

Are Neutron Stars Rich In H-dibaryons?

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The possible existence of an H-dibaryon near the $\Lambda - \Lambda$ threshold has still not been decided experimentally. This raises the question of the potential effects on neutron stars if it does exist. We explore the consequences within the quark-meson coupling model, using the excluded volume formalism. While the H is abundant in heavy stars the maximum mass is only lowered slightly by its presence.

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1. Introduction

The H-dibaryon is a 6-quark, spinless boson with isospin zero and baryon number 2 [1]. Its composition is uuddss. Theoretical studies of the H have concluded that the H, if it exists, is likely to have a mass around the $\Lambda - \Lambda$ threshold [2–5]. The elusive H has so far evaded experimental detection with the current lower limit at $M_H > 2224$ MeV [6]. However, there is a possibility that the H could exist within the cores of neutron stars (NS). Here we examine this issue within the framework of the quark-meson coupling (QMC) model, starting with its effects on the equation of state (EoS) of dense matter in β -equilibrium.

Heavy NS have a mass of order $2 M_\odot$ or more, giving them an inner core density of around $0.8 - 1.0 \text{ fm}^{-3}$ [7–11]. At these densities the argument for hyperons in β -equilibrium is particularly strong. The Λ is the first hyperon to appear, at just above $3 n_0$ in QMC [12–14]. Since the mass of the H is thought to be near the $\Lambda - \Lambda$ threshold, then the H, should it exist, would be expected to occur shortly after the Λ . However, like the hyperons, the H should lower the predicted maximum mass of the NS. This effect is expected to be more severe in the case of the H, since it is a boson with zero momentum, but this is countered by the interaction of the H with the surrounding baryonic medium [15, 16].

There has only been a handful of work modeling the appearance of the H in NS [15–18]. The intermediate range forces involving the H are created by the scalar and vector mesons with the coupling strengths $g_{\sigma,H}$ and $g_{\rho,H}$. These are often fitted under the assumption that the H is present within the star, matching available NS observations [15, 18]. QMC is attractive in terms of modeling the H because the coupling strengths are predicted within the theory and there is no freedom to adjust $g_{\sigma,H}$ and $g_{\rho,H}$. Either the H exists and is capable of producing a heavy mass star, or it is incompatible.

In the following section we outline the formalism of incorporating the H into the nuclear EoS. The theory used here is QMC with the excluded volume effect (EVE), with its details available in Refs. [14, 19, 20]. The results are then presented with heavy NS constraints and the ramifications of these are discussed. We finish with a short conclusion on whether NS are really H-matter stars.

2. QMC Equation of State with the H-particle

The Lagrangian for the H uses a minimal coupling scheme suggested by [15].

$$\mathcal{L}_D = \mathcal{D}_\mu^* H^* \mathcal{D}^\mu H - M_H^{*2} H^* H. \quad (1)$$

Here \mathcal{D}_μ is defined as $\mathcal{D}_\mu = \partial_\mu + ig_{\omega,H}\omega_\mu$, which is the standard replacement for the vector ω field. M_H^* is the effective mass and in QMC is given in equation (5). The equation of motion for the H is presented in Ref. [15]. Of immediate concern is the energy density and the mean-field contributions. Since the H does not carry isospin, only the σ and ω field equations are changed. The modifications to the mean fields are given in Eqs. (2) and (3) as follows:

$$m_\sigma^2 \sigma + \lambda_3 \frac{g_\sigma^3}{2} \sigma^2 = \sum_f n_f^s - \frac{\partial M_H^*}{\partial \sigma} n_H, \quad (2)$$

$$m_\omega^2 \omega = \sum_f g_{\omega,f} n_f^v + g_{\omega,H} n_H. \quad (3)$$

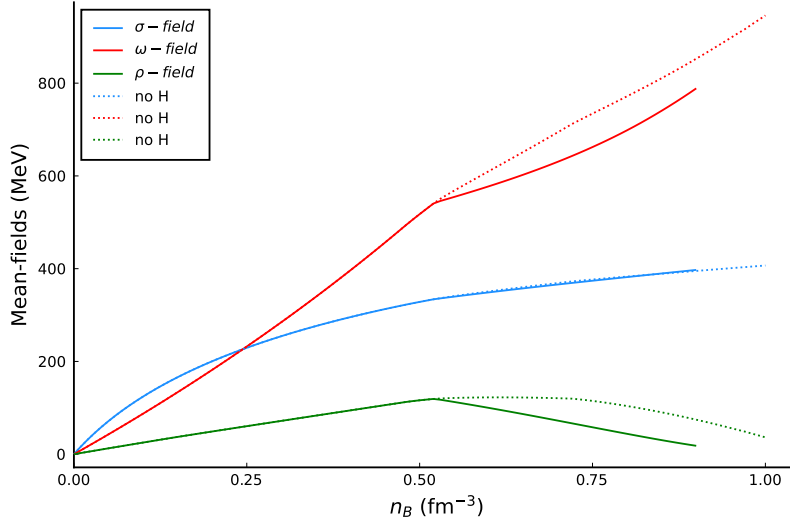


Figure 1: The mean-fields with neutron couplings are shown, with and without the H dibaryon. $M_H = 2247$ MeV is used here.

