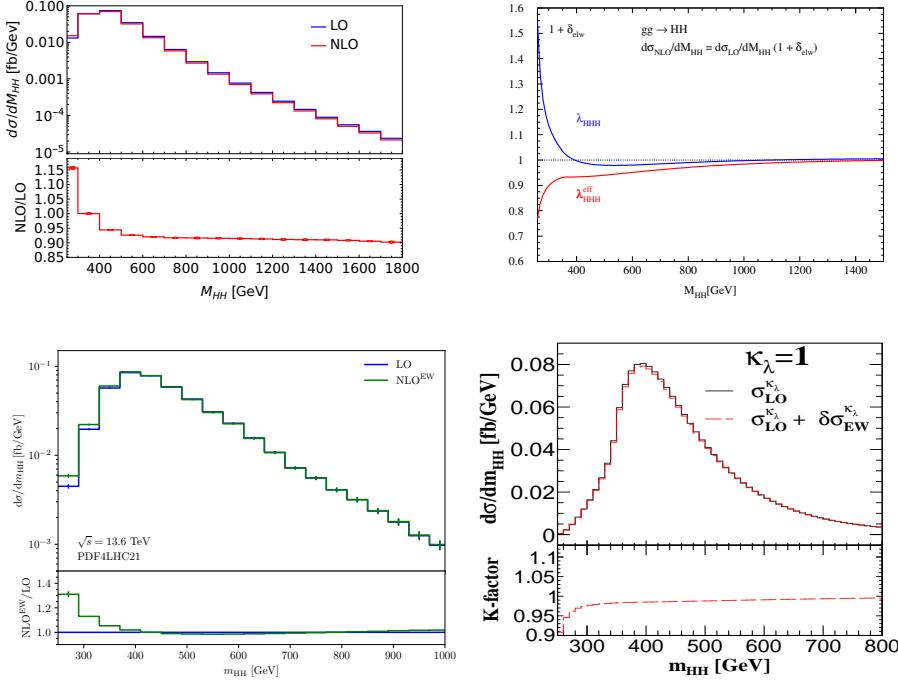
$\mu$	$M_{HH}/2$	$\sqrt{p_T^2 + m_H^2}$	$m_H$
LO	19.96(6)	21.11(7)	25.09(8)
NLO	19.12(6)	20.21(6)	23.94(8)
$\mathcal{K}$ -factor	0.958(1)	0.957(1)	0.954(1)

**Table 1:** LO and NLO EW corrected integrated cross sections (in fb) with  $\sqrt{s} = 14$  TeV. The uncertainties arise from statistical errors in phase space integration.

In Fig. 2, we present the invariant mass distribution of the Higgs pair,  $M_{HH}$ , taken from different literatures. The upper left plot is based on our calculation, which incorporates complete NLO EW corrections. The upper right plot is from [19], based on Top-Yukawa-induced corrections. The lower left plot is from [23], containing both Yukawa and Higgs self-coupling type corrections. The lower right plot is from [22], which includes Higgs self-coupling type corrections.

We observe that  $M_{HH}$  receives significant corrections at the  $HH$  production threshold in these plots. The two plots on the right-hand side suggest that Top-Yukawa-induced corrections and Higgs self-coupling type corrections have opposite signs in the threshold region. The combination of these two contributions gives positive corrections at the  $HH$  production threshold, as shown in the lower left plot, which amount to approximately  $\sim 30\%$ . Our calculation shows that the complete NLO EW correction is about  $\sim 15\%$  with the binning we selected. The two plots on the left-hand

side indicate that the gauge boson contributions are negative and important, as also pointed out in Ref. [23].



**Figure 2:** Invariant mass distribution of the Higgs pair. The upper left plot is based on our calculation, the upper right plot is taken from [19], the lower left plot is taken from [23] and the lower right plot is taken from [22].

#### 4. Conclusion

We review the recent progress in the calculation of NLO EW corrections to double Higgs production at the LHC. The complete NLO EW corrections are about +4% at the total cross section level and range from -10% to +15% at the differential level.

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