The λ_3 coefficients adjust the strength of the self interaction term necessary to lower the incompressibility [21]. $g_{\omega,H} = \frac{4}{3}g_{\omega,N}$, the strength of the coupling of the H to the ω field, is set by simple counting of non-strange quarks. This is the same scheme used in Ref. [15]. n_f^s and n_f^v are the scalar and vector densities, with the summation over n , p , Λ , Ξ^0 , and Ξ^- . The Σ and Δ have previously been shown not to appear as discussed in Refs. [20, 22]. The contribution to the energy density is

$$\epsilon_H = 2M_H^{*2}H^*H = M_H^*n_H. \quad (4)$$

We see that the H does not contribute directly to the pressure but there is an indirect contribution through the modification of the mean-fields described in Eqs. (2) and (3). These resulting changes to the mean-fields are displayed in Fig. 1.

$$\begin{aligned} M_H^* &= M_H - 2 \times [0.6672 + 0.04638R_H - 0.0022R_H^2]g_{\sigma\sigma} \\ &\quad + 2 \times [0.00146 + 0.0691R_H - 0.00862R_H^2](g_{\sigma\sigma})^2. \end{aligned} \quad (5)$$

The effective masses for the baryon octet in QMC are given in Ref. [23]. To model M_H^* , we note that the H has twice the quark composition of the Λ . In QMC the mesons only couple to the u and d quarks. Note that the scalar polarisability, d , encodes the strength of the 3-body force on the H. This is known to be sensitive to the free bag radius in the MIT bag model, R_N^{free} , which is used to confine the quarks. Because the H is a 6-quark state, R_H^{free} is bigger than R_N^{free} . Mulders and Thomas found that $R_H^{free} = 1.2 \times R_N^{free}$ [2]. Thus the effective mass of the H is expressed as above in Eq. (5). We use $M_H = [2247, 2258, 2269]$ MeV as suggested in Ref. [5].

NS are taken to be at zero temperature and electrically neutral. The β -equilibrium condition must satisfy electrical charge and baryon number conservation. The H is electrically neutral but has a baryon number of 2. Thus, the total baryon number density is $n_B = \sum_f n_f + 2n_H$, where n_f is summed over the baryons and n_H is the density of the H.

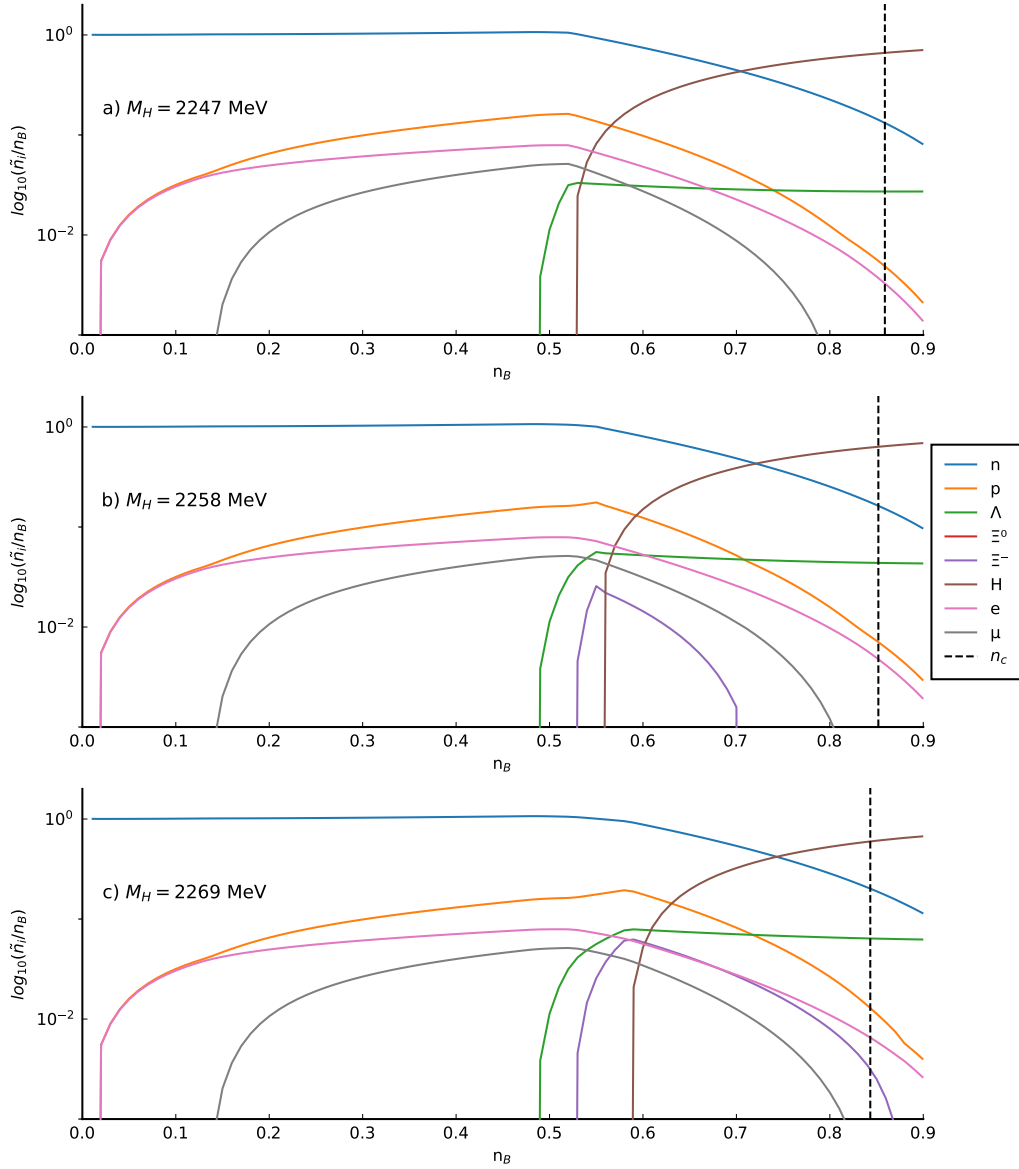


Figure 2: The EVE species fractions for a) $M_H = 2247$ MeV, b) $M_H = 2258$ MeV, and c) $M_H = 2269$ MeV. The black dashed lines indicate the central number density, n_c , of the maximum mass NS.

To model the short distance repulsion crucial to the NS EoS [13, 24] acting on all baryons, and the H, we use the excluded volume correction [25] previously used to analyse the case with only nucleons and hyperons [14]. The EVE number density is $\tilde{n}_f = \frac{n_f}{(1 - v_0 n_B)}$, with n_B defined above. Thus, we interpreted this as H having twice the excluded volume, v_0 , as the other baryons. For ease of comparison, we have chosen to use the same QMC parameters and a hard-core radius of $r = 0.45$ fm as used in Ref. [14], unless otherwise indicated.

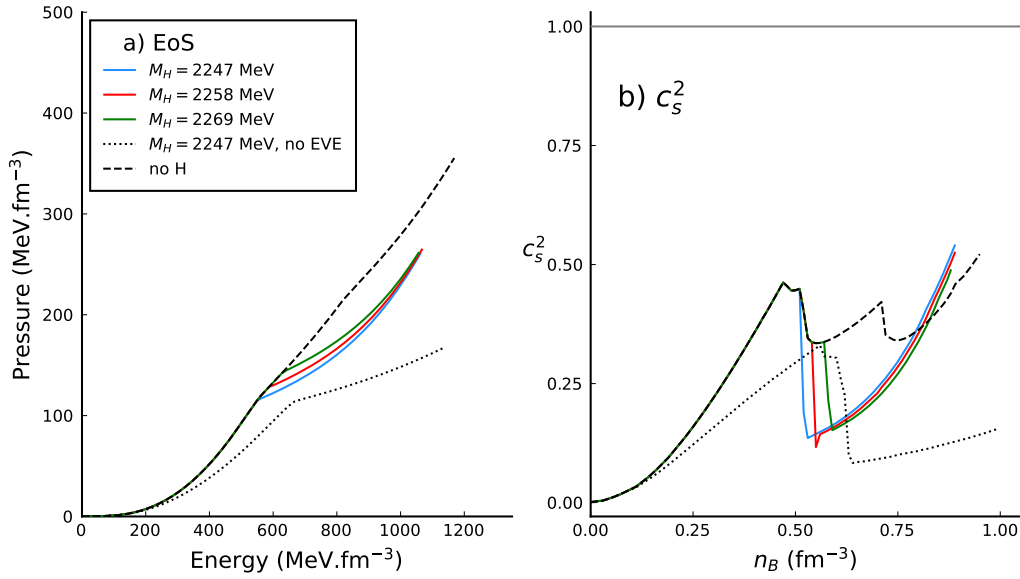


Figure 3: In a) we display the EoS with the accompanying b) speed of sound relative to light squared, c_s^2 . We have included the EoS without the H from Ref. [14] as the black dashed line. The dotted black curve are the results for $M_H = 2247$ MeV without the EVE.

3. Results and Discussion

Fig. 2 displays how the H particle affects the NS composition. We first note that since the chosen $M_H > 2M_\Lambda$, the H never appears before the Λ hyperon. The larger M_H , the larger the density when it appears. The appearance of the H increases the threshold density of the Ξ^0 , and as a consequence, no longer appears within the NS. For $M_H = 2247$ MeV, Ξ^- is also not present. Whether $\Xi^{0,-}$ appears is dependent on how soon the H-dibaryon appears. The vertical black lines indicate the central density (n_c) of the maximum mass neutron star. For larger M_H values, the central density is actually smaller. The H does alter the abundances of the nucleons and the hyperons, and near maximum, the H is the most populous particle within the cores of heavy NS.

In Fig. 3 we show the results for a) the EoS and b) c_s^2 , which is the speed of sound squared. EoS with H have less pressure than without H. We have added an additional EoS for $M_H = 2247$ MeV, without the excluded volume correction, to show that the QMC coupling strengths for $g_{\sigma,H}$ and $g_{\omega,H}$ can appropriately describe a star which is stable against compression. The massive loss of pressure corresponding to the appearance of the H, and $c_s^2 > 0$, indicates that the values of $g_{\sigma,H}$ and $g_{\omega,H}$ used in the QMC model do not lead to an unstable star.

It is known that the EVE may violate causality at higher densities. In Fig. 3 b) we show that $c_s^2 < 1$ in all cases, which satisfies relativity. It is interesting to see that with the H, the EoS is actually stiffer at high density. When the H appears at around $0.5 - 0.6$ fm⁻³ there is a significant loss of neutron degeneracy pressure. The same is true for hyperons. Without the H, the Ξ^0 appears at a little over 0.7 fm⁻³ [14], as seen by the dashed line falling suddenly in Fig. 3 b). Recall that the appearance of the H actually increases the threshold for the Ξ^0 above n_c for a maximum mass NS. Thus, when the H is present, there is no further softening of the EoS by the Ξ^0 (and Ξ^- for

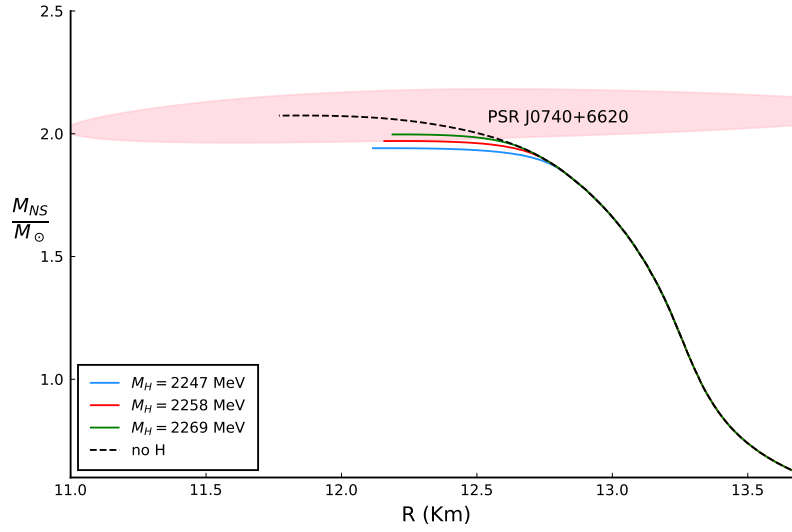


Figure 4: The TOV equation is used to produce the mass-radius curve for each of the EoS. The observed NS constrained used here is PSR J0740+6620 [27].

$M_H = 2247$ MeV). However, without the H, the EoS does suffer from further softening from the appearance of the Ξ hyperons.

The stiffer EoS at high densities, when the H is included, does not, however, translate to heavier NS. In Fig. 4 we show that the introduction of the H leads to a slight reduction of M_{Max}^{NS} . The closer M_H lies to the $\Lambda - \Lambda$ threshold, the more the decrease in M_{Max}^{NS} . Once the H appears the softening of the EoS leads to a mass plateau where the mass of the star hardly rises but becomes more and more compact. The results also show that smaller M_H leads to a smaller radius at M_{Max}^{NS} . Note that the H does not appear for low mass stars and thus the tidal deformability is unaffected at $\Lambda_{1.4} = 560$ [26].

4. Conclusion

Our results do indicate that the H particle can be successfully incorporated into QMC with natural couplings to the σ and ω fields. With $g_{\sigma,H}$ and $g_{\omega,H}$ fixed, the mass of the H determines the density at which the H appears at β -equilibrium. The H appears shortly after the Λ hyperon and leads to only a slight reduction of the NS maximum mass. The H is highly abundant and in the heaviest of NS, it is predicted to be dominant, suggesting that the cores of these stars have a sizable H-matter condensate.

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